1	Multicriteria asset management strategies for mixed transit fleet
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1 ABSTRACT

2 Agencies and policymakers require equitable and optimal allocation of funds among transit agencies for 3 not just regular operations and maintenance, but also for asset management including purchase of new buses 4 and rehabilitation of aging fleet. The paper proposes a hierarchical structure of resource allocation model 5 where federal funding is routed through the state, and ultimately to local transit agencies. The multicriteria 6 framework encompasses multiple dimensions such as selection of different improvement program options 7 (rehabilitation, remanufacturing, and replacement) of a mixed transit fleet spread over a temporally 8 continuous planning period. It leverages optimization models for capital allocation among transit agencies 9 in the state. Four sub-models are developed-two maximizing passenger miles traveled, and the other two 10 maximizing the total fleetwide remaining life, all under agency-specific budget, capacity and policy 11 constraints, and planning objectives. They are applied on real-world data from set of transit agencies spread 12 across the state of Tennessee, containing a heterogenous fleet of 254 total buses at various levels of aging. 13 Results indicate that by application of the framework, an average 40 percent additional mileage is generated 14 through the planning period with the same levels of fleet size, with nearly 30 percent of the fleet receiving 15 some form of improvement treatment per year.

Keywords: optimal resource allocation, transit asset management, rehabilitation and replacement, integer
 programming, branch and bound algorithm

1 **1. INTRODUCTION**

2 Local transit agencies often possess an aging bus fleet and must regularly allocate funds and 3 programs for fleet maintenance and upkeep. However, they must do so with limited resources, depending 4 most commonly on federal support. Recent surveys from 2012 indicate that public transit agencies spent 5 close to \$16.9 billion on capital investments, out of which annually authorized federal funding comprised 6 36 percent of these capital expenditures (FTA, 2015). For the remaining share, they rely on state and local 7 governments. Two main objectives for these funds include full replacement of old buses, and/or 8 rehabilitating some fleet to add extra service life. Ideally a bus at the end of its service life needs to be 9 replaced, but it is not always easy for many states to procure the matching funds for new buses for their 10 agencies. In such cases, various rebuilding alternatives are considered which, however, are not long-term 11 solutions.

12 Decision-making regarding replacement and timely rehabilitation thus becomes a critical 13 management aspect which requires a robust fund allocation mechanism to support such decisions. Complete 14 replacement may be the most desirable option from a quality perspective, but keeping budget constraints in mind, this option is not always readily available. Thus, the real challenge for agencies lies in finding an 15 16 optimal balance between the fraction of the total fleet selected for rebuilding and replacement. These 17 challenges form the key motivation for the current study, and the problem addressed here is typical of many 18 state Departments of Transportation (DOTs) in the U.S. that financially support their constituent transit 19 agencies.

Several studies have explored the economics of purchasing new buses versus rebuilding of existing buses. Khasnabis and Naseer (2000) found that it may be cost-effective to rebuild an existing bus by extending its effective life by a few years at a fraction of the procurement cost of a new bus, but only up to a certain limit. Another study developed a two-stage linear programming model to allocate resources among different improvement programs (Khasnabis et al. 2004). A few more recent studies explored optimization of different surrogates such as maximizing service life including Remaining Life (RL) of the overall fleet

(Mishra et al. 2010), maximizing the total system weighted average remaining life (TSWARL) (Mathew et 1 2 al. 2010), and minimizing net present cost (NPC) of investment (Mishra et al. 2013). The current study 3 builds upon these previous models, but from the operations point of view uses a new approach by optimizing another surrogate of quality of service- total passenger miles traveled (PSM) and uses a mixed fleet 4 5 (varying size and capacity) rather than a homogeneous one. The proposed framework addresses three key 6 dimensions for statewide transit fleet management, including choice of rebuild/replace option, 7 proportioning funds across agencies, and disbursement over time. The model is formulated as an asset 8 management problem that can be interfaced with the state DOT's long-term strategic transit plans.

9 The remainder of this paper is organized as follows: Section 3 covers the methodology, including 10 a general overview of the framework, and the detailed optimization model formulation. Section 4 presents 11 a real-world case study application of the proposed model, and covers a numerical analysis of the solutions 12 method and the results obtained therein. Section 5 concludes the paper by summarizing the study 13 contributions and implications for policy and practice, and describes potential future research avenues.

14 **2. LITERATURE REVIEW**

15 The literature review primarily focuses on the strategic resource allocation for fleet replacement 16 and rebuilding programs. Resource allocation under fixed budget and competing requirements are covered in many different areas including operations research, manufacturing, finance, and transportation 17 18 infrastructure (Ross 2000; Sheu 2006; Melachrinoudis and Kozanidis 2002; Ahmed 1983). Studies covering 19 asset management problems from the transit planning domain also include a variety of topics, such as 20 resource allocation to various agencies (Forkenbrock and Dueker 1979; Forkenbrock 1981), determination 21 of location, size and number of transit centers (Uyeno and Willoughby 1995), allocating fleets in 22 transportation networks (Diana, et al. 2006), and the dilemma of purchasing new buses or retiring old buses 23 (Simms et al. 1984; Khasnabis et al. 2002). Some studies exploring fleet management solutions covering 24 the needs of replacement and/or rebuilding of buses include Balzer et. al (1980), Rueda (1983), and Davenport (2005). 25

1 These problems have typically been formulated as linear programming or non-linear programming, 2 integer, mixed integer and dynamic programming models. (Ahmed 1983; Ariaratnam and MacLeod 2002; 3 Srour et al. 2006; Uyeno and Willoughby 1995; Melachrinoudis and Kozanidis 2002; Kozanidis and 4 Melachrinoudis 2004). Solution methods for these optimization problems are chosen depending on the 5 nature of the problem, although traditionally, they are solved by various forms of gradient search methods 6 (Deb 2001) that assume the search space to be uniform and unimodal for a unique solution. Since most 7 practical problems encountered in practice happen to be non-convex, some other ways to solve them are 8 employed, including Genetic Algorithm (GA), a general purpose robust solution algorithm (Mathew and 9 Mohan, 2003; Karlaftis et al. 2007; Deb 2001), and Branch and Bound Algorithm (BBA) to deal with 10 integer variables and constraints (Haggag 1981; Pillai 1998; Horn 2004; Mishra et al. 2013).

The literature lacks studies that develop resource allocation of mixed transit fleet to answer the question—"*with limited budget, how to allocate funds to constituent agencies to maintain at least the same number of fleet in a planning period, when each agency has a variety of buses (by age and size), and how to decide whether to replace, rehabilitate or to rebuild the existing buses.*" This paper develops a comprehensive mathematical programming model for funding allocation among a set of transit agencies for fleet management. A Branch and Bound Algorithm (BBA) is used as the solution method given its scalability for handling large problems.

18 **3. METHODOLOGY**

19 **3.1. Modeling Approach and Assumptions**

The paper represents a hierarchical structure of U.S. federal support for transit agencies, where the Federal Transit Administration (FTA) allocates the funding among state departments of transportations (DOTs, (Tennessee DOT, TDOT in this case)), which further distribute it among their constituent local transit operators. The funds are meant to keep the fleet in productive and safe operation within its minimum normal service life. Buses reaching their service life are eligible for replacement using these funds. However, under many practical scenarios, operating budgets may not be sufficient to guarantee funds for a full replacement, or the state DOTs are unable to furnish matching funds. In such cases funds may be allocated to only partially replace a part of the fleet, and partially rehabilitate the remainder using a variety of rebuilding program options, thus extending the service life by a few years. The remaining life can be extended by nearly four to ten years depending on the nature of the program and the size/characteristics of the bus, and studies such as Khasnabis et al. (2003) have shown that remanufacturing/rehabilitating of buses, if done properly, can be a cost-effective option.

Four total maintenance options are considered in this study, including three levels of rehabilitation 7 8 (REHAB1, REHAB2, REHAB3) each extending the service life by a limited number of years, and one 9 complete replacement option. In terms of size, buses are classified into small, medium, and large based on 10 its capacity, in accordance to a 2007 FTA study (FTA, 2007). The whole statewide fleet is considered where 11 30% of the fleet is categorized as small, 40% as medium, and the remaining 30% as heavy. Table 1 shows 12 a summary of the options considered, their expected benefits and costs associated with them. The costs of implementing each option vary by type of bus based on capacity. The information is based on real-life or 13 14 observed costs reported by the FTA. Fleet maintenance options above represent general bus rehabilitation 15 and rebuilding practices, that have been studied in the literature on the needs and experiences of the transit industry (Balzer et al. 1980; Felicetti 1985; Khasnabis and Naseer 2000). 16

17 **Table 1**

18	Fleet maintenance	options and	investment costs	(adapted)	from FTA, 2007)	•
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Maintenance	Cost Range by Fleet Size (Seat Range)										
Type (Years)	Small	Medium	Heavy								
REHAB1 (2 years)	\$3,000-\$6,600 (3-12 seats)	\$10,000-\$20,000 (13-24 seats)	\$36,000-\$106,200 (25-50 seats)								
REHAB2 (4 years)	\$5,400-\$11,880 (3-12 seats)	\$18,000-\$36,000 (13-24 seats)	\$65,000-\$191,750 (25-50 seats)								
REHAB3 (6 years)	\$7,500-\$16,500 (3-12 seats)	\$25,000-\$50,000 (13-24 seats)	\$90,000-\$265,500 (25-50 seats)								
REPLACE	\$15,000-\$33,000	\$50,000-\$100,000	\$180,000-\$531,000								
(8-12 years)	(3-12 seats)	(13-24 seats)	(25-50 seats)								

1 Some working assumptions are made regarding implementation of rehabilitation and replacement 2 policies. It is assumed that over the course of a planning horizon, for an individual bus, any rehabilitation 3 or replacement option may be implemented only once. A bus reaching the end of its remaining service life 4 must receive some form of maintenance. Also, however, a bus cannot receive more than one form of 5 maintenance in the same year. In terms of spending, it is assumed, that the spending costs may not exceed 6 the available budget though carry-over of funds from a future year are allowed as long as the total allocated 7 cost does not exceed the planning period budget. The assignment of a particular maintenance option to a 8 bus in a certain year is a decision variable that is decided by the optimization problem, and a bus may 9 receive more than one rehabilitation option before being selected for complete replacement.

10 A few different planning options are modeled and presented for comparison, represented through 11 four sub-models. In the first one, a fleet may be selected for a maintenance option a few years before the 12 end of its service life. This scenario is mileage-based and maximizes PSM, and is categorized under Total Passenger Miles Maximization Based Allocation (TPSMBA). It is henceforth referred to as "PSM 13 14 Scenario". Next, a more stringent strategy is evaluated wherein a bus is only eligible to receive improvement 15 when it is at the end of the remaining life (or service life is nearly zero). This scenario is a Minimum Normal 16 Service Life Based Allocation, and thus referred to as the "PSM-MNSL Scenario". The policies under this 17 scenario are relatively more conservative than PSM. The third and fourth scenarios are service life-based, 18 and are categorized as Minimum Normal Service Life Based Allocation (MNSLBA). The third scenario 19 maximizes the total remaining life (RML) of the fleet and is thus referred to as the "RML Scenario". The 20 fourth scenario is again a relatively more constrained where is the objective is to still maximize Total 21 Remaining Life like the third scenario, but a bus in this case is only eligible to receive maintenance when 22 its remaining life is depleted. This scenario is thus referred to as the "RML-MNSL Scenario". Ultimately, 23 a "Do-Nothing Scenario" is also evaluated where the agency does not use any form of resource allocation 24 framework. The relative benefits in terms of costs, surplus, and additional passenger miles generated, and 25 compared across the four different scenarios.

1 **3.2. Model Formulation**

2 3.2.1. PSM Scenario

The model is formulated as an optimization problem where the objective is to maximize PSM. Since each option adds some years to the service life of a bus, PSM quantifies the effectiveness of the maintenance in terms of additional passenger travel made possible by the treatment. It is thus a resulting surrogate of service life extension of a bus receiving maintenance treatment of any kind as mentioned above. The model is a variant of a resource allocation problem of the fleet for all the agencies over the entire planning period, subject to budget, demand, rebuild, and non-negativity constraints. This formulation is given below preceded by an explanation of notations:

10 Notation

Sets

Ι	Active buses in the fleet
М	Years within the analysis period (planning horizon)
Κ	Available maintenance options
Parameters	
В	Annual state DOT budget
ρ	Ratio of maximum allowable expenditure versus annual budget
C _i	Capacity of bus <i>i</i>
a _i	Current active miles of bus <i>i</i> as of the first year of analysis
y _i	Current age of bus <i>i</i> at of the first year of analysis
r _{im}	Current remaining life of bus <i>i</i> at year <i>m</i>
μ	Interest rates for funds borrowed
cs _m	Cumulative surplus at year <i>m</i>
l ^k	Additional life generated by a maintenance option k
j_m^k	Cost of maintenance option k at year m

PSM Total additional passenger miles generated through year *m* of planning

 θ_{im} Parameter for MNSL, 1 when the remaining life is zero, and zero otherwise

Decision Variables

 $x_{im}^{k} = \{0,1\}$ 1 if improvement k is implemented on fleet i at year m year of the planning period, and 0 otherwise

1 The PSM Scenario is formulated as follows:

Maximize:

$$PSM = \sum_{m=1}^{M} \sum_{i=1}^{l} \frac{c_i a_i}{y_i} + \sum_{m=1}^{M} \sum_{i=1}^{l} \sum_{k=1}^{K} \frac{c_i a_i x_{im}^k l^k}{y_i} + \sum_{i=1}^{l} \frac{c_i a_i}{y_i} (r_{i1} - M)$$
 Equation 1

subject to:

$$\sum_{m=1}^{M} \sum_{i=1}^{l} \sum_{k=1}^{K} x_{im}^{k} j_{m}^{k} (1+\mu)^{(m-1)} \leq \frac{(1+\mu)^{M}-1}{\mu} B$$
Equation 2
$$\sum_{m+1}^{m+l^{k}-1} x_{im}^{k} \leq x_{im}^{k} (l^{k}-1) \quad \forall i \in I, m \in M, k \in K$$
Equation 3
$$\sum_{k=1}^{K} x_{im}^{k} + r_{im} \geq 0 \quad \forall i \in I, m \in M$$
Equation 4
$$\sum_{k=1}^{K} x_{im}^{k} \leq 1 \quad \forall i \in I, m \in M$$
Equation 5
$$\sum_{m=1}^{M} x_{im}^{k} \leq 1 \quad \forall i \in I, k \in K$$
Equation 6
$$r_{i(m+1)} = r_{im} - 1 + \sum_{k=1}^{K} x_{im}^{k} l^{k} \quad \forall i \in I, m \in M$$

$cs_m = B - \sum_{i=1}^{A} \sum_{k=1}^{K} x_{im}^k j_m^k + cs_{m-1}(1+\mu) \ \forall \ m \in M$	Equation 8
$cs_m \ge -B\rho \forall \ m \in M$	Equation 9
$x_{im}^k = \{0,1\}, \forall i \in I, m \in M, k \in K$	Equation 10

2 The objective function in Equation 1 maximizes PSM generated from the maintenance options. 3 Equation 2 ensures that the cost for the entire improvement program must not exceed the total budget. 4 Equation 3 state that one fleet cannot receive any improvement during the extended years due to the last 5 improvement. In other words, the constraint prevents a bus from receiving a new improvement treatment 6 until it completely exhausts the benefits it gains from a previous treatment option. Equation 4 addresses the 7 policy where a bus reaching a remaining life of zero must receive improvement. Equation 5 restraints that 8 no more than one maintenance option may be implemented on a bus in a given year. Equation 6 limits the 9 number of maintenance options that a bus can receive over the planning period to one. Equation 7 develops 10 the linkage between the growth in remaining life as a result of the benefit of improvement. Equation 8 11 explains the compounded growth of the budgetary cumulative surplus from the previous year to the current 12 year. Equation 9 is a budgetary constraint indicating that funds borrowed cannot exceed the available credit 13 line or budget. Equation 10 defines the decision variable as binary variable where 1 indicates that an 14 improvement measure was implemented, and zero otherwise.

15 3.2.2. PSM-MNSL Scenario

As discussed earlier, the key difference in this scenario is that a bus is eligible to receive an improvement option only if its remaining life is zero. The parameter θ_{im} is a binary variable that take value of 1 when the remaining life is zero, and zero otherwise.

19 PSM-MNSL is formulated as follows:

20

1

Maximize

Equation 11

$$TPSM = \sum_{m=1}^{M} \sum_{i=1}^{l} \frac{c_i a_i}{y_i} + \sum_{m=1}^{M} \sum_{i=1}^{l} \sum_{k=1}^{K} \frac{c_i a_i x_{im}^k l^k}{y_i} + \sum_{i=1}^{l} \frac{c_i a_i}{y_i} (r_{i1} - M)$$

subject to:

$$\sum_{k=1}^{K} x_{im}^{k} = \theta_{im} \quad \forall i \in I, m \in M$$
 Equation 12

And Equations 2-10 mentioned under the TPSMBA Scenario.

The objective function in Equation 11 maximizes PSM generated from the maintenance options.
 Equation 12 addresses the policy that the bus can only receive improvement if and only if its remaining life
 is zero and only one improvement can be made per situation.

4 3.2.3. RML Scenario

5 In this scenario, the total remaining life across the entire fleet run is maximized. It follows the regulation

6 and policy of the PSM scenario, the only difference being the objective function.

7 RML is formulated as follows:

Maximize

$$RML = IM + \sum_{m=1}^{M} \sum_{i=1}^{l} \sum_{k=1}^{K} x_{im}^{k} l^{k} + \sum_{i=1}^{l} (r_{i1} - M)$$
 Equation 13

subject to: Equations 2-10 mentioned under the PSM Scenario.

8 The objective function in Equation 13 maximizes RML benefited from the maintenance options

9 3.2.4. RML-MNSL Scenario

- 10 In this scenario, again the total remaining life across the entire fleet run is maximized. It follows the
- 11 regulation and policy of the PSM scenario and the only difference is the objective function. However it

- 1 takes into account a relatively less flexible policy where a bus is not eligible to receive any form
- 2 improvement treatment until it reaches the end of its current service life.
- 3 RML-MNSL is formulated as follows:

Maximize

$$RML = IM + \sum_{m=1}^{M} \sum_{i=1}^{I} \sum_{k=1}^{K} x_{im}^{k} l^{k} + \sum_{i=1}^{I} (r_{i1} - M)$$

Equation 14

subject to: Equations 2-10 mentioned under the PSM Scenario and equation 12 under the PSM-MNSL Scenario

4 The next section covers the application of the above model to a real-life case study, and the 5 subsequent numerical analysis.

6 4. CASE-STUDY APPLICATION AND NUMERICAL ANALYSIS

7 4.1. Study-Area Description and Working Parameters

8 The State of Tennessee is considered in this study, where 15 agencies are expected to receive 9 funding to provide maintenance support for their aging fleet. As part of the optimal resource allocation 10 framework, it is required to determine the most appropriate amount of funding for these agencies. The 11 dataset containing key information on the fleet for model development and application, is obtained from 12 the National Transit Database (NTD), maintained by the FTA. The NTD records the financial, operating 13 and asset condition of transit systems across the country. Data obtained from the NTD for this case study 14 are thus 'known parameters'. Agencies report to NTD their operating fleet which includes these parameters. 15 For a typical fleet, the manufacturing year and the capacity of the bus, total active miles counted to the 16 point of the report, average lifetime miles are known.

In addition, certain parameters are derived from these known parameters which are used in the model development. They are listed as follows current age of fleet, remaining life of fleet, size of bus. In terms of funding, each year TDOT with an annual budget of \$5 million to be further distributed among its agencies. In case of a budget shortfall, the state agency can borrow additional capital, although at an interest

1 rate. The system revenues and surplus (if any) can then be used to repay the debt and interest. The interest 2 rates are assumed to be 5% per year compounded annually. Also, it is assumed that the agency cannot 3 borrow an amount more than 30% of the annual budget, to reflect credit line regulations that may cap the 4 borrowing.

5 **4.2.** Solution Approach

6 The case study contains a total fleet size of 254 individual buses belonging to a total 15 transit 7 agencies that operate on a capital-funding program administered by TDOT. Each bus has a different level 8 of remaining life, capacity, and other characteristics. Considering these 254 buses, each eligible to receive 9 one of the four maintenance options discussed earlier, over a ten-year analysis period, there are over 10,000 10 decision variables in the optimization structure, thus making it a fairly large problem. A Branch and Bound 11 Algorithm (BBA) solution approach is used. This is an enumeration approach for solving various problems 12 especially in discrete and combinatorial situations, including integer programming (IP). The decision 13 variable in the current study are integers (improvement options). Application of BBA is common for transit 14 fleet resource allocation (Mishra et al., 2013).

15 4.3. Results and Discussion

16

The results highlight both the total costs and benefits associated with implementing each planning 17 scenario, and the variations across fleet type and different budgetary allowances.

18 Table 2

	Tota	l Passenger I	Miles (Bill	ions)	Total Remaining Life (Years)				
Model	Small	Medium	Heavy	Total	Small	Medium	Heavy	Total	
PSM	0.35	0.90	5.34	6.58*	1,354	1,726	1,406	4,486	
PSM-MNSL	0.33	0.87	5.00	6.20	1,244	1,606	1,332	4,182	
RML	0.36	0.93	4.51	5.80	1,636	2,068	1,334	5,038*	
RML-MNSL	0.34	0.92	4.60	5.60	1,388	1,774	1,326	4,488	

19 Comparison of objective function between different models

²⁰ Notes: *Indicates the maximum value for the objective function

1 As seen in the resulting objective function values shown in Table 2, the PSM or RML relaxed 2 scenarios perform better in terms of their objectives compare to the restricted models. The PSM scenario 3 returns the highest benefits in terms of additional mileage generated fleetwide, whereas the RML model 4 does the same in terms of expanding the fleetwide remaining life. Figure 2 below shows the trends of the 5 total remaining life of the fleet under various resource allocation scenarios over the next ten-year planning 6 period. The scenario is also compared to the do-nothing option where the agencies do not implement any 7 maintenance program and the buses in their current form are not rehabilitated. The total remaining life of 8 the entire fleet through the ten-year planning period under each of the planning scenarios is shown in Figure 9 1(a) below. Additionally, Figures 1(b,c,d,e) show the total remaining life by fleet type (under all five model 10 scenarios).





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1(a) Total remaining life of mixed fleet under different planning scenarios



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2 It can be seen that under the PSM scenario where rehabilitation programs are implemented sooner, 3 total remaining life is higher than in both scenarios. Also, in the do-nothing scenario, the total remaining 4 life gradually drops to zero by the end of the planning period. The total remaining life of the fleet under the 5 PSM scenario also increases at a much faster rate than the more conservative MNSL through 2025, whereas 6 it nearly flattens out by 2021 under the do-nothing scenario because no life-extension policies are 7 implemented. In terms of total remaining life of different fleet type, all three sizes of buses receive nearly equitable benefits through the service life under PSM scenario, however heavy buses are expected to gain 8 9 the most by 2025 – an average of two years more than medium and small buses.

Benefits of implementing a resource allocation optimization framework are further quantified by evaluating the objective function (PSM) under various conditions, and are illustrated in Figure 2 below. The first Figure 2(a) shows the total benefits yielded in terms of total mileage the entire fleet can run each year until it is depleted. Figure 2(b) and 2(c) shows the total passenger miles added for the four planning scenarios distributed by type of fleet (there are no additional passenger miles generated in the do-nothing scenario).





7 8

It may be noted that as in the case of total remaining life, the mileage benefits are also achieved at a faster rate under the more flexible PSM scenario. Also, heavy buses gain additional benefits over the course of the planning period compared to small and medium sized buses under four planning scenarios. Additional insights are developed on the objective function by exploring the correlation between the value of the objective function (PSM) under the PSM scenario with the number of buses improved under each of the four improvement options. These relationships between the objective function and decision variables (buses under each improvement four options) are shown in Figure 3.





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Fig. 3. Relationship of PSM with improvement options

1 There appears to be a positive correlation between the frequency of application of each 2 improvement option and the objective function, indicating that higher the number of buses receiving each 3 improvement option, higher is the total additional passenger miles gained. Hence the new systemwide 4 benefits appear to be positively correlated with the frequency of implementation of improvement options 5 which indicates that the model performs as desired. However, REHAB3 does not follow this trend. By 6 observation, REHAB3 and replacement options are often the ultimate or penultimate improvement options 7 implemented on the fleet. However, given the costs associated with each option, REHAB3 is preferred 8 instead of full replacement. But at the same time, REPLACE generates more passenger miles in the long 9 run, and thus may be more effective. Thus, as budgetary conditions improve and spending becomes more 10 flexible, REHAB3 is replaced by the REPLACE option.

Fiscal considerations are also important in successful implementation of the programs. Given the budgetary constraints in the model, the proposed optimization framework can control costs through the planning period. Figure 4(a) compares the annual spending expected under various planning options, and the available budget, whereas Figure 4(b) illustrates the funding by type of bus based on capacity.



15 16

4(a) Annual spending compared to available budget



(b) Funding allocation by type of fleet for PSM and PSM-MNSL scenario

2

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Fig. 4. Costs of implementing systemwide fleet improvement programs

4 In terms of annual spending under the two planning scenarios, the PSM-MNSL scenario requires 5 much less initial funding as expected, since several buses may not be too close to their service life in the 6 early planning period. However, in the second half of the period (2021 onwards specifically), the costs 7 increase significantly and exceed the available budget. By the end of the ten-year period in 2025, the 8 funding requirements are almost 50% higher than the available yearly budget of \$5 million. It is thus likely 9 to produce an environment of much financial uncertainty in the long term which may not be desirable. 10 Spending under the PSM scenario, on the other hand, is relatively steadier and even aligns with the available 11 budget in equilibrium in the outer years (2024 onwards). The heterogeneity of the fleet in terms of capacity 12 also plays a role in funding allocation across the fleet. Also, it is observed that in the outer years, heavy 13 buses witness a larger increase in the passenger miles compared to small and medium-sized buses, while at 14 the same time the total proportion of funding allocated to them is also relatively higher.

The following plots go into details about funding allocation at the individual agency level. As mentioned earlier, 15 transit agencies spread across Tennessee are considered in this analysis. Figure 5(a) shows their geographical locations, and the existing fleet composition (small, medium, and heavy buses) as illustrated in the legend insert in the top left portion of the figure. A diverse mix of buses is observed across

- 1 agencies which captures the heterogeneity in fleet. Figure 5(b) reports the proportion of the total funding
- 2 allocated to each of the 15 statewide transit agencies considered in this study, while Figure 5(c) shows the
- 3 additional passenger miles traveled, distributed by agency.

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5(a) Geographical locations and fleet composition of transit agencies



5(b) Planning period expenditure allocation by transit agency





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5(c) Planning period passenger miles by transit agency

Fig. 5. Distribution of costs and benefits by agency through planning period (2016-2025).

5 It can be noted that the distribution of state funding across the 15 agencies considered in this study 6 is driven by the prevalent condition of fleet in the agency and in proportion to the respective individual fleet 7 size. More funds are directed to agencies operating a higher proportion of the total fleet. Also the benefits 8 associated with the resource allocation in terms of additional mileage generated are proportional to the 9 proportion of spending in each case.

Additional detailed results of the PSM scenario are presented in Table 3 below, including a distribution of remaining life across the fleet for each planning year, and the number of buses receiving each kind of improvement option (REHAB1, REHAB2, REHAB3, and REPLACE). Results on total annual spending per year expected in the future years and corresponding trends of the benefits gained in terms of PSM are also included. The last column indicates the proportion of fleet receiving some form of improvement treatment per year.

1 Table 3

		Distribution of Remaining Life							Life			Improvement Options				Annual Spending	TPSM	%Fleet	
Year	0	1	2	3	4	5	6	7	8	9	>=10	REHAB1	REHAB2	REHAB3	Replacement	(\$ mn)	(bn)	Improved	
2016	38	21	24	41	47	34	25	16	7	0	1	31	39	36	5	\$7.00	0.82	44%	
2017	11	40	40	49	16	19	14	5	13	18	29	9	30	22	1	\$4.62	0.82	24%	
2018	24	36	39	14	20	22	15	21	29	15	19	5	9	41	4	\$4.54	0.65	23%	
2019	4	39	17	21	29	34	41	30	15	15	9	1	11	28	3	\$4.02	1.05	17%	
2020	6	16	20	26	40	43	58	18	15	6	6	3	3	1	44	\$4.57	1.63	20%	
2021	6	15	25	40	36	48	13	17	9	6	39	0	0	1	37	\$4.99	1.38	15%	
2022	10	21	30	29	46	13	13	10	8	6	68	0	0	0	34	\$4.99	1.14	13%	
2023	10	29	27	45	8	11	8	9	12	11	84	0	0	0	41	\$5.00	1.09	16%	
2024	19	23	34	6	9	7	8	14	14	22	98	0	0	0	35	\$5.00	1.04	14%	
2025	9	34	6	9	5	8	14	20	27	39	83	0	0	0	33	\$5.00	1.97	13%	

2 Summary of PSM scenario results.

3

4 The total fleet size across all 15 agencies considered in this study is 254 as mentioned earlier. The 5 annual spending is close to the available annual budget of \$5 million in each year, where an average of 6 about 30% of the total fleet receive some form of improvement per year. The proportion of fleet receiving 7 improvement is higher in the earlier years and lower in the outer years after 2022 which is intuitive. Also, 8 the number of buses undergoing the final replacement option is lower in the earlier years and higher in the 9 later years, whereas inversely an opposite trend is observed across the other three rehabilitation-based 10 options. This again makes intuitive sense because the rehabilitation options are relatively cheaper to 11 implement and also add fewer years of life compared to the full replacement option, and hence may be 12 more optimal to implement sooner rather than later. It is interesting to note that the number of buses with a 13 remaining service life of more than or equal to 10 years increases gradually over the planning period, as 14 they receive one or more forms of improvement over the years. This indicates that the suggested model and 15 its optimization routine proceed as desired, and generate cumulative benefits over the years.

16 **5. CONCLUSIONS**

17 5.1. Summary of methodology and numerical findings

18 The model developed in this study provides a resource allocation framework across a mixed 19 statewide fleet consisting of buses of various capacities and remaining life. Four types of fleet life 20 improvement options (three levels of rehabilitation, and full replacement) are implemented among several

constituent agencies over a planning period in an equitable manner, based on prevailing characteristics of
 their existing fleet.

3 Two scenarios are implemented to reflect different planning or policy objectives of agencies in 4 real-life that may be driven by budgetary or other local constraints. The PSM and RML scenarios are more 5 flexible where they allow for an improvement option to be implemented on buses at any stage of their 6 service life, whereas under the corresponding Minimum Normal Service Life Based scenarios (PSM-7 MNSL, and RML-MNSL), a bus may be eligible to receive improvement only when it has reached the end 8 of its service life. For both scenarios, an integer programming-based resource allocation model is developed 9 with the objective of maximizing the PSM under several constraints including budgets, agency-specific 10 policies regarding borrowing funds, etc. PSM reflects the benefits quantified in terms of additional 11 passenger miles generated across the system over the coming years. A branch and bound algorithm is 12 implemented to solve the large-sized optimization model (with more than 10,000 total decision variables), 13 and a case-study of 15 transit agencies spread across Tennessee is presented. Both scenarios are compared 14 to a 'do-nothing' scenario to articulate the benefits of setting up an optimal resource allocation framework 15 over a simple fixed funding allocation.

Model results shows that PSM improves with the number of improvement options of each kind (REHAB1, REHAB2, REHAB3, and REPLACE) under various budget levels. Comparison between two planning objectives indicate that TPSMBA scenario may be more beneficial in the long-run compared to the MNSLBA scenario. Detailed results for the TPSMBA scenario illustrate merits of the proposed model, where it is evident that average remaining life of buses (or share of fleet with more than ten years of remaining service life) gradually rises towards the later years of the planning period (2016-2025).

22

5.2. Planning and policy implications

The case-study findings have several policy and planning contributions. Unlike previous studies in this domain where improvement options are applied individually for a specific year in the future for a single agency, the current model is more flexible where it can be applied over a temporally continuous planning horizon and across multiple agencies under the purview of a state agency. It is also multicriteria where size,
 budget and several policy constraints are considered. Transit agencies or state officials may utilize the
 framework for more effective and optimal asset management to enhance the service life and performance
 of their fleet, while implementing financially viable policies and improvement programs.

5 Based on the resource allocation framework presented in this study and the objectives and financial 6 constraints specified therein, a transit agency's desired goal would be to invoke an improvement program 7 that yields the largest supply-side benefits in terms of additional mileage or remaining fleet-life generated. 8 In this regard, for the Tennessee case-study, model results (in Table 3) suggest that implementing cheaper 9 and basic rehabilitation options of varying degrees (REHAB1, REHAB2, REHAB3) is more preferable in 10 the earlier years, whereas more the expensive full replacement (REPLACE) option is more optimal in the 11 outer years when a larger proportion of the fleet approaches the end of its service life and when other short-12 term rehabilitation options may not suffice. At the statewide level, allocation distribution illustrated in Table 13 3 and Figure 5 can be developed by the governing agencies to manage and assign funds among its 14 constituent agencies through designated improvement programs over a planning horizon, to match desired 15 quality/level-of-service requirements under prevalent budget conditions.

16 **5.3. Future work**

17 There are several future research avenues following the current work. The resource allocation 18 framework presented here considers key two criteria- mileage and remaining life. However, it can be 19 expanded to include emissions and air quality based criteria, which may be particularly relevant in light of 20 the emphasis laid on environmentally sustainable urban transportation planning and programming. A more 21 heterogenous fleet containing hybrid or low-emission buses, coupled with environmentally driven 22 objectives and policies may lead to more diverse resource allocation outcomes. Along the same lines, the 23 'equity' component is not explicitly considered in this study where the total statewide funds are allocated 24 more equitably among its agencies. The current set of results on funding allocation across agencies 25 indicates a more uneven distribution of funds, mainly driven by fleet size and age of individual agencies.

Ultimately, additional supply-side operational variables such as mean distance to failure of buses may be
 incorporated into the modeling framework to make it more dynamic.

Although the current model is demonstrated on a Tennessee-based fleet comprising of small,

4	medium, and large sized buses, it is transferable to other study areas where local agency-specific data can
5	be acquired, most of which can be obtained from federal-level databases such as the NTD. The model can
6	thus serve as a useful asset management tool for local and state agencies that intend to implement fiscal
7	programs to preserve their aging fleet.
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