



Producing Broadband Synthetic Time Histories for Central and Eastern North America

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Outline:

- **Introduction**
- **Generation of Synthetics**
 - Engineering Approaches
 - Seismological Approaches
 - ✓ Stochastic Methods
 - ✓ Kinematic methods
- **The suggested Hybrid Broad Band Approach**
- **Sample Model Mw=6.5**
- **Case Study** : Application for Seismic Analysis of a Bridge in Memphis
- **Summary**

Introduction:

Generation of Synthetic Time Histories

- A promising solution in the absence of suitable real earthquake records in terms of M , R , and site characteristics are scarce

- **Applications:**

- **Time history analysis (Eng. viewpoint)**

- **Particular structures** (towers, power plants, dams, high tech facilities, base-isolated structures, and irregular buildings)
- **Dynamic nonlinear analysis** of structures is recommended by building codes

- **GMPEs (Seismological viewpoint)**

- Regions with historical seismicity while insufficient
- Complement of the available catalog

- **Goal:** Update GMPE **Pezeshk et al. (2011)** used by USGS

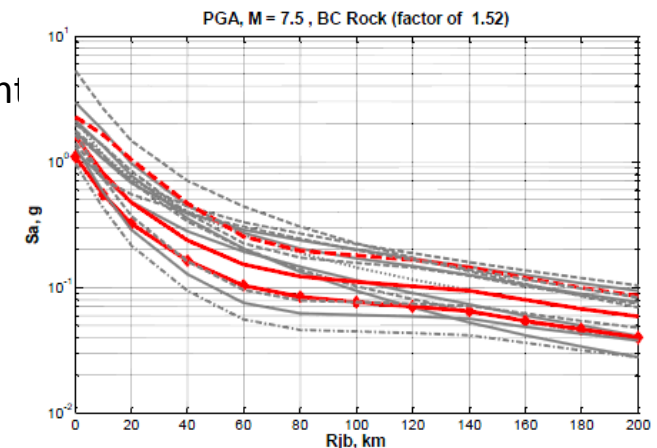


Figure is taken from Workshop on CEUS GMPEs for 2014 maps, Sanaz Rezaeian, Dec 12, 12, Berkeley, CA

Generation of Synthetic Time Histories (Cont.)

☐ Synthetic Generation Approaches:

- **Engineering:**

More focused on the **spectrum matching** of generated seismograms with a target spectrum (like UHS from PSHA, etc.)

- **Seismological**

- **Dynamic Models**

Complicated

Validate and simulate a scenario

- **Kinematic Models**

Low frequency in short distances

- **Stochastic Methods**

Point Source Stochastic (~SMSIM)

Finite-Fault stochastic methods (~EXSIM)

- **Hybrid Broadband (HBB)**

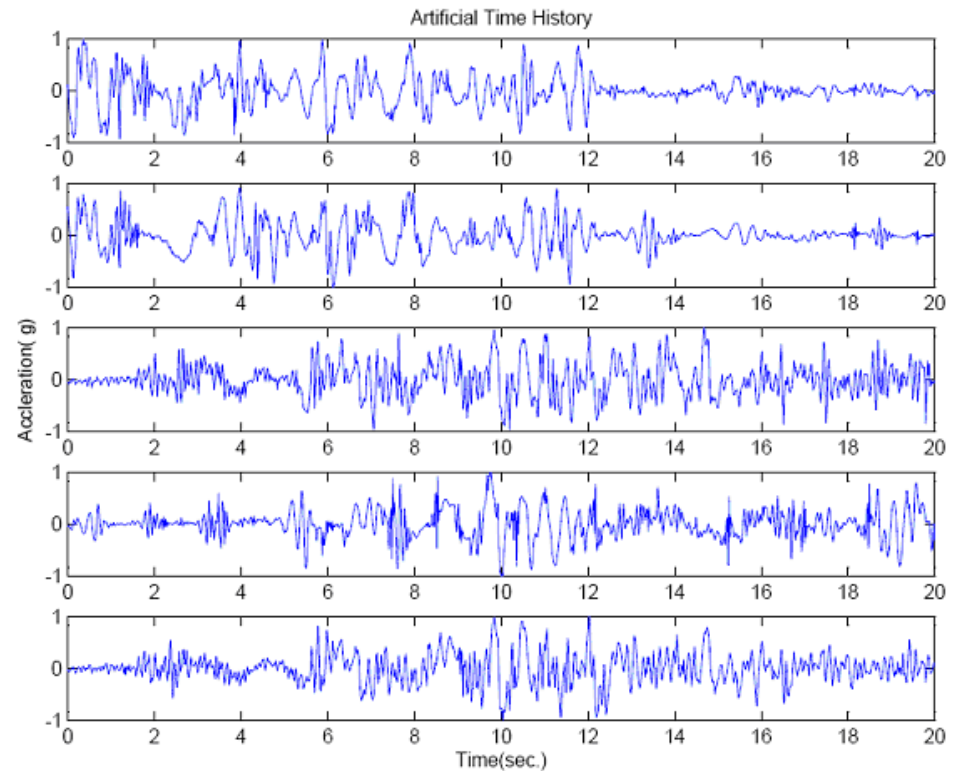
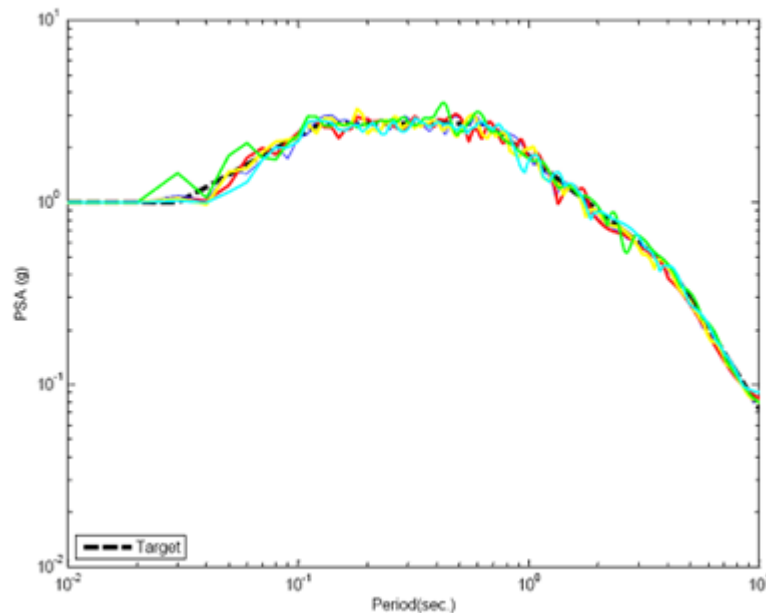
Low Freq.: Kinematic model of EQ source & Deterministic model of wave propagation

High Freq.: Uses Stochastic Method



Engineering approach-Spectrum Matching

- ✓ Different techniques in time/freq. domain
Fourier/Wavelet/GA/ANN/PCA etc.



G. Ghodrati Amiri, A. **Shahjoui**, S. Saadat and M. Ajalloeian; (2011), "Implementation of Genetic Algorithm, MLFF Neural Network, Principal Component Analysis and Wavelet Packet Transform in Generation of Compatible Seismic Ground Acceleration Time Histories," Journal of Earthquake Engineering (JEE); 15(1), 50-76

High freq. >> Stochastic

Low freq.>> Kinematic model of source and deterministic approach for path

□ Part A: Stochastic Methods

3 Main parameters: Source, Path, Site

➤ Part A-1: The source effect: $E(M_0, f)$

The most commonly used model of the earthquake source spectrum is the ω -square model

$M_0 f_0^3 = \text{constant} \gg \text{const. Stress drop } (\Delta\sigma)$ $f_0 = \text{Corner freq.}$

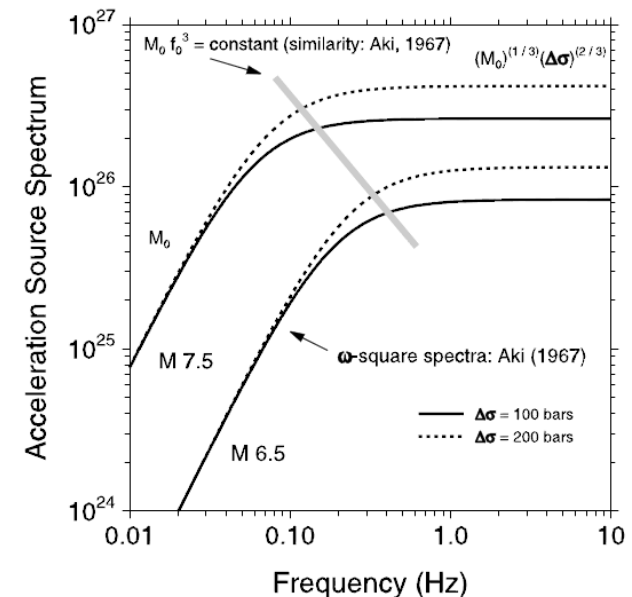
$$f_0 = 4.9 \cdot 10^6 \beta_s (\Delta\sigma / M_0)^{1/3}$$

β_s : Shear wave velocity(km/s); $\Delta\sigma$ (Bar); M_0 (dyne-cm)

F_0 : Static Corner Freq., Dynamic Corner Freq., Single, Double

$$E(M_0, f) = CM_0 S(M_0, f) \gg \underline{S(M_0, f) : \text{Disp. Source Spec.}}$$

$$S(M_0, f) = S_a(M_0, f) * S_b(M_0, f) : \underline{\text{shape of source spectral}}$$



➤ Part A-2: Path Effect, $P(R, f)$

$$P(R, f) = Z(R) \exp\{-\pi f R / Q(f)\} c_Q\}$$

$Z(R)$: Geometrical spreading

$Q(f)$: Seismic Attenuation = af^n

(Anelastic attenuation)

$$Z(R) = \begin{cases} \frac{R_0}{R} & R \leq R_1 \\ Z(R_1) \left(\frac{R_1}{R}\right)^{p_1} & R_1 \leq R \leq R_2 \\ \vdots & \\ Z(R_n) \left(\frac{R_n}{R}\right)^{p_n} & R_n \leq R \end{cases}$$

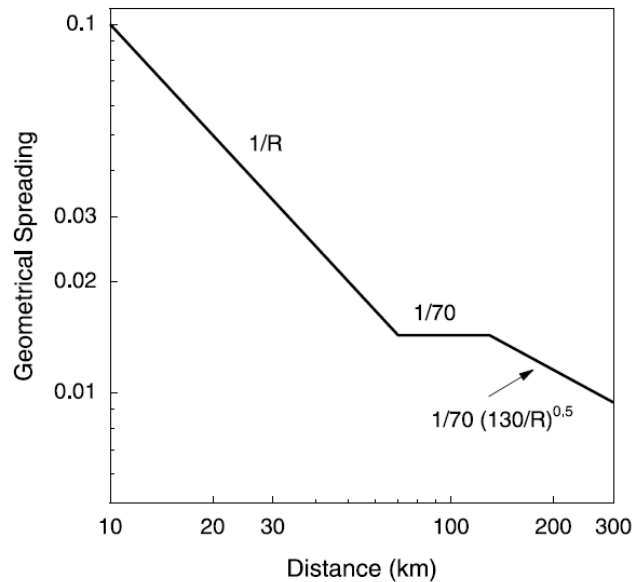
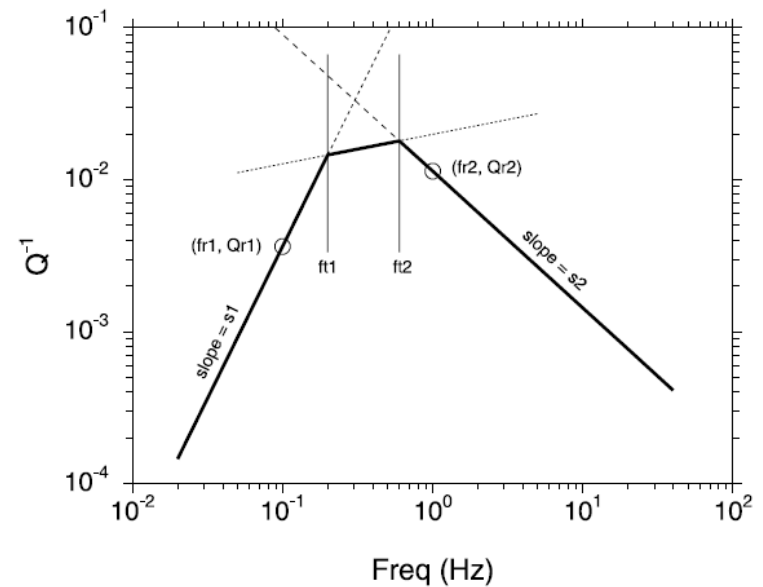


Figure 5

The geometrical spreading function used in applications in central and eastern North America by ATKINSON and BOORE (1995) and FRANKEL *et al.* (1996).



➤ Part A-3: Site Effect, $G(f)$

$$G(f) = A(f) * D(f)$$

$A(f)$: Amplification factor > relative to source

$D(f)$: Diminution function > path-independent loss of energy in high freq. > κ_0 (kappa)

$$A(f(z)) = \sqrt{Z_s / \bar{Z}(f)} \quad Z_s = \rho_s \beta_s$$

$$\bar{Z}(f) = \int_0^{t(z(f))} \rho(z) \beta(z) dt \bigg/ \int_0^{t(z(f))} dt$$

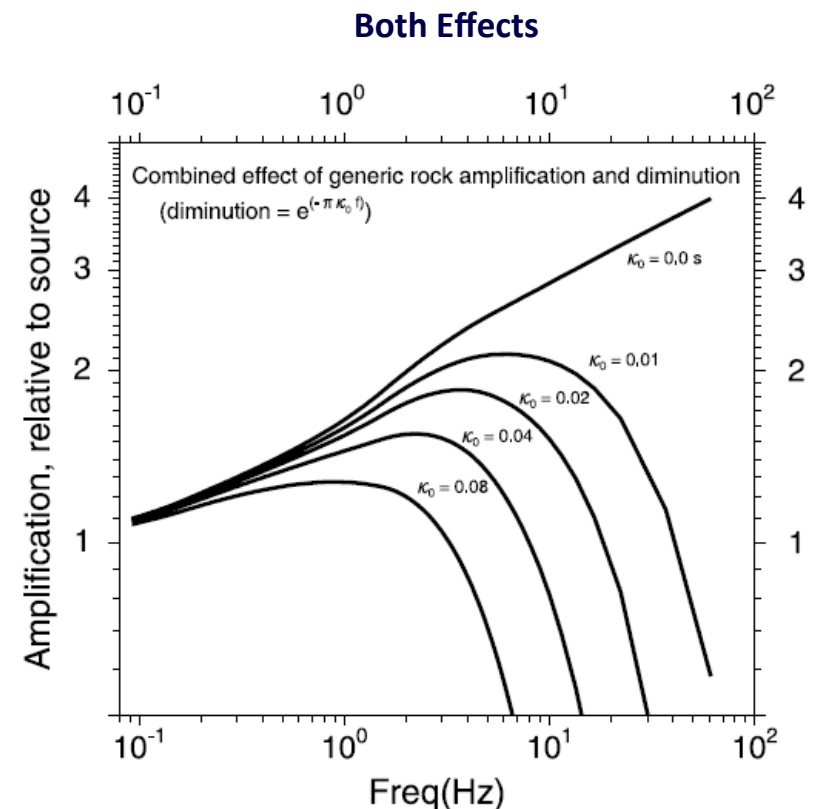
$$\bar{Z}(f) = \int_0^{z(f)} \rho(z) dz \bigg/ \int_0^{z(f)} \frac{1}{\beta(z)} dz$$

Two filters are in common use: the $f_{\max}$ filter

$$D(f) = [1 + (f/f_{\max})^8]^{-1/2}$$

(HANKS, 1982; BOORE, 1983), and the κ_0 filter

$$D(f) = \exp(-\pi \kappa_0 f) ,$$



Part A-4: Ground Motion Type, $I(f)$

Filtering:

$$I(f) = \frac{-Vf^2}{(f^2 - f_r^2) - 2ff_r\xi i}$$

f_r : undamped natural freq.

ξ : damping

V : gain(for response spectra: $V=1$)



Synthetic Generation> Seismological Approaches> Hybrid Broadband > **Kinematic Models**

Low freq.>> Kinematic model of source and deterministic approach for path

Kinematic Models:

Need to define shaking scenarios (faulting, slip, rupture, etc.)

Engineering Application of shaking scenarios:

✓ **Intensity measures:** PGA, PGV, PGD, SA

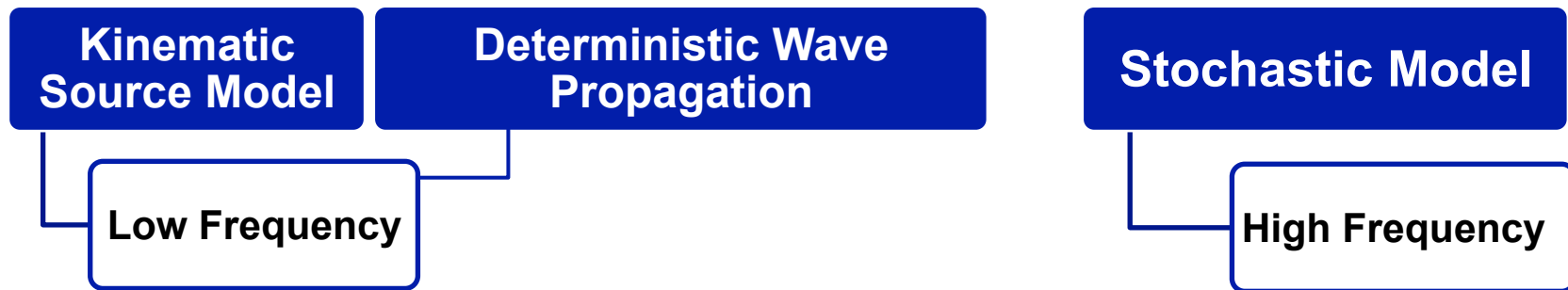
✓ **Different intensity measures are required for different type of structure:**

- **PGD:** related to **low freq.** ($f < 1$ Hz), correlated to M & focal mechanism.>>
long span bridges, displacement-based design approaches, and base-isolation devices.
- **PGV:** controlled by f_c and coherent **low-intermediate freq.** (1-3)Hz
- **PGA:** affected by **high freq.** that are strongly affected by small scale heterogeneities of rupture & propagation medium. >>

buildings and tunnels

The Proposed Method

➤ **Technique:** Hybrid Broadband (HBB) Synthetic Generation



□ **Kinematic Models:**

- **Need to define shaking scenarios (faulting, slip, rupture, etc.)**
- **Variability of kinematic parameters of Source (Site viabilities are excluded)**
 - ✓ Rupture velocity
 - ✓ Slip distribution
 - ✓ Position of nucleation point (Hypocenter)
 - ✓ Source-time function (STF)
 - ✓ Rise time



Kinematic Source Modeling:

➤ **Set parameters and consider the correlations**

- Estimate the rupture area based on M_w
- Calculate Average slip and slip velocity
- Distribute slip: Finite-Source Model as **Spatial Random Field Model** to characterize complexity (heterogeneities) in earthquake slip distribution >> ACF>> **Asperity regions**
- Define hypothetical Hypocenter
- Define the Soil layer density and wave velocities (P, S)
- Define Rupture (ratio, function etc.)
- Define Rise Rime (ration, value, function, etc.)
- Define Source Time Function (STF)

➤ **Consider source variability**

- Uncertainties are considered in the method by applying random components



Deterministic Wave Propagation

- GFs for wave propagation $\leftrightarrow$ *discrete wavenumber, finite-element method* (DWFE).
 - **Strength:**
 - include complete response of the earth structure
 - P, S waves and directivity in near-field are included in seismograms
 - **Weakness:** Anelastic attenuation can not be modeled

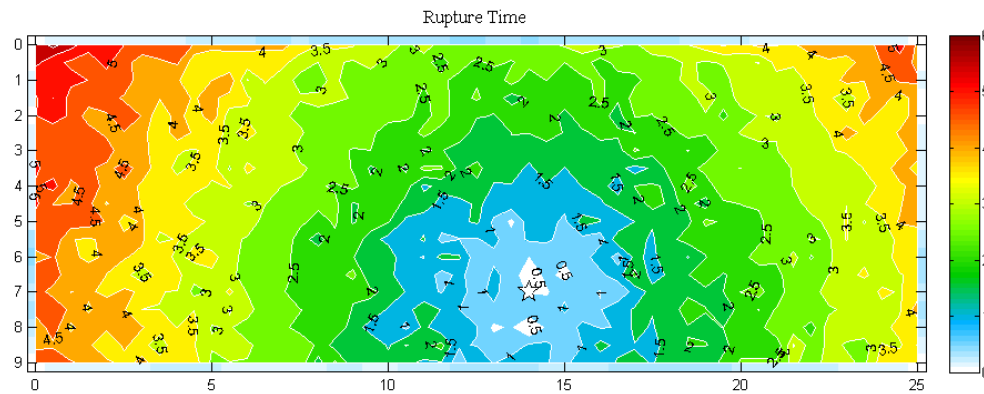
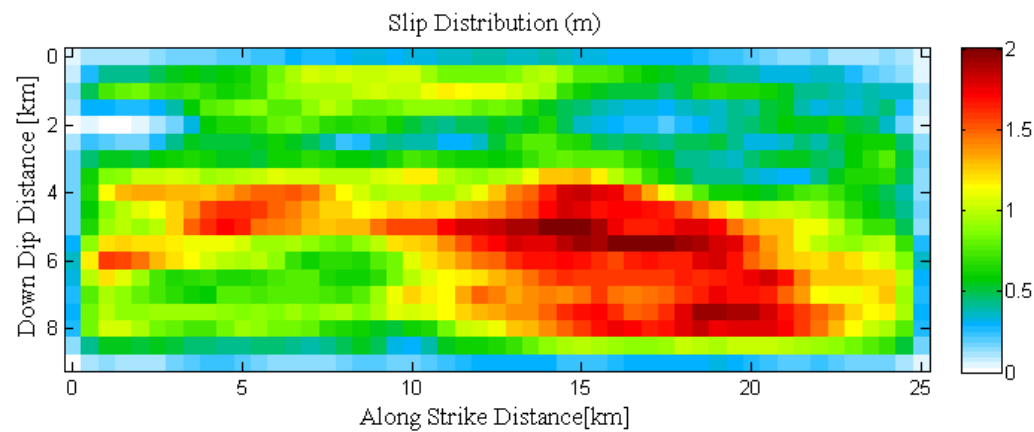
How does it work:

- ✓ **Calculate Green's function** in frequency, wavenumber, and depth domain. (fault geom. Independent)
- ✓ **Calculate traction Green's function** in frequency: traction on a defined fault surface for a set of observer location (*independent of rupture model*)
- ✓ **Apply representation theorem:** dot product of traction vector on a fault plane with slip & surface integral over the fault
- ✓ **Transfer to time domain:** IFFT, and apply appropriate filter

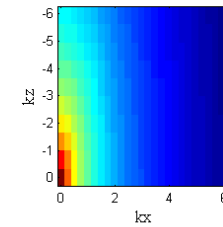
>> Long period synthetic at desired observers

Sample Model Mw=6.5

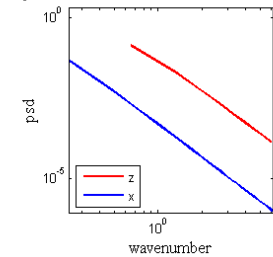
Fault Modeling



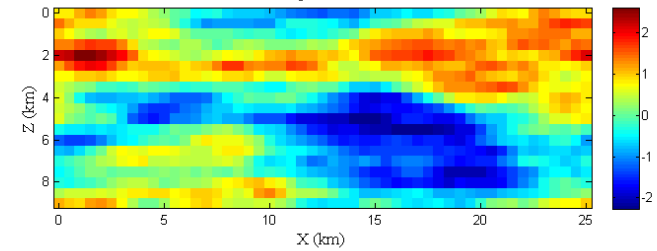
2D-Power Spectral Density (in log-units)



1D-spectra (az, ax = 2.1814, 9.0337, dz, dx = 0.5, 0.5)



Resulting Random Field

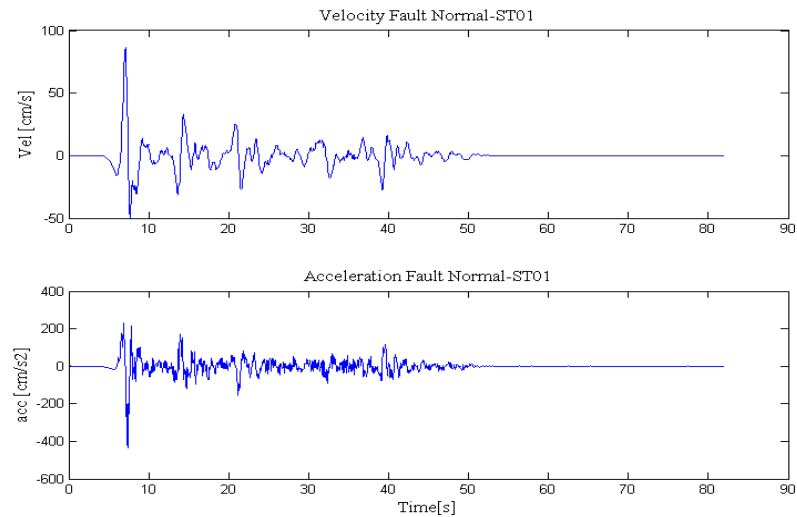
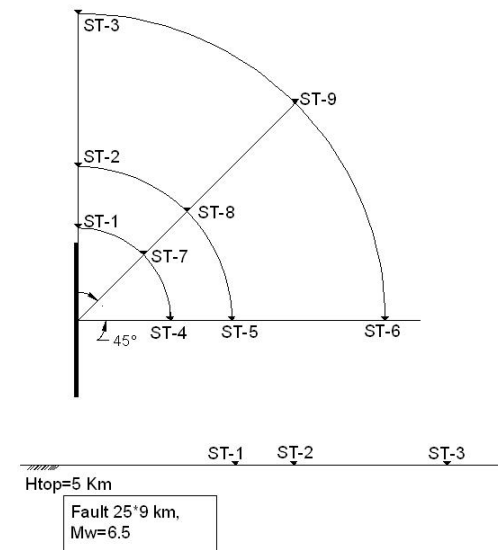


Mai, P.M., and G.C. Beroza (2002). A spatial random-field model to characterize complexity in earthquake slip, J. Geoph. Res., 107(B11), 2308, doi:10.1029/2001JB000588, 2002.

Modeling of Mw=6.5

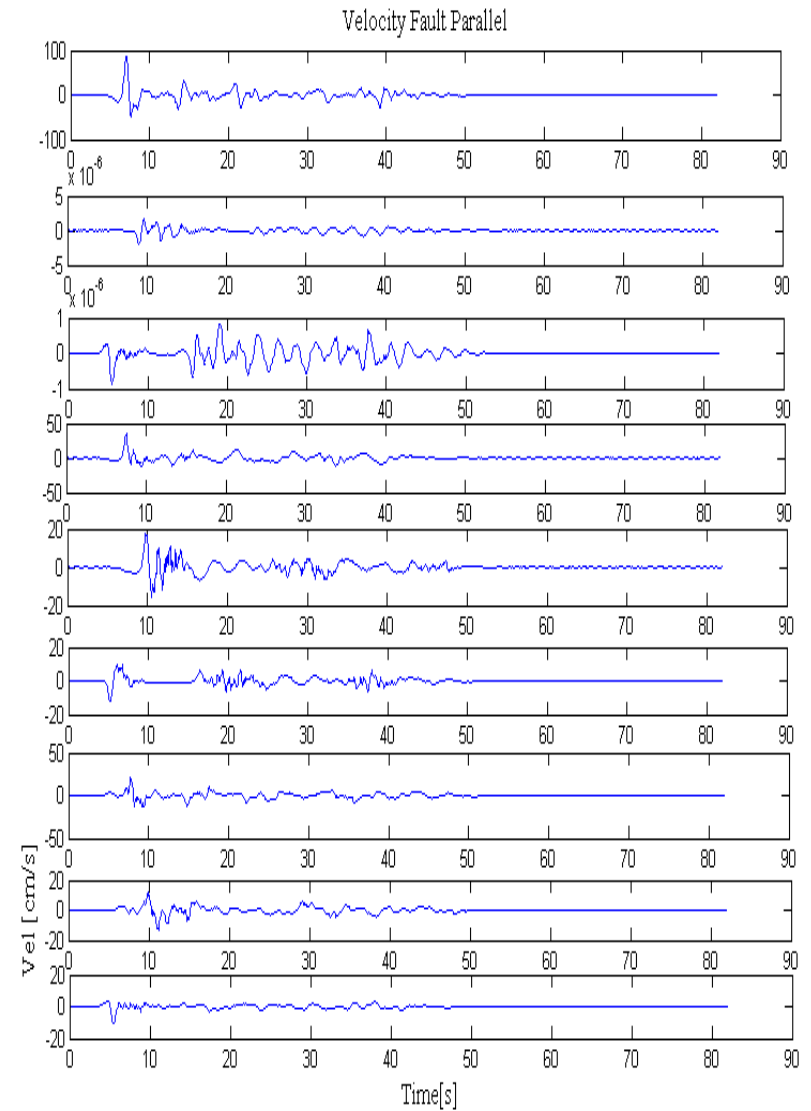
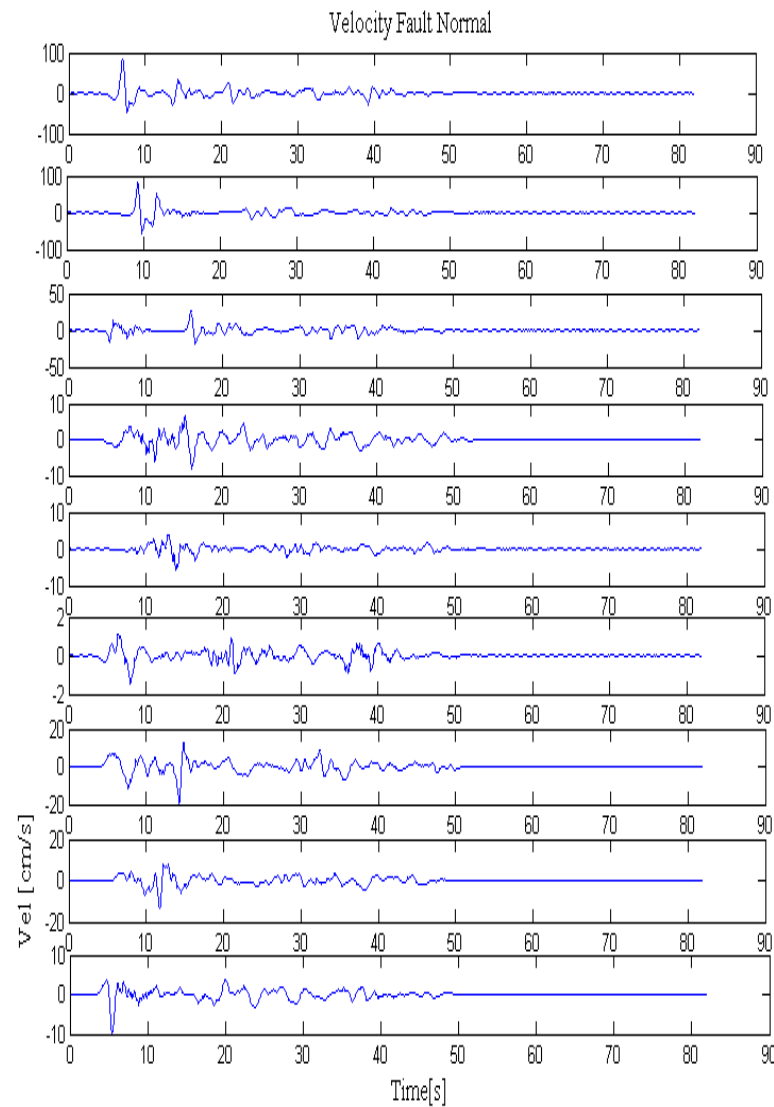
Velocity model used in synthetic generations*

Z (km)	V _p (km/s)	V _s (km/s)	Rho (g/cm ³)
0.000	1.633	1	2.32
0.092	1.633	1	2.32
0.200	1.633	1	2.32
0.500	1.796	1.1	2.32
0.700	2.286	1.4	2.38
0.900	2.776	1.7	2.40
1.000	3.266	2	2.50
2.500	5.715	3.5	2.70
5.000	5.226	3.2	2.70
10.00	5.715	3.5	2.70

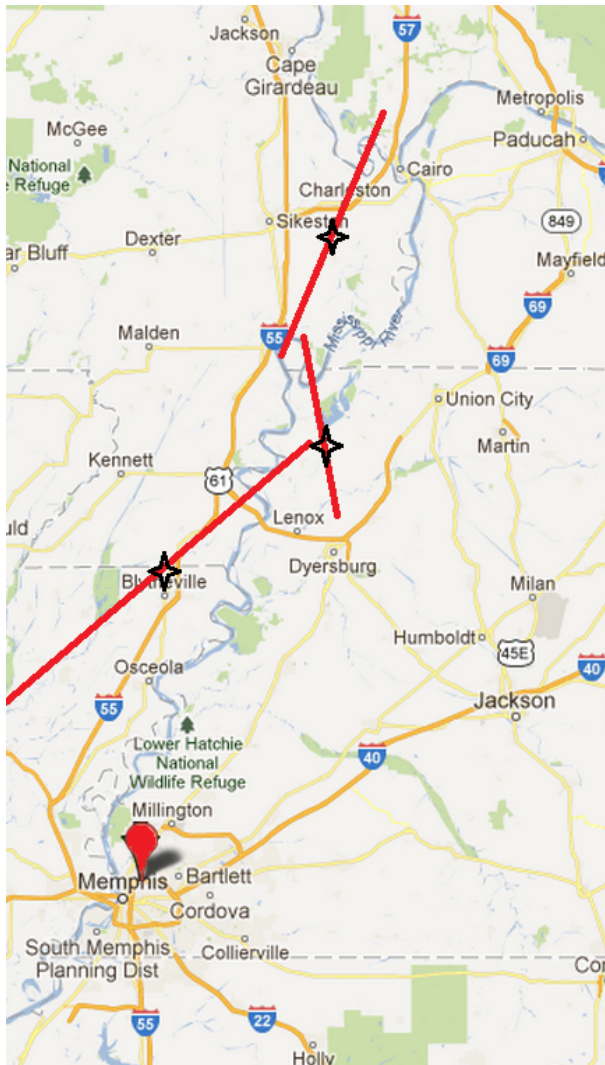


* Pezeshk, S., A. Zandieh, and B. Tavakoli. (2011). Hybrid empirical ground-motion prediction equations for eastern North America using NGA models and updated seismological parameters. , Bull. Seismol. Soc. Am 101(4), pp.1859-1870,

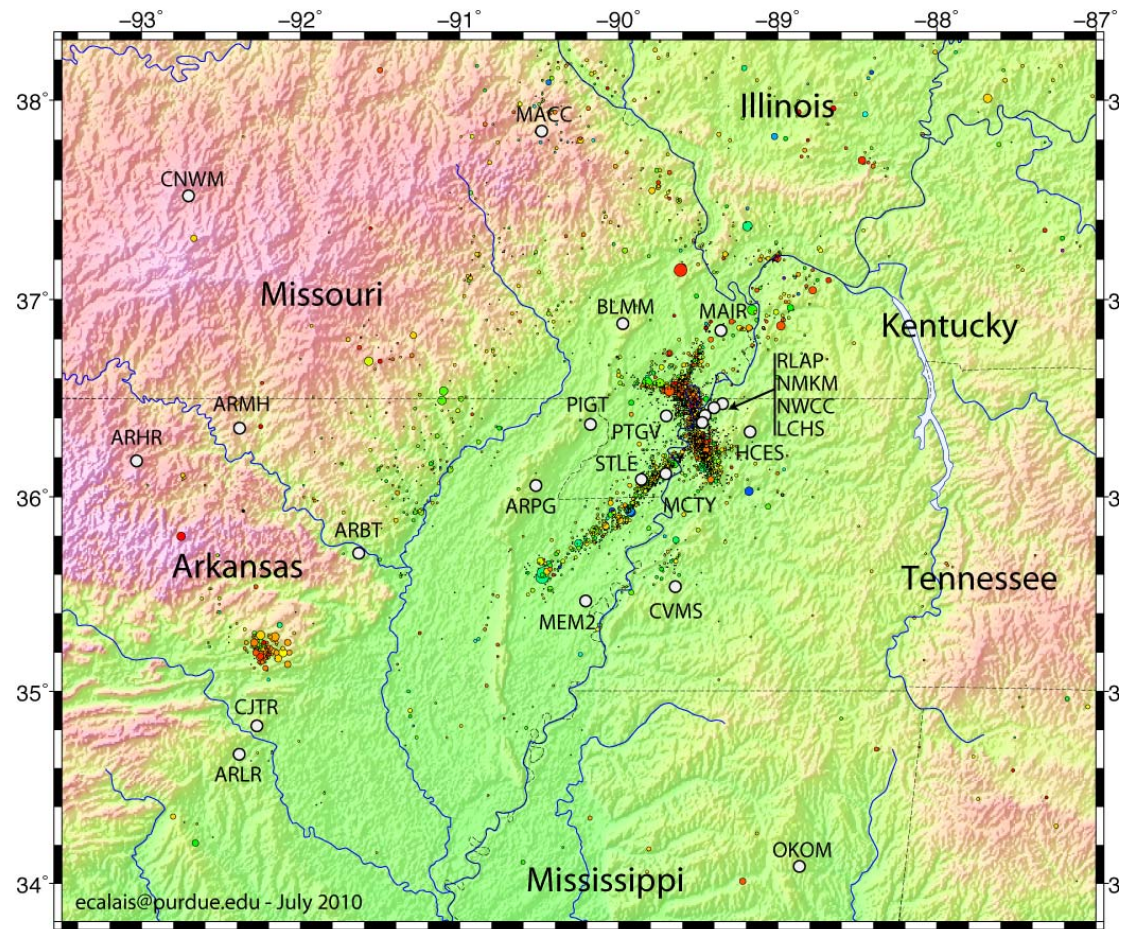
Velocity time histories generated for stations ST01 to ST09 from top to bottom, respectively. Time origin is initiation of rupture at hypocenter.



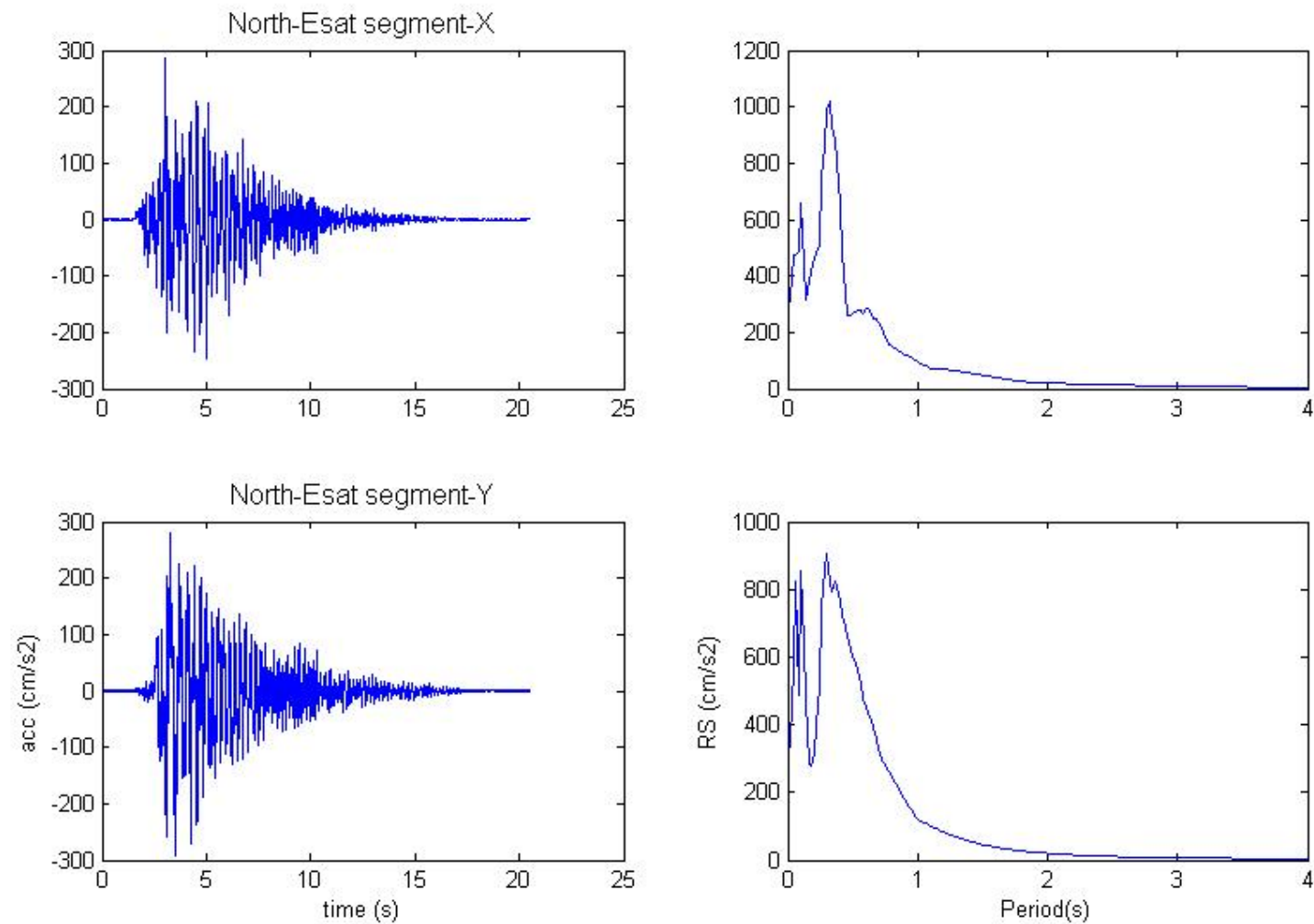
Case Study : Application for Seismic Analysis of a Bridge in Memphis



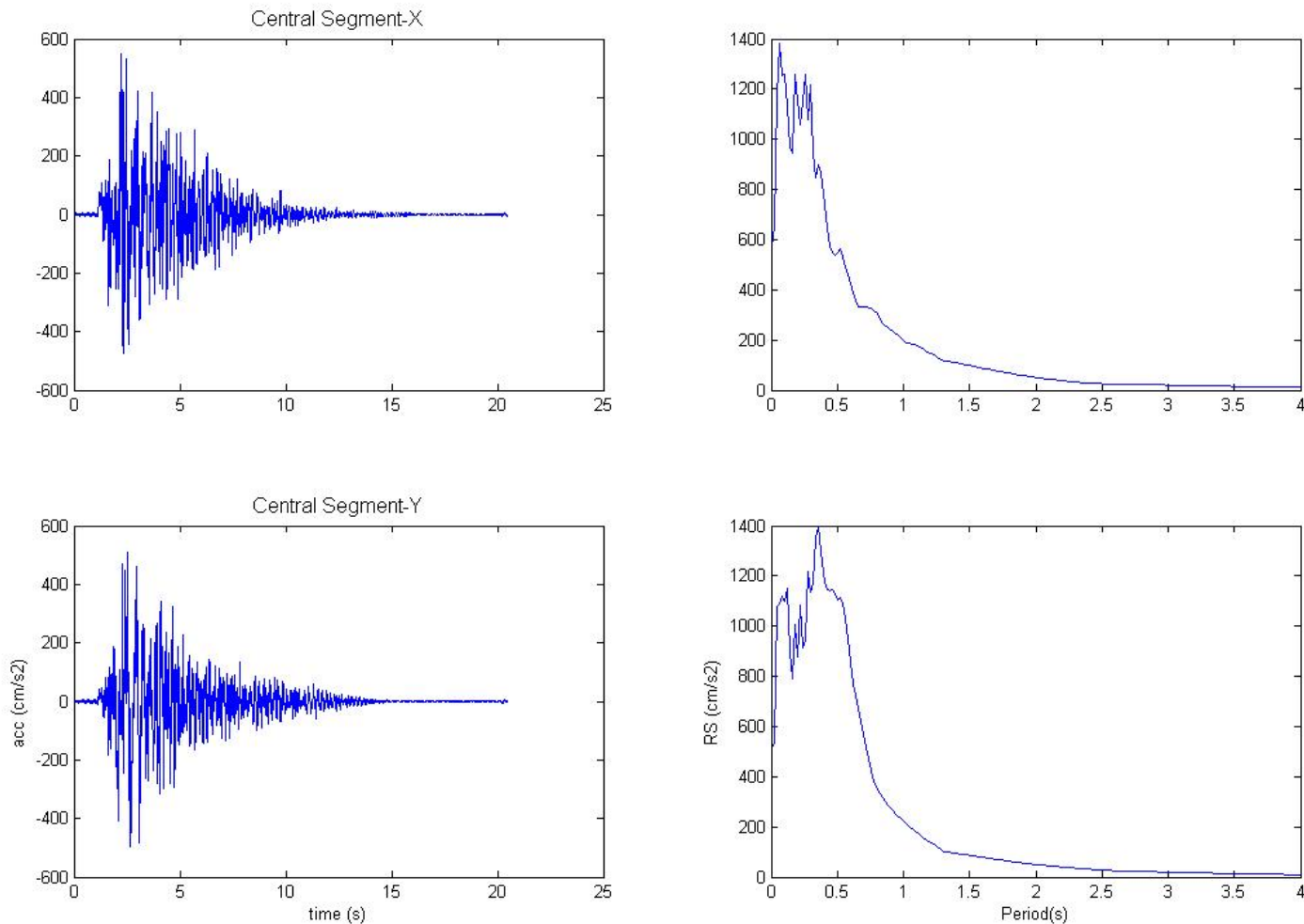
NMSZ



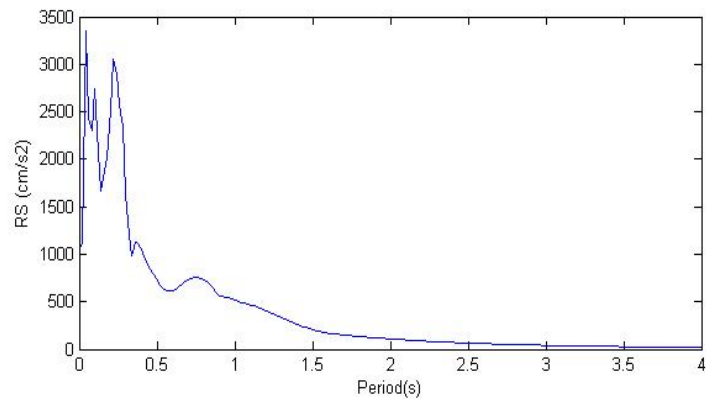
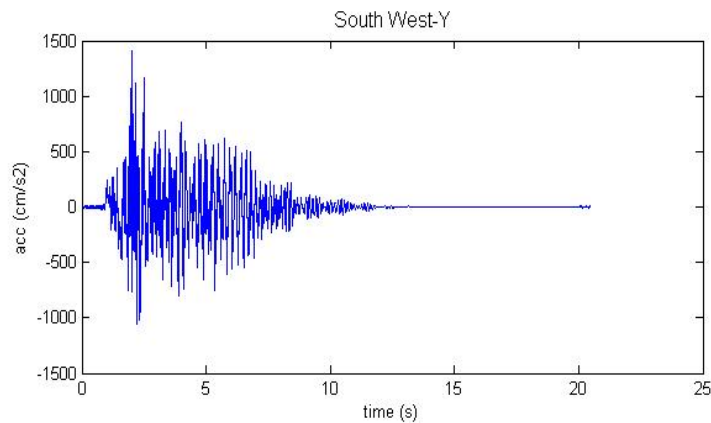
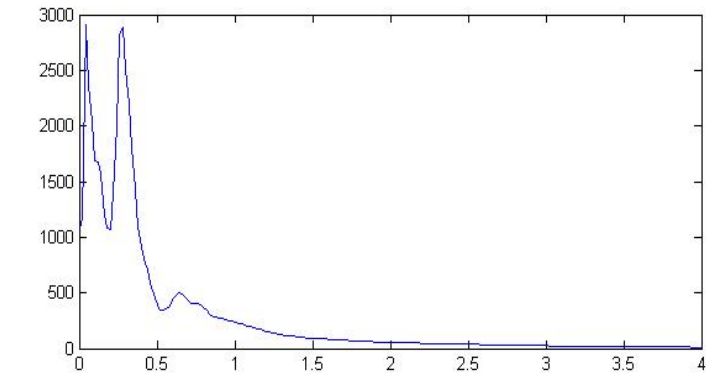
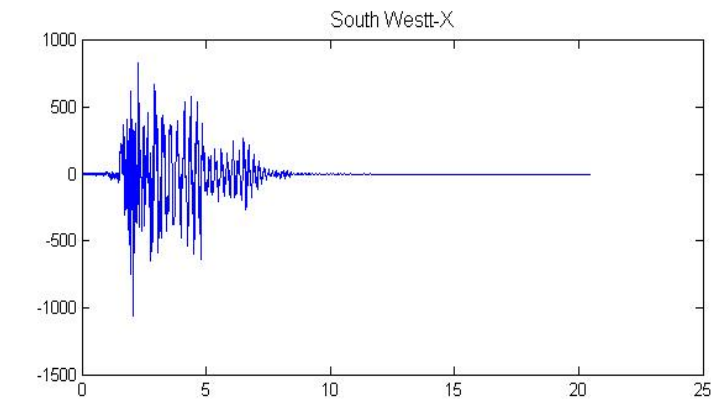
Synthetic from Mw=7.4 in North East part records at Memphis (~ 182 km)



Synthetic from Mw=7.4 in Central part records at Memphis (~ 145 km)



Synthetic from Mw=7.4 in South-West part Records at Memphis (~ 90 km)





Summary:

- A HBB method is proposed for generation of seismic time histories in a broad frequency band (0-10 Hz) appropriate for the Central and Eastern North America
- Application: Time History analysis & Complement of the catalog for GMPE
- In HBB, for High Freq., we used Stochastic models and for long period we used the Kinematic model
- Wave propagations are modeled by generation Green's function
- Slip distribution on the fault rupture is calculated based on both the Von Karman auto correlation function (ACF) and fractal distribution
- We put some random components in all the processes in order to consider variability and uncertainties of the parameters
- The synthetics for magnitudes of $M_w=5.5$, 6.5 and 7.5 are generated as the complement of the available catalog
- Next step we will compare the synthetic's spectra with the NGA equations



Acknowledgement

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Thanks For Your Attention

