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# COMPREHENSIVE DESIGN EXAMPLE FOR PRESTRESSED CONCRETE (PSC) GIRDER SUPERSTRUCTURE BRIDGE WITH COMMENTARY 

(Task order DTFH61-02-T-63032)

## US CUSTOMARY UNITS

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Technical Report Documentation Page


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## 1. INTRODUCTION

This example is part of a series of design examples sponsored by the Federal Highway Administration. The design specifications used in these examples is the AASHTO LRFD Bridge design Specifications. The intent of these examples is to assist bridge designers in interpreting the specifications, limit differences in interpretation between designers, and to guide the designers through the specifications to allow easier navigation through different provisions. For this example, the Second Edition of the AASHTO-LRFD Specifications with Interims up to and including the 2002 Interim is used.

This design example is intended to provide guidance on the application of the AASHTO-LRFD Bridge Design Specifications when applied to prestressed concrete superstructure bridges supported on intermediate multicolumn bents and integral end abutments. The example and commentary are intended for use by designers who have knowledge of the requirements of AASHTO Standard Specifications for Highway Bridges or the AASHTO-LRFD Bridge Design Specifications and have designed at least one prestressed concrete girder bridge, including the bridge substructure. Designers who have not designed prestressed concrete bridges, but have used either AASHTO Specification to design other types of bridges may be able to follow the design example, however, they will first need to familiarize themselves with the basic concepts of prestressed concrete design.

This design example was not intended to follow the design and detailing practices of any particular agency. Rather, it is intended to follow common practices widely used and to adhere to the requirements of the specifications. It is expected that some users may find differences between the procedures used in the design compared to the procedures followed in the jurisdiction they practice in due to Agency-specific requirements that may deviate from the requirements of the specifications. This difference should not create the assumption that one procedure is superior to the other.

Reference is made to AASHTO-LRFD specifications article numbers throughout the design example. To distinguish between references to articles of the AASHTO-LRFD specifications and references to sections of the design example, the references to specification articles are preceded by the letter "S". For example, S5.2 refers to Article 5.2 of AASHTO-LRFD specifications while 5.2 refers to Section 5.2 of the design example.

Two different forms of fonts are used throughout the example. Regular font is used for calculations and for text directly related to the example. Italic font is used for text that represents commentary that is general in nature and is used to explain the intent of some specifications provisions, explain a different available method that is not used by the example, provide an overview of general acceptable practices and/or present difference in application between different jurisdictions.

## 2. EXAMPLE BRIDGE

### 2.1 Bridge geometry and materials

## Bridge superstructure geometry

Superstructure type: Reinforced concrete deck supported on simple span prestressed girders made continuous for live load.

Spans: Two spans at 110 ft . each
Width: $\quad 55^{\prime}-4 \frac{1}{2 \prime \prime}$ total
52'-0" gutter line-to-gutter line (Three lanes 12 '- 0 " wide each, 10 ft . right shoulder and 6 ft . left shoulder. For superstructure design, the location of the driving lanes can be anywhere on the structure. For substructure design, the maximum number of 12 ft . wide lanes, i.e., 4 lanes, is considered)

Railings: $\quad$ Concrete Type F-Parapets, $1^{\prime}-8 \frac{1 / 4 "}{}$ wide at the base
Skew: 20 degrees, valid at each support location
Girder spacing: $\quad 9^{\prime}-8{ }^{\prime \prime}$
Girder type: $\quad$ AASHTO Type VI Girders, 72 in. deep, 42 in . wide top flange and 28 in . wide bottom flange (AASHTO 28/72 Girders)

Strand arrangement: Straight strands with some strands debonded near the ends of the girders
Overhang: $\quad 3^{\prime}-6^{1 / 4}$ " from the centerline of the fascia girder to the end of the overhang
Intermediate diaphragms: For load calculations, one intermediate diaphragm, 10 in. thick, 50 in . deep, is assumed at the middle of each span.

Figures 2-1 and 2-2 show an elevation and cross-section of the superstructure, respectively. Figure 2-3 through $2-6$ show the girder dimensions, strand arrangement, support locations and strand debonding locations.

Typically, for a specific jurisdiction, a relatively small number of girder sizes are available to select from. The initial girder size is usually selected based on past experience. Many jurisdictions have a design aid in the form of a table that determines the most likely girder size for each combination of span length and girder spacing. Such tables developed using the HS-25 live loading of the AASHTO Standard Specifications are expected to be applicable to the bridges designed using the AASHTO-LRFD Specifications.

The strand pattern and number of strands was initially determined based on past experience and subsequently refined using a computer design program. This design was refined using trial and error until a pattern produced stresses, at transfer and under service loads, that fell within the permissible stress limits and produced load resistances greater than the applied loads under the strength limit states. For debonded strands, S5.11.4.3 states that the number of partially debonded strands should not exceed 25 percent of the total number of strands. Also, the number of debonded strands in any horizontal row shall not exceed 40 percent of the strands in that row. The selected pattern has 27.2 percent of the total strands debonded. This is slightly higher than the 25 percent stated in the specifications, but is acceptable since the specifications require that this limit "should" be satisfied. Using the word "should" instead of "shall" signifies that the specifications allow some deviation from the limit of 25 percent.

Typically, the most economical strand arrangement calls for the strands to be located as close as possible to the bottom of the girders. However, in some cases, it may not be possible to satisfy all specification requirements while keeping the girder size to a minimum and keeping the strands near the bottom of the beam. This is more pronounced when debonded strands are used due to the limitation on the percentage of debonded strands. In such cases, the designer may consider the following two solutions:

- Increase the size of the girder to reduce the range of stress, i.e., the difference between the stress at transfer and the stress at final stage.
- Increase the number of strands and shift the center of gravity of the strands upward.

Either solution results in some loss of economy. The designer should consider specific site conditions (e.g., cost of the deeper girder, cost of the additional strands, the available under-clearance and cost of raising the approach roadway to accommodate deeper girders) when determining which solution to adopt.

## Bridge substructure geometry

Intermediate pier: Multi-column bent ( 4 - columns spaced at $14^{\prime}-1$ ")
Spread footings founded on sandy soil
See Figure 2-7 for the intermediate pier geometry
End abutments: Integral abutments supported on one line of steel H-piles supported on bedrock. U wingwalls are cantilevered from the fill face of the abutment. The approach slab is supported on the integral abutment at one end and a sleeper slab at the other end. See Figure 2-8 for the integral abutment geometry

## Materials

Concrete strength
Prestressed girders: Initial strength at transfer, $\mathrm{f}_{\mathrm{ci}}=4.8 \mathrm{ksi}$
28-day strength, $\mathrm{f}_{\mathrm{c}}=6 \mathrm{ksi}$
Deck slab: $\quad 4.0$ ksi
Substructure: $\quad 3.0 \mathrm{ksi}$
Railings: $\quad 3.5$ ksi
Concrete elastic modulus (calculated using S5.4.2.4)
Girder final elastic modulus, $\mathrm{E}_{\mathrm{c}} \quad=4,696 \mathrm{ksi}$
Girder elastic modulus at transfer, $\mathrm{E}_{\mathrm{ci}} \quad=4,200 \mathrm{ksi}$
Deck slab elastic modulus, $\mathrm{E}_{\mathrm{s}} \quad=3,834 \mathrm{ksi}$
Reinforcing steel
Yield strength, $\quad \mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi}$
Prestressing strands
0.5 inch diameter low relaxation strands Grade 270

Strand area, $\mathrm{A}_{\mathrm{ps}} \quad=0.153 \mathrm{in}^{2}$
Steel yield strength, $\mathrm{f}_{\mathrm{py}} \quad=243 \mathrm{ksi}$
Steel ultimate strength, $\mathrm{f}_{\mathrm{pu}} \quad=270 \mathrm{ksi}$
Prestressing steel modulus, $\mathrm{E}_{\mathrm{p}} \quad=28,500 \mathrm{ksi}$

## Other parameters affecting girder analysis

Time of Transfer = 1 day
Average Humidity $\quad=70 \%$


Figure 2-1 - Elevation View of the Example Bridge


Figure 2-2 - Bridge Cross-Section

### 2.2 Girder geometry and section properties

## Basic beam section properties

Beam length, L
Depth
Thickness of web
Area, $\mathrm{A}_{\mathrm{g}}$
Moment of inertia, $\mathrm{I}_{\mathrm{g}}$
N.A. to top, $\mathrm{y}_{\mathrm{t}}$
N.A. to bottom, $\mathrm{yb}_{\mathrm{b}}$

Section modulus, $\mathrm{S}_{\text {TOP }}$
Section modulus, $\mathrm{S}_{\mathrm{BOT}}$
CGS from bottom, at 0 ft .
CGS from bottom, at 11 ft .
CGS from bottom, at 54.5 ft .
$\mathrm{P} / \mathrm{S}$ force eccentricity at 0 ft ., $\mathrm{e}_{0}$,
$\mathrm{P} / \mathrm{S}$ force eccentricity at $11 \mathrm{ft} ., \mathrm{e}_{11},=31.222$ in
$\mathrm{P} / \mathrm{S}$ force eccentricity at $54.5 \mathrm{ft}, \mathrm{e}_{54.5},=31.380 \mathrm{in}$.

## Interior beam composite section properties

Effective slab width $=111 \mathrm{in}$. (see calculations in Section 2.3)
Deck slab thickness $=8$ in. (includes $1 / 2$ in. integral wearing surface which is not included in the calculation of the composite section properties)

Haunch depth $=4 \mathrm{in}$. (maximum value - notice that the haunch depth varies along the beam length and, hence, is ignored in calculating section properties but is considered when determining dead load)

| Moment of inertia, $\mathrm{I}_{\mathrm{c}}$ | $=1,384,254 \mathrm{in}^{4}$ |
| :--- | :--- |
| N.A. to slab top, $\mathrm{y}_{\mathrm{sc}}$ | $=27.96 \mathrm{in}$. |
| N.A. to beam top, $\mathrm{y}_{\mathrm{tc}}$ | $=20.46 \mathrm{in}$. |
| N.A. to beam bottom, ybc | $=51.54 \mathrm{in}$. |
| Section modulus, $\mathrm{S}_{\text {TOP SLAB }}$ | $=49,517 \mathrm{in}^{3}$ |
| Section modulus, $^{\text {S }}$ TOP BEAM | $=67,672 \mathrm{in}^{3}$ |
| Section modulus, $\mathrm{S}_{\text {BOT BEAM }}$ | $=26,855 \mathrm{in}^{3}$ |

## Exterior beam composite section properties

| Effective Slab Width | $=97.75 \mathrm{in}$. (see c |
| :--- | :--- |
| Deck slab thickness | $=8 \mathrm{in} . \quad$ (includes |
| calculatio |  |



Figure 2-3 - Beam Cross-Section Showing 44 Strands


Figure 2-4 - General Beam Elevation

Figure 2-5 - Elevation View of Prestressing Strands

+-Bonded Strand
$\oplus$ - Debonded Strand

For location of Sections A-A, B-B and C-C, see Figure 2-5

Figure 2-6 - Beam at Sections A-A, B-B, and C-C


Figure 2-7 - Intermediate Bent


Figure 2-8 - Integral Abutment

### 2.3 Effective flange width (S4.6.2.6)

Longitudinal stresses in the flanges are distributed across the flange and the composite deck slab by inplane shear stresses, therefore, the longitudinal stresses are not uniform. The effective flange width is a reduced width over which the longitudinal stresses are assumed to be uniformly distributed and yet result in the same force as the non-uniform stress distribution if integrated over the entire width.

The effective flange width is calculated using the provisions of S4.6.2.6. See the bulleted list at the end of this section for a few $S 4.6 .2 .6$ requirements. According to S4.6.2.6.1, the effective flange width may be calculated as follows:

## For interior girders :

The effective flange width is taken as the least of the following:

- One-quarter of the effective span length $\quad=0.25(82.5)(12)$

$$
=247.5 \mathrm{in} .
$$

- 12.0 times the average thickness of the slab, plus the greater of the web thickness $\quad=12(7.5)+8=104 \mathrm{in}$. or one-half the width of the top flange of the girder $=12(7.5)+0.5(42)$

$$
=\underline{111 \mathrm{in}} .
$$

- The average spacing of adjacent beams $=9 \mathrm{ft}$.- 8 in . or 116 in .

The effective flange width for the interior beam is 111 in .

## For exterior girders :

The effective flange width is taken as one-half the effective width of the adjacent interior girder plus the least of:

- One-eighth of the effective span length $\quad=0.125(82.5)(12)$

$$
=123.75 \mathrm{in} .
$$

- 6.0 times the average thickness of the slab, plus the greater of half the web thickness

$$
\begin{aligned}
& =6.0(7.5)+0.5(8) \\
& =49 \mathrm{in} . \\
& =6.0(7.5)+0.25(42) \\
& =55.5 \mathrm{in} .
\end{aligned}
$$

or one-quarter of the width of the top flange of the basic girder

## Design Step 2 - Example Bridge

- The width of the overhang


## Prestressed Concrete Bridge Design Example

$=3 \mathrm{ft} .-6^{1 / 4} \mathrm{in}$. or 42.25 in.

Therefore, the effective flange width for the exterior girder is:

$$
(111 / 2)+42.25=97.75 \mathrm{in} .
$$

Notice that:

- The effective span length used in calculating the effective flange width may be taken as the actual span length for simply supported spans or as the distance between points of permanent dead load inflection for continuous spans, as specified in S4.6.2.6.1. For analysis of I-shaped girders, the effective flange width is typically calculated based on the effective span for positive moments and is used along the entire length of the beam.
- The slab thickness used in the analysis is the effective slab thickness ignoring any sacrificial layers (i.e., integral wearing surfaces)
- S4.5 allows the consideration of continuous barriers when analyzing for service and fatigue limit states. The commentary of S4.6.2.6.1 includes an approximate method of including the effect of the continuous barriers on the section by modifying the width of the overhang. Traditionally, the effect of the continuous barrier on the section is ignored in the design of new bridges and is ignored in this example. This effect may be considered when checking existing bridges with structurally sound continuous barriers.
- Simple-span girders made continuous behave as continuous beams for all loads applied after the deck slab hardens. For two-equal span girders, the effective length of each span, measured as the distance from the center of the end support to the inflection point for composite dead loads (load is assumed to be distributed uniformly along the length of the girders), is 0.75 the length of the span.


## 3. FLOWCHARTS

## Main Design Steps



## Main Design Steps (cont.)



> Section in Example

Design Step 7.1

Design Step 7.2

## Deck Slab Design



## Deck Slab Design (cont.)



## General Superstructure Design

(Notice that only major steps are presented in this flowchart. More detailed flowcharts of the design steps follow this flowchart)


## General Superstructure Design (cont.)



## Live LoadDistribution Factor Calculations



Section in Example

Design Step 5.1

Design Step 5.1.3

Design Step 5.1.6

Design Step 5.1.5

Design Step 5.1.7

Design Step 5.1.8

## Live LoadDistribution Factor Calculations (cont.)



Section in Example

Design Step 5.1.9

Design Step 5.1.10

Design Step 5.1.15

## Creep and Shrinkage Calculations



## Creep and Shrinkage Calculations (cont.)



## Prestressing Losses Calculations



## Prestressing Losses Calculations (cont.)



## Flexural Design



## Section in Example

Design Step 5.6.1.1

Design Step 5.6.2.1

Design Step 5.6.1.2

Design Step 5.6.2.2

## Flexural Design (cont.)



## Flexural Design (cont.)



## Flexural Design (cont.)



Section in Example

Design Step 5.6.8

## Shear Design - Alternative 1, Assumed Angle ?



## Shear Design - Alternative 1, Assumed Angle ? (cont.)



## Shear Design - Alternative 1, Assumed Angle ? (cont.)



## Shear Design - Alternative 2, Assumed Strain $e_{x}$



## Shear Design - Alternative 2, Assumed Strain $\mathrm{e}_{\mathrm{x}}$ (cont.)



## Shear Design - Alternative 2, Assumed Strain $\mathrm{e}_{\mathrm{x}}$ (cont.)



## Steel-Reinforced Elastomeric Bearing Design - Method A (Reference Only)



## Steel-Reinforced Elastomeric Bearing Design - Method A (Reference Only) (cont.)



## Steel-Reinforced Elastomeric Bearing Design - Method B



## Steel-Reinforced Elastomeric Bearing Design - Method B (cont.)



## SUBSTRUCTURE

## Integral Abutment Design



## Intermediate Bent Design



## Intermediate Bent Design (cont.)



## Intermediate Bent Design (cont.)



## Design Step $\mid$ DECK SLAB DESIGN

4
Design Step
4.1

In addition to designing the deck for dead and live loads at the strength limit state, the AASHTO-LRFD specifications require checking the deck for vehicular collision with the railing system at the extreme event limit state. The resistance factor at the extreme event limit state is taken as 1.0. This signifies that, at this level of loading, damage to the structural components is allowed and the goal is to prevent the collapse of any structural components.

The AASHTO-LRFD Specifications include two methods of deck design. The first method is called the approximate method of deck design (S4.6.2.1) and is typically referred to as the equivalent strip method. The second is called the Empirical Design Method (S9.7.2).

The equivalent strip method is based on the following:

- A transverse strip of the deck is assumed to support the truck axle loads.
- The strip is assumed to be supported on rigid supports at the center of the girders. The width of the strip for different load effects is determined using the equations in S4.6.2.1.
- The truck axle loads are moved laterally to produce the moment envelopes. Multiple presence factors and the dynamic load allowance are included. The total moment is divided by the strip distribution width to determine the live load per unit width.
- The loads transmitted to the bridge deck during vehicular collision with the railing system are determined.
- Design factored moments are then determined using the appropriate load factors for different limit states.
- The reinforcement is designed to resist the applied loads using conventional principles of reinforced concrete design.
- Shear and fatigue of the reinforcement need not be investigated.

The Empirical Design Method is based on laboratory testing of deck slabs. This testing indicates that the loads on the deck are transmitted to the supporting components mainly through arching action in the deck, not through shears and moments as assumed by traditional design. Certain limitations on the geometry of the deck are listed in S9.7.2. Once these limitations are satisfied, the specifications give reinforcement ratios for both the longitudinal and transverse reinforcement for both layers of deck reinforcement. No other design calculations are required for the interior portions of the deck. The overhang region is then designed for vehicular collision with the railing system and for
dead and live loads acting on the deck. The Empirical Design Method requires less reinforcement in the interior portions of the deck than the Approximate Method.

For this example, the Approximate Method (Strip Width Method) is used.


Figure 4-1 - Bridge Cross-Section

Required information:
Girder spacing
Top cover

$$
\begin{aligned}
& =9 \mathrm{ft}-8 \mathrm{in} . \\
& =21 / 2 \mathrm{in} .(\mathrm{S} 5.12 .3) \\
& \quad \text { (includes } 1 / 2 \mathrm{in} . \text { integral wearing surface) } \\
& =1 \mathrm{in.}(\mathrm{~S} 5.12 .3) \\
& =60 \mathrm{ksi} \\
& =4 \mathrm{ksi} \\
& =150 \mathrm{pcf} \\
& =30 \mathrm{psf}
\end{aligned}
$$

Bottom cover
Steel yield strength
Slab conc. compressive strength
Concrete density
Future wearing surface density

## Design Step

DECK THICKNESS

The specifications require that the minimum thickness of a concrete deck, excluding any provisions for grinding, grooving and sacrificial surface, should not be less than 7 in. (S9.7.1.1). Thinner decks are acceptable if approved by the bridge owner. For slabs with depths less than $1 / 20$ of the design span, consideration should be given to prestressing in the direction of that span in order to control cracking.

Most jurisdictions require a minimum deck thickness of 8 in., including the $1 / 2$ inch integral wearing surface.

In addition to the minimum deck thickness requirements of S9.7.1.1, some jurisdictions check the slab thickness using the provisions of S2.5.2.6.3. The provisions in this article are meant for slab-type bridges and their purpose is to limit deflections under live loads. Applying these provisions to the design of deck slabs rarely controls deck slab design.

For this example, a slab thickness of 8 in., including the $1 / 2$ inch integral wearing surface, is assumed. The integral wearing surface is considered in the weight calculations. However, for resistance calculations, the integral wearing surface is assumed to not contribute to the section resistance, i.e., the section thickness for resistance calculations is assumed to be 7.5 in .

## Design Step

OVERHANG THICKNESS

For decks supporting concrete parapets, the minimum overhang thickness is 8 in. (S13.7.3.1.2), unless a lesser thickness is proven satisfactory through crash testing of the railing system. Using a deck overhang thickness of approximately $3 / 4$ " to 1 " thicker than the deck thickness has proven to be beneficial in past designs.

For this example, an overhang thickness of 9 in ., including the $1 / 2 \mathrm{in}$. sacrificial layer is assumed in the design.

## Design Step

CONCRETE PARAPET

A Type-F concrete parapet is assumed. The dimensions of the parapet are shown in Figure 4-2. The railing crash resistance was determined using the provisions of SA13.3.1. The characteristics of the parapet and its crash resistance are summarized below.

Concrete Parapet General Values and Dimensions:

| Mass per unit length | $=650 \mathrm{lb} / \mathrm{ft}$ |
| :--- | :--- |
| Width at base | $=1 \mathrm{ft} .-81 / 4 \mathrm{in}$. |
| Moment capacity at the base calculated |  |
| assuming the parapet acts as a vertical |  |
| cantilever, $\mathrm{M}_{\mathrm{c}} /$ length | $=17.83 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$ |
| Parapet height, H | $=42 \mathrm{in}$. |
| Length of parapet failure mechanism, $\mathrm{L}_{\mathrm{c}}$ | $=235.2 \mathrm{in}$. |
| Collision load capacity, $\mathrm{R}_{\mathrm{w}}$ | $=137.22 \mathrm{k}$ |

Notice that each jurisdiction typically uses a limited number of railings. The properties of each parapet may be calculated once and used for all deck slabs. For a complete railing design example, see Lecture 16 of the participant notebook of the National Highway Institute Course No. 13061.


## Figure 4-2 - Parapet Cross-Section

The load capacity of this parapet exceeds the minimum required by the Specifications. The deck overhang region is required to be designed to have a resistance larger than the actual resistance of the concrete parapet (SA13.4.2).

## Design Step

EQUIVALENT STRIP METHOD (S4.6.2)
Moments are calculated for a deck transverse strip assuming rigid supports at web centerlines. The reinforcement is the same in all deck bays. The overhang is designed for cases of DL + LL at the strength limit state and for collision with the railing system at the extreme event limit state.

## Design Step <br> 4.5.1

Design dead load moments:
Load factors (S3.4.1):
Slab and parapet:
Minimum $=0.9$
Maximum $=1.25$

Future wearing surface:
Minimum $=0.65$
Maximum $=1.5$

It is not intended to maximize the load effects by applying the maximum load factors to some bays of the deck and the minimum load factors to others. Therefore, for deck slabs the maximum load factor controls the design and the minimum load factor may be ignored.

Dead loads represent a small fraction of the deck loads. Using a simplified approach to determine the deck dead load effects will result in a negligible difference in the total (DL $+L L)$ load effects. Traditionally, dead load positive and negative moments in the deck, except for the overhang, for a unit width strip of the deck are calculated using the following approach:

$$
\mathrm{M}=\mathrm{wl}^{2} / \mathrm{c}
$$

where:
$\mathrm{M}=$ dead load positive or negative moment in the deck for a unit width strip (k-ft/ft)
$\mathrm{w}=$ dead load per unit area of the deck (ksf)
| = girder spacing (ft.)
c $=$ constant, typically taken as 10 or 12
For this example, the dead load moments due to the self weight and future wearing surface are calculated assuming $\mathrm{c}=10$.

Self weight of the deck $=8(150) / 12=100 \mathrm{psf}$
Unfactored self weight positive or negative moment $=(100 / 1000)(9.66)^{2} / 10$

$$
=0.93 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
$$

Future wearing surface $=30 \mathrm{psf}$
Unfactored FWS positive or negative moment $\quad=(30 / 1000)(9.66)^{2} / 10$
$=0.28 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$

Design Step
4.6

DISTANCE FROM THE CENTER OF THE GIRDER TO THE DESIGN SECTION FOR NEGATIVE MOMENT

For precast I-shaped and T-shaped concrete beams, the distance from the centerline of girder to the design section for negative moment in the deck should be taken equal to one-third of the flange width from the centerline of the support (S4.6.2.1.6), but not to exceed 15 in .

Girder top flange width $=42$ in.
One-third of the girder top flange width $=14 \mathrm{in} .<15 \mathrm{in} . \mathbf{O K}$

## Design Step

 4.7
## DETERMINING LIVE LOAD EFFECTS

Using the approximate method of deck analysis (S4.6.2), live load effects may be determined by modeling the deck as a beam supported on the girders. One or more axles may be placed side by side on the deck (representing axles from trucks in different traffic lanes) and move them transversely across the deck to maximize the moments (S4.6.2.1.6). To determine the live load moment per unit width of the bridge, the calculated total live load moment is divided by a strip width determined using the appropriate equation from Table S4.6.2.1.3-1. The following conditions have to be satisfied when determining live load effects on the deck:

Minimum distance from center of wheel to the inside face of parapet $=1$ ft. $($ S3.6.1.3 $)$
Minimum distance between the wheels of two adjacent trucks $=4 \mathrm{ft}$.
Dynamic load allowance $=33 \%($ S3.6.2.1 $)$
Load factor $($ Strength $I)=1.75($ S3.4.1 $)$
Multiple presence factor (S3.6.1.1.2):

$$
\begin{array}{ll}
\text { Single lane } & =1.20 \\
\text { Two lanes } & =1.00 \\
\text { Three lanes } & =0.85
\end{array}
$$

(Note: the "three lanes" situation never controls for girder spacings up to 16 ft.)
Trucks were moved laterally to determine extreme moments (S4.6.2.1.6)
Fatigue need not be investigated for concrete slabs in multi-girder bridges (S9.5.3 and S5.5.3.1)

Resistance factors, $\varphi$, for moment: $\quad 0.9$ for strength limit state (S5.5.4.2)
1.0 for extreme event limit state (S1.3.2.1)

In lieu of this procedure, the specifications allow the live load moment per unit width of the deck to be determined using Table SA4.1-1. This table lists the positive and negative moment per unit width of decks with various girder spacings and with various distances from the design section to the centerline of the girders for negative moment. This table is based on the analysis procedure outlined above and will be used for this example.

Table SA4.1-1 does not include the girder spacing of 9'-8". It does include girder spacings of $9^{\prime}-6^{\prime \prime}$ and $9^{\prime}-9^{\prime \prime}$. Interpolation between the two girder spacings is allowed. However, due to the small difference between the values, the moments corresponding to the girder spacing of $9^{\prime}-9^{\prime \prime}$ are used which gives slightly more conservative answers than interpolating. Furthermore, the table lists results for the design section for negative moment at 12 in . and 18 in . from the center of the girder. For this example, the distance from the design section for negative moment to the centerline of the girders is 14 in . Interpolation for the values listed for 12 in . and 18 in . is allowed. However, the value corresponding to the 12 in . distance may be used without interpolation resulting in a more conservative value. The latter approach is used for this example.

## Design Step

DESIGN FOR POSITIVE MOMENT IN THE DECK

The reinforcement determined in this section is based on the maximum positive moment in the deck. For interior bays of the deck, the maximum positive moment typically takes place at approximately the center of each bay. For the first deck bay, the bay adjacent to the overhang, the location of the maximum design positive moment varies depending on the overhang length and the value and distribution of the dead load. The same reinforcement is typically used for all deck bays.

## Factored loads

## Live load

From Table SA4.1-1, for the girder spacing of 9'-9" (conservative):
Unfactored live load positive moment per unit width $=6.74 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Maximum factored positive moment per unit width $=1.75(6.74)$

$$
=11.80 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
$$

This moment is applicable to all positive moment regions in all bays of the deck (S4.6.2.1.1).

Deck weight
$1.25(0.93)=1.16 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Future wearing surface

$$
1.5(0.28)=0.42 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
$$

$\underline{\text { Dead load + live load design factored positive moment (Strength I limit state) }}$

$$
\begin{aligned}
\mathrm{M}_{\mathrm{DL}+\mathrm{LL}} & =11.8+1.16+0.42 \\
& =13.38 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Notice that the total moment is dominated by the live load.
Resistance factor for flexure at the strength limit state, $\varphi=0.90$ (S5.5.4.2.1)
The flexural resistance equations in the AASHTO-LRFD Bridge Design Specifications are applicable to reinforced concrete and prestressed concrete sections. Depending on the provided reinforcement, the terms related to prestressing, tension reinforcing steel and/or compression reinforcing steel, are set to zero. The following text is further explanation on applying these provisions to reinforced concrete sections and the possible simplifications to the equations for this case.

For rectangular section behavior, the depth of the section in compression, $c$, is determined using Eq. S5.7.3.1.1-4:

$$
\begin{equation*}
c=\frac{A_{p s} f_{p u}+A_{s} f_{y}-A_{s}^{\prime} f_{y}^{\prime}}{0.85 f_{c}^{\prime} \beta_{l} b+k_{A_{p s}} \frac{f_{p u}}{d_{p}}} \tag{S5.7.3.1.1-4}
\end{equation*}
$$

where:
$A_{p s}=$ area of prestressing steel $\left(\right.$ in $\left.^{2}\right)$
$f_{p u}=$ specified tensile strength of prestressing steel (ksi)
$f_{p y}=$ yield strength of prestressing steel (ksi)
$A_{s}=$ area of mild steel tension reinforcement $\left(\right.$ in $\left.^{2}\right)$
$A_{s}^{\prime}=$ area of compression reinforcement $\left(\right.$ in $\left.^{2}\right)$
$f_{y}=$ yield strength of tension reinforcement (ksi)
$f^{\prime}{ }_{y}=$ yield strength of compression reinforcement $(k s i)$
$b=$ width of rectangular section (in.)
$d_{p}=$ distance from the extreme compression fiber to the centroid of the prestressing tendons (in.)
$c=$ distance between the neutral axis and the compressive face (in.)
$\beta_{1}=$ stress block factor specified in S5.7.2.2

For reinforced concrete sections (no prestressing) without reinforcement on the compression side of the section, the above equation is reduced to:

$$
c=\frac{A_{s} f_{y}}{0.85 f_{c}^{\prime} \beta_{1} b}
$$

The depth of the compression block, $a$, may be calculates as:

$$
a=c \beta_{l}
$$

These equations for " $a$ " and " $c$ " are identical to those traditionally used in reinforced concrete design. Many text books use the following equation to determine the reinforcement ratio, $\rho$, and area of reinforcement, $A_{s}$ :

$$
\begin{aligned}
& k^{\prime}=M_{u} /\left(\varphi b d^{2}\right) \\
& \rho=0.85\left(\frac{f_{c}^{\prime}}{f_{y}}\left[1.0-\sqrt{1.0-\frac{2 k^{\prime}}{0.85 f_{c}^{\prime}}}\right]\right. \\
& A_{s}=\rho d_{e}
\end{aligned}
$$

A different method to determine the required area of steel is based on using the above equation for " $a$ " and " $c$ " with the Eq. S5.7.3.2.2-1 as shown below. The nominal flexural resistance, $M_{n}$, may be taken as:

$$
\begin{equation*}
M_{n}=A_{p} f_{p s}\left(d_{p}-a / 2\right)+A_{s} f_{y}\left(d_{s}-a / 2\right)-A_{s}^{\prime} f_{y}\left(d_{s}^{\prime}-a / 2\right)+0.85 f_{c}^{\prime}\left(b-b_{w}\right) \beta_{l} h_{f}\left(a / 2-h_{f} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

where:
$f_{p s}=$ average stress in prestressing steel at nominal bending resistance specified in Eq. S5.7.3.1.1-1 (ksi)
$d_{s}=$ distance from extreme compression fiber to the centroid of nonprestressed tensile reinforcement (in.)
$d_{s}^{\prime}=$ distance from extreme compression fiber to the centroid of compression reinforcement (in.)
$b=$ width of the compression face of the member (in.)
$b_{w}=$ web width or diameter of a circular section (in.)
$h_{f}=$ compression flange depth of an I or T member (in.)

For rectangular reinforced concrete sections (no prestressing) without reinforcement on the compression side of the section, the above equation is reduced to:

$$
M_{n}=A_{s} f_{y}\left(d_{s}-\frac{a}{2}\right)
$$

From the equations for " $c$ " and " $a$ " above, substituting for:

$$
\begin{aligned}
& a=c \beta_{l}=\frac{A_{s} f_{y}}{0.85 f_{c}^{\prime} b} \text { in the equation for } M_{n} \text { above yields: } \\
& M_{n}=A_{s} f_{y}\left(d_{s}-\frac{a}{2}\right)=f_{y} d_{s} A_{s}-\left(\frac{f_{y}^{2}}{1.7 f_{c}^{\prime} b}\right) A_{s}^{2}
\end{aligned}
$$

Only $A_{s}$ is unknown in this equation. By substituting for $b=12$ in., the required area of reinforcement per unit width can be determined by solving the equation.

Both methods outlined above yield the same answer. The first method is used throughout the following calculations.

For the positive moment section:
$d_{e}=$ effective depth from the compression fiber to the centroid of the tensile force in the tensile reinforcement (in.)
$=$ total thickness - bottom cover $-1 / 2$ bar diameter - integral wearing surface $=8-1-1 / 2(0.625)-0.5$
$=6.19 \mathrm{in}$.
$\mathrm{k}^{\prime}=\mathrm{M}_{\mathrm{u}} /\left(\varphi \mathrm{bd}^{2}\right)$
$=13.38 /\left[0.9(1.0)(6.19)^{2}\right]$
$=0.388 \mathrm{k} / \mathrm{in}^{2}$

$$
\begin{aligned}
\rho & =0.85\left(\frac{\mathrm{f}_{\mathrm{c}}^{\prime}}{\mathrm{f}_{\mathrm{y}}}\right)\left[1.0-\sqrt{1.0-\frac{2 \mathrm{k}^{\prime}}{0.85 \mathrm{f}_{\mathrm{c}}^{\prime}}}\right] \\
& =0.00688
\end{aligned}
$$

Therefore,
Required $\mathrm{A}_{\mathrm{s}}=\mathrm{\rho d}_{\mathrm{e}}=0.00688(6.19)=0.0426 \mathrm{in}^{2} / \mathrm{in}$.
Required \#5 bar spacing with bar area $0.31 \mathrm{in}^{2}=0.31 / 0.0426=7.28 \mathrm{in}$.
Use \#5 bars at 7 in . spacing

## Check maximum and minimum reinforcement

Based on past experience, maximum and minimum reinforcement requirements never control the deck slab design. The minimum reinforcement requirements are presented in S5.7.3.3.2. These provisions are identical to those of the AASHTO Standard Specifications. These provisions are illustrated later in this example.

Maximum reinforcement requirements are presented in S5.7.3.3.1. These requirements are different from those of the AASHTO Standard Specifications. Reinforced concrete sections are considered under-reinforced when $c / d_{e}=0.42$. Even though these requirements are not expected to control the design, they are illustrated below to familiarize the user with their application.

Check depth of compression block:

$$
\begin{aligned}
\mathrm{T} & =\text { tensile force in the tensile reinforcement }(\mathrm{k}) \\
& =0.31(60) \\
& =18.6 \mathrm{k} \\
\mathrm{a} & =18.6 /[0.85(4)(7)] \\
& =0.78 \mathrm{in} .
\end{aligned}
$$

$\beta_{1}=$ ratio of the depth of the equivalent uniformly stressed compression zone assumed in the strength limit state to the depth of the actual compression zone
$=0.85$ for $f_{c}=4$ ksi (S5.7.2.2)
c $=0.78 / 0.85$
$=0.918 \mathrm{in}$.
Check if the section is over-reinforced

$$
\begin{aligned}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} & =0.918 / 6.19 \\
& =0.15<0.42 \text { OK }(\mathrm{S} 5.7 .3 .3 .1)
\end{aligned}
$$

Check for cracking under Service I Limit State (S5.7.3.4)
Allowable reinforcement service load stress for crack control using Eq. S5.7.3.4-1:

$$
\mathrm{f}_{\mathrm{sa}}=\frac{\mathrm{Z}}{\left(\mathrm{~d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3}} \leq 0.6 \mathrm{f}_{\mathrm{y}}=36 \mathrm{ksi}
$$



Figure 4-3-Bottom Transverse Reinforcement
where:
$d_{c}=$ thickness of concrete cover measured from extreme tension fiber to center of bar located closest thereto (in.)
$=1.3125 \mathrm{in}$. $<(2+1 / 2$ bar diameter $) \mathrm{in}$. OK
$\mathrm{A}=$ area of concrete having the same centroid as the principal tensile reinforcement and bounded by the surfaces of the cross-section and a straight line parallel to the neutral axis, divided by the number of bars (in ${ }^{2}$ )
$=2(1.3125)(7)$
$=18.375 \mathrm{in}^{2}$
$\mathrm{Z}=$ crack control parameter (k/in)
$=130 \mathrm{k} / \mathrm{in}$. for severe exposure conditions
By substituting for $\mathrm{d}_{\mathrm{c}}$, A and Z :

$$
\mathrm{f}_{\mathrm{sa}}=45 \mathrm{ksi}>36 \mathrm{ksi} \text { therefore, use maximum allowable } \mathrm{f}_{\mathrm{sa}}=36 \mathrm{ksi}
$$

Notice that the crack width parameter, Z, for severe exposure conditions was used to account for the remote possibility of the bottom reinforcement being exposed to deicing salts leaching through the deck. Many jurisdictions use Z for moderate exposure conditions when designing the deck bottom reinforcement except for decks in marine environments. The rationale for doing so is that the bottom reinforcement is not directly exposed to salt application. The difference in interpretation rarely affects the design because the maximum allowable stress for the bottom reinforcement, with a 1 in . clear concrete cover, is typically controlled by the $0.6 f_{y}$ limit and will not change if moderate exposure was assumed.

## Stresses under service loads (S5.7.1)

In calculating the transformed compression steel area, the Specifications require the use of two different values for the modular ratio when calculating the service load stresses caused by dead and live loads, $2 n$ and $n$, respectively. For deck design, it is customary to ignore the compression steel in the calculation of service load stresses and, therefore,
this provision is not applicable. For tension steel, the transformed area is calculated using the modular ratio, $n$.

Modular ratio for 4 ksi concrete, $n=8$

Assume stresses and strains vary linearly
Dead load service load moment $=0.93+0.28=1.21 \mathrm{k}$-ft/ft
Live load service load moment $=6.74 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Dead load + live load service load positive moment $=7.95 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$


## Figure 4-4 - Crack Control for Positive Moment Reinforcement Under Live Loads

The transformed moment of inertia is calculated assuming elastic behavior, i.e. linear stress and strain distribution. In this case, the first moment of area of the transformed steel on the tension side about the neutral axis is assumed equal to that of the concrete in compression. The process of calculating the transformed moment of inertia is illustrated in Figure 4-4 and by the calculations below.

For 4 ksi concrete, the modular ratio, $\mathrm{n}=8$ (S6.10.3.1.1b or by dividing the modulus of elasticity of the steel by that of the concrete and rounding up as required by S5.7.1)

Assume the neutral axis is at a distance " $y$ " from the compression face of the section Assume the section width equals the reinforcement spacing $=7 \mathrm{in}$.

The transformed steel area $=($ steel area $)($ modular ratio $)=0.31(8)=2.48 \mathrm{in}^{2}$

By equating the first moment of area of the transformed steel to that of the concrete, both about the neutral axis:

$$
2.48(6.19-y)=7 y(y / 2)
$$

Solving the equation results in $\mathrm{y}=1.77 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{I}_{\text {transformed }} & =2.48(6.19-1.77)^{2}+7(1.77)^{3} / 3 \\
& =61.4 \mathrm{in}^{4}
\end{aligned}
$$

Stress in the steel, $\mathrm{f}_{\mathrm{s}}=(\mathrm{Mc} / \mathrm{I}) \mathrm{n}$, where M is the moment acting on 7 in . width of the deck.

$$
\begin{aligned}
\mathrm{f}_{\mathrm{s}} & =[[(7.95(12 / 12)(7)(4.42)] / 61.4] 8 \\
& =32.05 \mathrm{ksi}
\end{aligned}
$$

Allowable service load stress $=36 \mathrm{ksi}>32.05 \mathrm{ksi}$ OK

## Design Step

4.9

## DESIGN FOR NEGATIVE MOMENT AT INTERIOR GIRDERS

## a. Live load

From Table SA4.1-1, for girder spacing of $9^{\prime}-9^{\prime \prime}$ and the distance from the design section for negative moment to the centerline of the girder equal to 12 in . (see Design Step 4.7 for explanation):

Unfactored live load negative moment per unit width of the deck $=4.21 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Maximum factored negative moment per unit width at the design section for negative moment $=1.75(4.21)=7.37 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$

## b. Dead load

Factored dead load moments at the design section for negative moment:
Dead weight
$1.25(0.93)=1.16 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Future wearing surface
$1.5(0.28)=0.42 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Dead Load + live load design factored negative moment $=1.16+0.42+7.37$

$$
=8.95 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
$$

$\begin{aligned} \mathrm{d} & =\text { distance from compression face to centroid of tension reinforcement (in.) } \\ & =\text { total thickness }- \text { top cover }-1 / 2 \text { bar diameter }\end{aligned}$
Assume \#5 bars; bar diameter $=0.625$ in., bar area $=0.31 \mathrm{in}^{2}$

$$
\begin{aligned}
\mathrm{d} & =8-21 / 2-1 / 2(0.625) \\
& =5.19 \mathrm{in} .
\end{aligned}
$$

Required area of steel $=0.0339 \mathrm{in}^{2} / \mathrm{in}$.
Required spacing $=0.31 / 0.0339=9.15 \mathrm{in}$.
Use \#5 at 9 in. spacing
As indicated earlier, checking the minimum and maximum reinforcement is not expected to control in deck slabs.

Check for cracking under service limit state (S5.7.3.4)
Allowable service load stresses:

$$
\mathrm{f}_{\mathrm{sa}}=\frac{\mathrm{Z}}{\left(\mathrm{~d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3}} \leq 0.6 \mathrm{f}_{\mathrm{y}}=36 \mathrm{ksi}
$$

Concrete cover $=2 \frac{1}{2}$ in. $-1 / 2 \mathrm{in}$. integral wearing surface $=2 \mathrm{in}$.
(Note: maximum clear cover to be used in the analysis $=2 \mathrm{in}$.) (S5.7.3.4)
where:
$d_{c}=$ clear cover $+1 / 2$ bar diameter

$$
=2+1 / 2(0.625)
$$

$$
=2.31 \mathrm{in}
$$

$$
\mathrm{A}=2(2.31)(9)
$$

$$
=41.58 \mathrm{in}^{2}
$$

$$
\mathrm{Z}=130 \mathrm{k} / \mathrm{in} \text {. for severe exposure conditions }
$$

$$
\mathrm{f}_{\mathrm{sa}}=28.38 \mathrm{ksi}
$$

As explained earlier, service load stresses are calculated using a modular ratio, $\mathrm{n}=8$.
Dead load service load moment at the design section for negative moment near the middle $=-1.21 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$.


Figure 4-5a - Crack Control for Negative Moment Reinforcement Under Live Loads

Live load service bad moment at the design section in the first interior bay near the first interior girder $=-4.21 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$.

Transformed section properties may be calculated as done for the positive moment section in Design Step 4.8. Refer to Figure 4-5a for the section dimensions and location of the neutral axis. The calculations are shown below.

Maximum dead load + live load service load moment $=5.42 \mathrm{k}$ - ft/ft

$$
\begin{aligned}
& \mathrm{n}=8 \\
& \mathrm{I}_{\text {transformed }}=43.83 \mathrm{in}^{4}
\end{aligned}
$$

Total DL + LL service load stresses $=[[5.42(9)(3.75)] / 43.83](8)$

$$
=33.39 \mathrm{ksi}>\mathrm{f}_{\mathrm{sa}}=28.38 \mathrm{ksi} \mathbf{N G}
$$

To satisfy the crack control provisions, the most economical change is to replace the reinforcement bars by smaller bars at smaller spacing (area of reinforcement per unit width is the same). However, in this particular example, the \#5 bar size cannot be reduced as this bar is customarily considered the minimum bar size for deck main reinforcement. Therefore, the bar diameter is kept the same and the spacing is reduced.

Assume reinforcement is \#5 at 8 in . spacing (refer to Figure 4-5b).

$$
\mathrm{I}_{\text {transformed }}=42.77 \mathrm{in}^{4}
$$

Total DL + LL service load stresses $=[[5.42(8)(3.68) / 42.77](8)$

$$
=29.85 \mathrm{ksi}
$$

$$
\mathrm{f}_{\mathrm{sa}}=29.52 \mathrm{ksi}
$$

Applied stress $=29.85 \mathrm{ksi} \cong \mathrm{f}_{\mathrm{sa}}=29.52 \mathrm{ksi}$
Use main negative moment reinforcement \#5 at 8 in . spacing


Figure 4-5b - Crack Control for Negative Moment Reinforcement Under Live Loads

## Design Step $\mid$ DESIGN OF THE OVERHANG

4.10


Figure 4-6 - Overhang Region, Dimensions and Truck Loading

Assume that the bottom of the deck in the overhang region is 1 inch lower than the bottom of other bays as shown in Figure 4-6. This results in a total overhang thickness equal to 9 in . This is usually beneficial in resisting the effects of vehicular collision. However, a section in the first bay of the deck, where the thickness is smaller than that of the overhang, must also be checked.

## Assumed loads

Self weight of the slab in the overhang area $=112.5 \mathrm{lb} / \mathrm{ft}^{2}$ of the deck overhang surface area

Weight of parapet $=650 \mathrm{lb} / \mathrm{ft}$ of length of parapet

Future wearing surface $=30 \mathrm{lb} / \mathrm{ft}^{2}$ of deck surface area
As required by SA13.4.1, there are three design cases to be checked when designing the deck overhang regions.

Design Case 1: Check overhang for horizontal vehicular collision load (SA13.4.1, Case 1)


Figure 4-7-Design Sections in the Overhang Region

The overhang is designed to resist an axial tension force from vehicular collision acting simultaneously with the collision + dead load moment.

The resistance factor, $\varphi=1.0$ for extreme event limit state (S1.3.2.1). The Specification requires that load effects in the extreme event limit state be multiplied by $\eta_{i} \geq 1.05$ for bridges deemed important or $\eta_{i} \geq 0.95$ for bridges deemed not important. For this example, a value of $\eta_{i}=1.0$ was used.
a. At inside face of parapet (Section A-A in Figure 4-7)
(see Design Step 4.4 for parapet characteristics)
$\mathrm{M}_{\mathrm{c}}=$ moment capacity of the base of the parapet given as $17.83 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$.
When this moment is transmitted to the deck overhang it subjects the deck to negative moment.

For a complete railing design example that includes sample detailed calculations of railing parameters, see Lecture 16 of the participant notebook of the National Highway Institute Course No. 13061.

$$
\begin{aligned}
\mathrm{M}_{\mathrm{DL}, \text { slab }} & =0.1125(20.25 / 12)^{2} / 2 \\
& =0.16 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
& \\
\mathrm{M}_{\mathrm{DL}, \text { parapet }} & =0.65(20.25-7.61) / 12 \\
& =0.68 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Design factored moment $=-17.83-1.25(0.16+0.68)=-18.88 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$

Design axial tensile force (SA13.4.2) $=\mathrm{R}_{W} /\left(\mathrm{L}_{\mathrm{c}}+2 \mathrm{H}\right)$

$$
\begin{aligned}
& =137.22 /[(235.2+2(42) / 12] \\
& =5.16 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

h slab $=9 \mathrm{in}$.
Assuming \#5 reinforcement bars,
d = overhang slab thickness - top cover $-1 / 2$ bar diameter $=9-21 / 2-1 / 2(0.625)$ $=6.19 \mathrm{in}$.

Assume required area of steel $=0.70 \mathrm{in}^{2} / \mathrm{ft}$
The over-reinforced section check is not expected to control. However, due to the additional reinforcement in the overhang, it is prudent to perform this check using the provisions of S5.7.3.3.1.

Effective depth of the section, $\mathrm{h}=6.19 \mathrm{in}$.
(Notice that the overhang has 1 inch additional thickness at its bottom)
For a section under moment and axial tension, P , the nominal resistance, $\mathrm{M}_{\mathrm{n}}$, may be calculated as:

$$
\mathrm{M}_{\mathrm{n}}=\mathrm{T}(\mathrm{~d}-\mathrm{a} / 2)-\mathrm{P}(\mathrm{~h} / 2-\mathrm{a} / 2)
$$

Tension in reinforcement, $\mathrm{T}=0.70(60)=42.0 \mathrm{k} / \mathrm{ft}$
Compression in concrete, $\mathrm{C}=42.0-5.16=36.84 \mathrm{k} / \mathrm{ft}$

$$
\begin{aligned}
\mathrm{a} & =\mathrm{C} / \mathrm{b} \beta_{1} \mathrm{f}_{\mathrm{c}} \\
& =36.84 /[12(0.85)(4)] \\
& =0.90 \mathrm{in} . \\
\mathrm{M}_{\mathrm{n}} & =42.0[6.19-(0.9 / 2)]-5.16[(6.19 / 2)-(0.9 / 2)] \\
& =227.43 / 12 \\
& =18.95 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Notice that many designers determine the required reinforcement for sections under moment and axial tension, P , as the sum of two components:

1) the reinforcement required assuming the section is subjected to moment
2) $P / f_{y}$

This approach is acceptable as it results in more conservative results, i.e., more reinforcement.

Resistance factor $=1.0$ for extreme event limit state $($ S1.3.2.1 $)$

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =\varphi \mathrm{M}_{\mathrm{n}} \\
& =1.0(18.95)=18.95 \mathrm{k}-\mathrm{ft} / \mathrm{ft}>\mathrm{M}_{\mathrm{u}}=18.88 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \quad \mathbf{O K}
\end{aligned}
$$

$$
\mathrm{c} / \mathrm{d}_{\mathrm{e}}=(0.9 / 0.85) /(6.19)=0.17<0.42 \text { steel yields before concrete crushing, i.e., }
$$ the section is not over-reinforced

## b. At design section in the overhang (Section B-B in Figure 4-7)

Assume that the minimum haunch thickness is at least equal to the difference between the thickness of the interior regions of the slab and the overhang thickness, i.e., 1 in . This means that when designing the section in the overhang at 14 in . from the center of the girder, the total thickness of the slab at this point can be assumed to be 9 in . For thinner haunches, engineering judgment should be exercised to determine the thickness to be considered at this section.

At the inside face of the parapet, the collision forces are distributed over a distance $L_{c}$ for the moment and $L_{c}+2 H$ for axial force. It is reasonable to assume that the distribution length will increase as the distance from the section to the parapet increases. The value of the distribution angle is not specified in the specifications and is determined using engineering judgment. In this example, the distribution length was increased at a $30^{\circ}$ angle from the base of the parapet (see Figure 48). Some designers assume a distribution angle of $45^{\circ}$, this angle would have also been acceptable.


Figure 4-8 - Assumed Distribution of Collision Moment Load in the Overhang

Collision moment at the design section $=\mathrm{M}_{\mathrm{c}} \mathrm{L}_{\mathrm{c}} /\left[\mathrm{L}_{\mathrm{c}}+2(0.577) \mathrm{X}\right]$

$$
\begin{aligned}
& =-17.83(235.2) /[235.2+2(0.577)(8)] \\
& =-17.16 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Dead load moment at the design section:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{DL}, \text { slab }} & =0.1125(28.25 / 12)^{2} / 2 \\
& =0.31 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
& \\
\mathrm{M}_{\mathrm{DL}, \text { parapet }} & =0.65(28.25-7.61) / 12 \\
& =1.12 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
& \\
\mathrm{M}_{\mathrm{DL}, \text { FWS }} & =0.03(8 / 12)^{2} / 2 \\
& =0.007 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Factored design $\mathrm{M}=-17.16-1.25(0.31+1.12)-1.5(0.007)=-18.96 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Design tensile force $=\mathrm{R}_{\mathrm{w}} /\left[\mathrm{L}_{\mathrm{c}}+2 \mathrm{H}+2(0.577) \mathrm{X}\right]$

$$
\begin{aligned}
& =137.22 /[[235.2+2(42)+2(0.577)(8)] / 12] \\
& =5.01 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

$$
\text { h slab }=9 \mathrm{in} .
$$

By inspection, for Section AA, providing an area of steel $=0.70 \mathrm{in}^{2} / \mathrm{ft}$ resulted in a moment resistance of $18.95 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \cong$ the design moment for Section B-B.

Therefore, the required area of steel for Section B-B $=0.70 \mathrm{in}^{2} / \mathrm{ft}$

## c. Check dead load + collision moments at design section in first span (Section C-C in Figure 4-7)

The total collision moment can be treated as an applied moment at the end of a continuous strip. The ratio of the moment $M_{2} / M_{1}$ (see Figure 4-9) can be calculated for the transverse design strip. As an approximation, the ratio $M_{2} / M_{1}$ may be taken equal to 0.4. This approximation is based on the fact that $M_{2} / M_{1}=0.5$ if the rotation at the first interior girder is restrained. Since this rotation is not restrained, the value of $M_{2}$ will be less than $0.5 M_{1}$. Thus, the assumption that $M_{2} / M_{1}=0.4$ seems to be reasonable. The collision moment per unit width at the section under consideration can then be determined by dividing the total collision moment by the distribution length. The distribution length may be determined using the $30^{\circ}$ distribution as illustrated in Figure $4-8$ except that the distance " $X$ " will be 36 in. for Section C.

The dead load moments at the design section for negative moment to the inside of the exterior girder may be determined by superimposing two components: (1) the moments in the first deck span due to the dead loads acting on the overhang (see Figure 410), and (2) the effect of the dead loads acting on the first span of the deck (see Figure 4-11).


Figure 4-9 - Assumed Distribution of the Collision Moment Across the Width of the Deck


Figure 410 - Dead Load Moment at Design Section Due to Dead Loads on the Overhang


Figure 4-11 - Dead Load Moment at Design Section Due to Dead Loads on the First Deck Span

Collision moment at exterior girder, $\mathrm{M}_{1}=-17.83 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Collision moment at first interior girder, $\mathrm{M}_{2}=0.4(17.83)=7.13 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$

By interpolation for a section in the first interior bay at 14 in . from the exterior girder:
Total collision moment $=-17.83+14(17.83+7.13) / 116=-14.81 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$

Using the $30^{\circ}$ angle distribution, as shown in Figure 4-8:
Design collision moment $=-14.81 \mathrm{~L}_{\mathrm{c}} /\left[\mathrm{L}_{\mathrm{c}}+2(0.577)(22+14)\right]=-12.59 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
where $L_{c}=235.2 \mathrm{in}$.
Dead load moment at the centerline of the exterior girder:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{DL}, \text { Slab }} & =-0.1125(42.25 / 12)^{2} / 2 \\
& =-0.70 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
\mathrm{M}_{\mathrm{DL}, \text { Parapet }} & =-0.65(42.25-7.61) / 12 \\
& =-1.88 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
\mathrm{M}_{\mathrm{DL}, \text { FWS }} & =-0.03[(42.25-20.25) / 12]^{2} / 2 \\
& =-0.05 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Factored dead load moment at the centerline of the exterior girder:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{FDL}} & =1.25(-0.70)+1.25(-1.88)+1.5(-0.05) \\
& =-3.3 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Based on Figure 4-10
The design factored dead load moment at the design section due to loads on the overhang is:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{FDL}, \mathrm{O}} & =0.83(-3.3) \\
& =-2.74 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

From Figure 4 11, the dead load design factored moment due to DL on the first deck span is:

$$
\begin{aligned}
\mathrm{M} & =1.25\left[0.1125\left[0.4(9.66)(14 / 12)-(14 / 12)^{2} / 2\right]\right]+1.5\left[0.03\left[0.4(9.66)(14 / 12)-(14 / 12)^{2} / 2\right]\right] \\
& =0.71 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Total design dead load + collision moment:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{DL}+\mathrm{C}} & =-12.59-2.74+0.71 \\
& =-14.62 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Resistance factor $=1.0$ for extreme event limit state $($ S1.3.2.1 $)$
Assuming the slab thickness at this section equals 8 in. and the effective depth equals 5.19 in.;

Required area of steel $=0.62 \mathrm{in}^{2} / \mathrm{ft}$

## Design Case 2: Vertical collision force (SA13.4.1, Case 2)

For concrete parapets, the case of vertical collision never controls
Design Case 3: Check DL + LL (SA13.4.1, Case 3)
Except for decks supported on widely spaced girders (approximately 12 ft . and 14 ft . girder spacing for girders with narrow flanges and wide flanges, respectively), Case 3 does not control the design of decks supporting concrete parapets. Widely spaced girders allow the use of wider overhangs which in turn may lead to live load moments that may exceed the collision moment and, thus, control the design. The deck of this example is highly unlikely to be controlled by Case 3. However, this case is checked to illustrate the complete design process.

Resistance factor $=0.9$ for strength limit state $($ S5.5.4.2.1 $)$.

## a. Design section in the overhang (Section B-B in Figure 4-7)

The live load distribution width equations for the overhang (S4.6.2.1.3) are based on assuming that the distance from the design section in the overhang to the face of the parapet exceeds 12 in . such that the concentrated load representing the truck wheel is located closer to the face of the parapet than the design section. As shown in Figure 412, the concentrated bad representing the wheel load on the overhang is located to the inside of the design section for negative moment in the overhang. This means that the distance " X " in the distribution width equation is negative which was not intended in developing this equation. This situation is becoming common as prestressed girders with wide top flanges are being used more frequently. In addition, Figure 4-6 may be wrongly interpreted as that there is no live load negative moment acting on the overhang. This would be misleading since the wheel load is distributed over the width of the wheels in the axle. Live load moment in these situations is small and is not expected to control design. For such situations, to determine the live load design moment in the overhang, either of the following two approaches may be used:

1) The design section may be conservatively assumed at the face of the girder web, or
2) The wheel load may be distributed over the width of the wheels as shown in Figure 4-12 and the moments are determined at the design section for negative moment. The distribution width may be calculated assuming " X " as the distance from the design section to the edge of the wheel load nearest the face of the parapet.

The latter approach is used in this example. The wheel load is assumed to be distributed over a tire width of 20 in . as specified in S3.6.1.2.5.


Figure 4-12 - Overhang Live Load - Distributed Load

Using the multiple presence factor for a single truck $=1.2$ (S3.6.1.1.2) and dynamic load allowance for truck loading $=1.33$ (S3.6.2.1), live load moment may be determined.

Equivalent strip width for live load $=45+10(6 / 12)$

$$
=50 \text { in. }(\mathrm{S} 4.6 .2 .1 .3)
$$

Design factored moment:

$$
\begin{align*}
\mathrm{M}_{\mathrm{n}}= & -1.25(0.1125)[(42.25-14) / 12]^{2} / 2 \\
& -1.25(0.65)(42.25-14-7.61) / 12 \\
& -1.5(0.03)[(42.25-20.25-14) / 12]^{2} / 2 \\
& -1.75(1.33)(1.2)\left[16 /(20 / 12)\left[\left((6 / 12)^{2} / 2\right) /(50 / 12)\right]\right. \\
= & -2.60 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
\mathrm{~d}= & 6.19 \mathrm{in} . \tag{4}
\end{align*}
$$

Required area of steel $=0.09 \mathrm{in}^{2} / \mathrm{ft}$
b. Check dead load + live load moments at design section in first span (Section C-C in Figure 4-7)


Figure 4-13 - Overhang Live Load

Assume slab thickness at this section $=8$ in. (conservative to ignore the haunch)
Based on the earlier calculations for this section under collision + DL, DL factored moment at the section $=-2.74 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$.

Determining live load at this section may be conducted by modeling the deck as a beam supported on the girders and by moving the design load across the width of the deck to generate the moment envelopes. However, this process implies a degree of accuracy that may not be possible to achieve due to the approximate nature of the distribution width and other assumptions involved, e.g., the girders are not infinitely rigid and the top flange is not a point support. An approximate approach suitable for hand calculations is illustrated in Figure 4-13. In this approximate approach, the first axle of the truck is applied to a simply supported beam that consists of the first span of the deck and the overhang. The negative moment at the design section is then calculated. The multiple presence factor for a single lane (1.2) and dynamic load allowance (33\%) are also applied. Based on the dimensions and the critical location of the truck axle shown in Figure 4-13, the unfactored live load moment at the design section for negative moment is $3.03 \mathrm{k}-\mathrm{ft}$.

Live load moment (including the load factor, dynamic load allowance and multiple presence factor $)=3.03(1.75)(1.33)(1.2)=8.46 \mathrm{k}-\mathrm{ft}$

Since the live load negative moment is produced by a load on the overhang, use the overhang strip width at the girder centerline.

Equivalent strip width $=45+10(10 / 12)=53.3$ in. $(S 4.6 .2 .1 .3)$
Design factored moment $(\mathrm{DL}+\mathrm{LL})=2.74+8.46 /(53.3 / 12)$

$$
\begin{equation*}
=4.65 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \tag{5}
\end{equation*}
$$

Required area of steel $=0.19 \mathrm{in}^{2} / \mathrm{ft}$

## DETAILING OF OVERHANG REINFORCEMENT

From the different design cases of the overhang and the adjacent region of the deck, the required area of steel in the overhang is equal to the largest of (1), (2), (3), (4) and (5) $=0.7 \mathrm{in}^{2} / \mathrm{ft}$

The provided top reinforcement in the slab in regions other than the overhang region is: $\# 5$ at 8 in. $=0.31(12 / 8)=0.465 \mathrm{in}^{2} / \mathrm{ft}$
$0.465 \mathrm{in}^{2} / \mathrm{ft}$ provided $<0.7 \mathrm{in}^{2} / \mathrm{ft}$ required, therefore, additional reinforcement is required in the overhang.

Bundle one \#4 bar to each top bar in the overhang region of the deck.

Provided reinforcement $=(0.2+0.31)(12 / 8)=0.76 \mathrm{in}^{2} / \mathrm{ft}>0.7 \mathrm{in}^{2} / \mathrm{ft}$ required OK.
Notice that many jurisdictions require a \#5 minimum bar size for the top transverse reinforcement. In this case, the \#4 bars used in this example would be replaced by \#5 bars. Alternatively, to reduce the reinforcement area, a \#5 bar may be added between the alternating main bars if the main bar spacing would allow adding bars in between without resulting in congested reinforcement.

Check the depth of the compression block:

$$
\begin{aligned}
\mathrm{T} & =60(0.76) \\
& =45.6 \mathrm{kips} \\
\mathrm{a} & =45.6 /[0.85(4)(12)] \\
& =1.12 \mathrm{in} . \\
\beta_{1} & =0.85 \text { for } \mathrm{f}_{\mathrm{c}}=4 \mathrm{ksi} \\
\mathrm{c} & =1.12 / 0.85 \\
& =1.32 \mathrm{in} .
\end{aligned}
$$

Among Sections A, B and C of Figure 4-7, Section C has the least slab thickness. Hence, the ratio $c / d_{e}$ is more critical at this section.

$$
\mathrm{d}_{\mathrm{e}} \text { at Section C-C = } 5.19 \mathrm{in} .
$$

Maximum $c / d_{e}=1.32 / 5.19=0.25<0.42$ OK (S5.7.3.3.1)

Cracking under service load in the overhang needs to be checked. The reinforcement area in the overhang is $65 \%$ larger than the negative moment reinforcement in the interior portions of the deck, yet the applied service moment $(2.74+3.03=5.77 \mathrm{k}$ - $\mathrm{ft} / \mathrm{ft})$ is $6 \%$ larger than the service moment at interior portions of the deck $(5.42 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$ from Step 4.9). By inspection, cracking under service load does not control.

Determine the point in the first bay of the deck where the additional bars are no longer needed by determining the point where both (DL + LL) moment and (DL + collision) moments are less than or equal to the moment of resistance of the deck slab without the additional top reinforcement. By inspection, the case of (DL + LL) does not control and only the case of (DL + collision) needs to be checked.

Negative moment resistance of the deck slab reinforced with \#5 bars at 8 in . spacing is $10.15 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$ for strength limit state (resistance factor $=0.9$ ), or $11.27 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$ for the extreme event limit state (resistance factor $=1.0$ ). By calculating the moments at different points along the deck first span in the same manner they were calculated for Section C-C for (DL + collision), it was determined that the design negative moment is
less than $11.27 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$ at a point approximately 25 in . from the centerline of the exterior girder.

The theoretical termination point from the centerline of the exterior girder is 25 in .

Extend the additional bars beyond this point for a distance equal to the cut-off length. In addition, check that the provided length measured beyond the design section for moment is larger than the development length (S5.11.1.2.1).

## Cut-off length requirement (S5.11.1.2.1)

Checking the three requirements of S5.11.1.2.1, the cut-off length is controlled by 15 times the bar diameter.

Cut-off length $=15(0.625)=9.375 \mathrm{in}$.
Required length past the centerline of the exterior girder $=25+9.375$

$$
=34.375 \mathrm{in}
$$

## Development length (S5.11.2)

The basic development length, $\left.\right|_{\mathrm{db}}$, is taken as the larger of:

$$
\frac{1.25 \mathrm{~A}_{\mathrm{b}} \mathrm{f}_{\mathrm{y}}}{\sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}}}=\frac{1.25(0.31)(60)}{\sqrt{4}}=11.625 \mathrm{in} .
$$

OR

$$
0.4 \mathrm{~d}_{\mathrm{b}} \mathrm{f}_{\mathrm{y}}=0.4(0.625)(60)=15 \mathrm{in} .
$$

OR
12 in.

Therefore, the basic development length $=15 \mathrm{in}$.
Correction factors:
Epoxy-coated bars $=1.2($ S5.11.2.1.2 $)$
Two bundled bars $=1.0$ (S5.11.2.3)
Spacing > 6 in. $=0.8($ S5.11.2.1.3 $)$

Development length $=15(1.2)(1.0)(0.8)=14.4 \mathrm{in}$.
Required length of the additional bars past the centerline of the exterior girder $=14+$ $14.4=28.4 \mathrm{in} .<34.375 \mathrm{in}$. (needed to be satisfy cut off requirements) OK

Extend the additional bars in the overhang a minimum of 34.375 in . (say 3 ft .) beyond the centerline of the exterior girder.


Figure 4-14 - Length of the Overhang Additional Bars

LONGITUDINAL REINFORCEMENT

Percentage of longitudinal reinforcement $=\frac{220}{\sqrt{\mathrm{~S}}} \leq 67 \%$
where:
$\mathrm{S}=$ the effective span length taken as equal to the effective length specified in S9.7.2.3 (ft.); the distance between sections for negative moment and sections at the ends of one deck span

$$
\begin{aligned}
& =(116-14-14)(12) \\
& =7.33 \mathrm{ft} .
\end{aligned}
$$

Percentage $=\frac{220}{\sqrt{7.33}}=81 \%>67 \%$

Use $67 \%$ of transverse reinforcement
Transverse reinforcement $=\# 5$ at 7 in . spacing $=0.53 \mathrm{in}^{2} / \mathrm{ft}$
Required longitudinal reinforcement $=0.67(0.53)=0.36 \mathrm{in}^{2} / \mathrm{ft}$
Use \#5 bars; bar diameter $=0.625 \mathrm{in}$., bar area $=0.31 \mathrm{in}^{2}$
Required spacing $=0.31 / 0.36=0.86 \mathrm{ft} .(10.375 \mathrm{in}$.
Use \#5 bars at 10 in . spacing

## Top longitudinal reinforcement

There are no specific requirements to determine this reinforcement. Many jurisdictions use \#4 bars at 12 in . spacing for the top longitudinal reinforcement.

## Design Step

DECK TOP LONGITUDINAL REINFORCEMENT IN THE GIRDER NEGATIVE MOMENT REGION, I.E., OVER THE INTERMEDIATE SUPPORTS OF THE GIRDERS

For simple span precast girders made continuous for live load: design according to S5.14.1.2.7
(Notice that for continuous steel girders, this reinforcement is designed according to S6.10.3.7.)

The required reinforcement area is determined during girder design. See Section 5.6 for the calculations for this reinforcement.

Provided reinforcement area $=14.65 \mathrm{in}^{2}$

Use \#6 bars at 5.5 in . spacing in the top layer \#6 bars at 8.5 in. spacing in the bottom layer

## Design Step $\mid$ CHECK SHRINKAGE AND TEMPERATURE REINFORCEMENT <br> 4.14 ACCORDING TO S5.10.8

Reinforcement for shrinkage and temperature stresses is provided near surfaces of concrete exposed to daily temperature changes. Shrinkage and temperature reinforcement is added to ensure that the total reinforcement on exposed surfaces is not less than the following:

$$
\begin{equation*}
\mathrm{A}_{\mathrm{s}} \geq 0.11 \mathrm{~A}_{\mathrm{g}} / \mathrm{f}_{\mathrm{y}} \tag{S5.10.8.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{g}} & =\text { gross area of the section }\left(\mathrm{in}^{2}\right) \\
& =12(7.5) \\
& =90 \mathrm{in}^{2} / \mathrm{ft} . \text { width of deck } \\
\mathrm{f}_{\mathrm{y}} & =\text { specified yield strength of the reinforcing bars }(\mathrm{ksi}) \\
& =60 \mathrm{ksi}
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s} \text { req }} & =0.11(90 / 60) \\
& =0.165 \mathrm{in}^{2} / \mathrm{ft} . \text { width of deck }
\end{aligned}
$$

This area should be divided between the two surfaces, $\mathrm{A}_{\text {s req }}$ per surface $=0.0825 \mathrm{in}^{2} / \mathrm{ft}$. width of deck.

Assuming longitudinal reinforcement is \#4 bars at 12 in . spacing:
$\mathrm{A}_{\mathrm{s} \text {, provided }}=0.2 \mathrm{in}^{2} / \mathrm{ft}$. width of deck $>0.0825 \mathrm{in}^{2} / \mathrm{ft}$. width of deck required $\mathbf{O K}$


Figure 4-15 - Deck Reinforcement at Midspan of Girders


Figure 4-16 - Deck Reinforcement at Intermediate Pier

# Prestressed Concrete Bridge Design Example 

## Design Step LIVE LOAD DISTRIBUTION FACTORS <br> 5.1 (S4.6.2.2)

The AASHTO-LRFD Specifications allow the use of advanced methods of analysis to determine the live load distribution factors. However, for typical bridges, the specifications list equations to calculate the distribution factors for different types of bridge superstructures. The types of superstructures covered by these equations are described in Table S4.6.2.2.1-1. From this table, bridges with concrete decks supported on precast concrete I or bulb-tee girders are designated as cross-section " $K$ ". Other tables in S4.6.2.2.2 list the distribution factors for interior and exterior girders including cross-section " $K$ ". The distribution factor equations are largely based on work conducted in the NCHRP Project 12-26 and have been verified to give accurate results compared to 3-dimensional bridge analysis and field measurements. The multiple presence factors are already included in the distribution factor equations except when the tables call for the use of the lever rule. In these cases, the computations need to account for the multiple presence factors. Notice that the distribution factor tables include a column with the heading "range of applicability". The ranges of applicability listed for each equation are based on the range for each parameter used in the study leading to the development of the equation. When the girder spacing exceeds the listed value in the "range of applicability" column, the specifications require the use of the lever rule (S4.6.2.2.1). One or more of the other parameters may be outside the listed range of applicability. In this case, the equation could still remain valid, particularly when the value(s) is(are) only slightly out of the range of applicability. However, if one or more of the parameters greatly exceed the range of applicability, engineering judgment needs to be exercised.

Article S4.6.2.2.2d of the specifications states: "In beam-slab bridge cross-sections with diaphragms or cross-frames, the distribution factor for the exterior beam shall not be taken less than that which would be obtained by assuming that the cross-section deflects and rotates as a rigid cross-section". This provision was added to the specifications because the original study that developed the distribution factor equations did not consider intermediate diaphragms. Application of this provision requires the presence of a sufficient number of intermediate diaphragms whose stiffness is adequate to force the cross section to act as a rigid section. For prestressed girders, different jurisdictions use different types and numbers of intermediate diaphragms. Depending on the number and stiffness of the intermediate diaphragms, the provisions of S4.6.2.2.2d may not be applicable. For this example, one deep reinforced concrete diaphragm is located at the midspan of each span. The stiffness of the diaphragm was deemed sufficient to force the cross-section to act as a rigid section, therefore, the provisions of S4.6.2.2.2d apply.

Notice that the AASHTO Standard Specifications express the distribution factors as a fraction of wheel lines, whereas the AASHTO-LRFD Specifications express them as a fraction of full lanes.

For this example, the distribution factors listed in S4.6.2.2.2 will be used.

Notice that fatigue in the prestressing steel need not be checked for conventional prestressed girders (S5.5.3) when maximum stress in the concrete at Service III limit state is taken according to Table S5.9.4.2.2-1. This statement is valid for this example. The fatigue distribution factors are calculated in the following sections to provide the user with a complete reference for the application of the LRFD distribution factors.

Required information:
AASHTO Type I-Beam (28/72)
Noncomposite beam area, $\mathrm{Ag}_{\mathrm{g}}$

$$
=1,085 \mathrm{in}^{2}
$$

Noncomposite beam moment of inertia, $\mathrm{I}_{\mathrm{g}} \quad=733,320 \mathrm{in}^{4}$
Deck slab thickness, $\mathrm{t}_{\mathrm{s}} \quad=8 \mathrm{in}$.
Span length, L $=110 \mathrm{ft}$.
Girder spacing, S
$=9 \mathrm{ft}$. -8 in .
Modulus of elasticity of the beam, $\mathrm{E}_{\mathrm{B}}$
$=4,696 \mathrm{ksi}($ S5.4.2.4 $)$
Modulus of elasticity of the deck, $\mathrm{E}_{\mathrm{D}}$
$=3,834 \mathrm{ksi}($ S5.4.2.4 $)$
C.G. to top of the basic beam $=35.62 \mathrm{in}$.
C.G. to bottom of the basic beam $=36.38 \mathrm{in}$.

Design Step
5.1.1

$$
\begin{align*}
\mathrm{n} & =\mathrm{E}_{\mathrm{B}} / \mathrm{E}_{\mathrm{D}}  \tag{S4.6.2.2.1-2}\\
& =4,696 / 3,834 \\
& =1.225
\end{align*}
$$

Design Step
Calculate $\mathrm{e}_{\mathrm{g}}$, the distance between the center of gravity of the noncomposite beam and the deck. Ignore the thickness of the haunch in determining eg. It is also possible to ignore the integral wearing surface, i.e., use $t_{5}=7.5 \mathrm{in}$. However the difference in the distribution factor will be minimal.

$$
\begin{aligned}
\mathrm{e}_{\mathrm{g}} & =\mathrm{NA} A_{\mathrm{YT}}+\mathrm{t}_{\mathrm{s}} / 2 \\
& =35.62+8 / 2 \\
& =39.62 \mathrm{in} .
\end{aligned}
$$

Calculate $\mathrm{K}_{\mathrm{g}}$, the longitudinal stiffness parameter.

$$
\begin{align*}
\mathrm{K}_{\mathrm{g}} & =\mathrm{n}\left(\mathrm{I}+\mathrm{Ae}_{\mathrm{g}}{ }^{2}\right)  \tag{S4.6.2.2.1-1}\\
& =1.225\left[733,320+1,085(39.62)^{2}\right] \\
& =2,984,704 \mathrm{in}^{4}
\end{align*}
$$

## Interior girder

5.1.4

Calculate the moment distribution factor for an interior beam with two or more design lanes loaded using Table S4.6.2.2.2b-1.

$$
\mathrm{D}_{\mathrm{M}}=0.075+(\mathrm{S} / 9.5)^{0.6}(\mathrm{~S} / \mathrm{L})^{0.2}\left(\mathrm{~K}_{\mathrm{g}} / 12.0 \mathrm{Lt}_{\mathrm{s}}^{3}\right)^{0.1}
$$

$$
\begin{align*}
& =0.075+(9.667 / 9.5)^{0.6}(9.667 / 110)^{0.2}\left[2,984,704 /\left[12(110)(8)^{3}\right]\right]^{0.1} \\
& =0.796 \text { lane } \tag{1}
\end{align*}
$$

Design Step
5.1.5

According to S4.6.2.2.2e, a skew correction factor for moment may be applied for bridge skews greater than 30 degrees. The bridge in this example is skewed 20 degrees, and, therefore, no skew correction factor for moment is allowed.

Calculate the moment distribution factor for an interior beam with one design lane loaded using Table S4.6.2.2.2b-1.

$$
\begin{align*}
\mathrm{D}_{\mathrm{M}} & =0.06+(\mathrm{S} / 14)^{0.4}(\mathrm{~S} / \mathrm{L})^{0.3}\left(\mathrm{~K}_{\mathrm{g}} / 12.0 \mathrm{Lt}_{\mathrm{s}}^{3}\right)^{0.1} \\
& =0.06+(9.667 / 14)^{0.4}(9.667 / 110)^{0.3}\left[2,984,704 /\left[12(110)(8)^{3}\right]\right]^{0.1} \\
& =0.542 \text { lane } \tag{2}
\end{align*}
$$

Notice that the distribution factor calculated above for a single lane loaded already includes the 1.2 multiple presence factor for a single lane, therefore, this value may be used for the service and strength limit states. However, multiple presence factors should not be used for the fatigue limit state. Therefore, the multiple presence factor of 1.2 for the single lane is required to be removed from the value calculated above to determine the factor used for the fatigue limit state.

For single-lane loading to be used for fatigue design, remove the multiple presence factor of 1.2.

$$
\begin{align*}
\mathrm{D}_{\mathrm{M}} & =0.542 / 1.2 \\
& =0.452 \text { lane } \tag{3}
\end{align*}
$$

## Design Step

5.1.6

## Skew correction factor for shear

According to S4.6.2.2.3c, a skew correction factor for support shear at the obtuse corner must be applied to the distribution factor of all skewed bridges. The value of the correction factor is calculated using Table S4.6.2.2.3c-1

$$
\begin{aligned}
\mathrm{SC} & =1.0+0.20\left(12.0 \mathrm{Lt}_{\mathrm{s}}^{3} / \mathrm{K}_{\mathrm{g}}\right)^{0.3} \tan \theta \\
& =1.0+0.20\left[\left[12.0(110)(8)^{3}\right] / 2,984,704\right]^{0.3} \tan 20 \\
& =1.047
\end{aligned}
$$

Calculate the shear distribution factor for an interior beam with two or more design lanes loaded using Table S4.6.2.2.3a-1.

$$
\mathrm{D}_{\mathrm{V}}=0.2+(\mathrm{S} / 12)-(\mathrm{S} / 35)^{2}
$$

$$
\begin{aligned}
& =0.2+(9.667 / 12)-(9.667 / 35)^{2} \\
& =0.929 \text { lane }
\end{aligned}
$$

Apply the skew correction factor:

$$
\begin{align*}
\mathrm{D}_{\mathrm{V}} & =1.047(0.929) \\
& =0.973 \text { lane } \tag{4}
\end{align*}
$$

## Design Step

5.1.8
using Table S4.6.2.2.3a-1.

$$
\begin{aligned}
\mathrm{D}_{\mathrm{V}} & =0.36+(\mathrm{S} / 25.0) \\
& =0.36+(9.667 / 25.0) \\
& =0.747 \text { lane }
\end{aligned}
$$

Apply the skew correction factor:

$$
\begin{align*}
\mathrm{D}_{\mathrm{V}} & =1.047(0.747) \\
& =0.782 \text { lane } \tag{5}
\end{align*}
$$

For single-lane loading to be used for fatigue design, remove the multiple presence factor of 1.2.

$$
\begin{align*}
\mathrm{D}_{\mathrm{V}} & =0.782 / 1.2 \\
& =0.652 \text { lane } \tag{6}
\end{align*}
$$

## Design Step

From (1) and (2), the service and strength limit state moment distribution factor for the interior girder is equal to the larger of 0.796 and 0.542 lane. Therefore, the moment distribution factor is 0.796 lane.

From (3):
The fatigue limit state moment distribution factor is 0.452 lane
From (4) and (5), the service and strength limit state shear distribution factor for the interior girder is equal to the larger of 0.973 and 0.782 lane. Therefore, the shear distribution factor is 0.973 lane.

From (6):
The fatigue limit state shear distribution factor is 0.652 lane

## Design Step <br> 5.1.10

Figure 5.1-1 - Lever Rule

Design Step
5.1.11

Exterior girder


Calculate the moment distribution factor for an exterior beam with two or more design lanes using Table S4.6.2.2.2d-1.

$$
\begin{aligned}
& \mathrm{D}_{\mathrm{M}}=\mathrm{e} \mathrm{D}_{\text {MInterior }} \\
& \\
& \mathrm{e}=0.77+\mathrm{d}_{\mathrm{e}} / 9.1
\end{aligned}
$$

where $d_{e}$ is the distance from the centerline of the exterior girder to the inside face of the curb or barrier.
$\mathrm{e}=0.77+1.83 / 9.1$ $=0.97$

$$
\begin{align*}
\mathrm{D}_{\mathrm{M}} & =0.97(0.796) \\
& =0.772 \text { lane } \tag{7}
\end{align*}
$$

Design Step
Calculate the moment distribution factor for an exterior beam with one design lane using

### 5.1.12

 the lever rule as per Table S4.6.2.2.2d-1.$$
\begin{aligned}
\mathrm{D}_{\mathrm{M}} & =[(3.5+6)+3.5] / 9.667 \\
& =1.344 \text { wheels } / 2 \\
& =0.672 \text { lane }
\end{aligned}
$$

(8) (Fatigue)

Notice that this value does not include the multiple presence factor, therefore, it is adequate for use with the fatigue limit state. For service and strength limit states, the multiple presence factor for a single lane loaded needs to be included.

$$
\begin{aligned}
\mathrm{D}_{\mathrm{M}} & =0.672(1.2) \\
& =0.806 \text { lane }
\end{aligned}
$$

(9) (Strength and Service)

Design Step
5.1.13

Calculate the shear distribution factor for an exterior beam with two or more design lanes loaded using Table S4.6.2.2.3b-1.

$$
\mathrm{D}_{\mathrm{V}}=\mathrm{e} \mathrm{D}_{\text {Vinterior }}
$$

where:

$$
\begin{aligned}
\mathrm{e} & =0.6+\mathrm{d}_{\mathrm{e}} / 10 \\
& =0.6+1.83 / 10 \\
& =0.783
\end{aligned}
$$

$$
\begin{align*}
\mathrm{D}_{\mathrm{V}} & =0.783(0.973) \\
& =0.762 \text { lane } \tag{10}
\end{align*}
$$

Design Step
5.1.14

## Design Step

5.1.15
(11) (Fatigue)
(12) (Strength and Service)

Notice that S4.6.2.2.2d includes additional requirements for the calculation of the distribution factors for exterior girders when the girders are connected with relatively stiff cross-frames that force the cross-section to act as a rigid section. As indicated in Design Step 5.1, these provisions are applied to this example; the calculations are shown below.

Additional check for rigidly connected girders (S4.6.2.2.2d)
The multiple presence factor, m , is applied to the reaction of the exterior beam (Table S3.6.1.1.2-1)

$$
\begin{aligned}
& \mathrm{m}_{1}=1.20 \\
& \mathrm{~m}_{2}=1.00
\end{aligned}
$$

$$
\begin{align*}
& \mathrm{m}_{3}=0.85 \\
& \mathrm{R}=\mathrm{N}_{\mathrm{L}} / \mathrm{N}_{\mathrm{b}}+\mathrm{X}_{\mathrm{ext}}(\Sigma \mathrm{e}) / \Sigma \mathrm{x}^{2} \tag{SC4.6.2.2.2d-1}
\end{align*}
$$

where:
$\mathrm{R}=$ reaction on exterior beam in terms of lanes
$\mathrm{N}_{\mathrm{L}}=$ number of loaded lanes under consideration
e = eccentricity of a design truck or a design land load from the center of gravity of the pattern of girders (ft.)
$\mathrm{x}=$ horizontal distance from the center of gravity of the pattern of girders to each girder (ft.)
$\mathrm{X}_{\mathrm{ext}}=$ horizontal distance from the center of gravity of the pattern to the exterior girder (ft.)

See Figure 5.1-1 for dimensions.
One lane loaded (only the leftmost lane applied):

$$
\begin{aligned}
\mathrm{R} & =1 / 6+24.167(21) /\left[2\left(24.167^{2}+14.5^{2}+4.833^{2}\right)\right] \\
& =0.1667+0.310 \\
& =0.477
\end{aligned}
$$

Add the multiple presence factor of 1.2 for a single lane:

$$
\begin{aligned}
\mathrm{R} & =1.2(0.477) \\
& =0.572
\end{aligned}
$$

(Strength)
Two lanes loaded:

$$
\begin{aligned}
\mathrm{R} & =2 / 6+24.167(21+9) /\left[2\left(24.167^{2}+14.5^{2}+4.833^{2}\right)\right] \\
& =0.333+0.443 \\
& =0.776
\end{aligned}
$$

Add the multiple presence factor of 1.0 for two lanes loaded:

$$
\begin{aligned}
\mathrm{R} & =1.0(0.776) \\
& =0.776
\end{aligned}
$$

(Strength)

Three lanes loaded:

$$
\begin{aligned}
\mathrm{R} & =3 / 6+24.167(21+9-3) /\left[2\left(24.167^{2}+14.5^{2}+4.833^{2}\right)\right] \\
& =0.5+0.399 \\
& =0.899
\end{aligned}
$$

Add the multiple presence factor of 0.85 for three or more lanes loaded:

$$
\begin{aligned}
\mathrm{R} & =0.85(0.899) \\
& =0.764
\end{aligned}
$$

(Strength)
These values do not control over the distribution factors summarized in Design Step 5.1.16.


Figure 5.1-2 - General Dimensions

Design Step
5.1.16

From (7) and (9), the service and strength limit state moment distribution factor for the exterior girder is equal to the larger of 0.772 and 0.806 lane. Therefore, the moment distribution factor is 0.806 lane.

From (8):
The fatigue limit state moment distribution factor is 0.672 lane
From (10) and (12), the service and strength limit state shear distribution factor for the exterior girder is equal to the larger of 0.762 and 0.845 lane. Therefore, the shear distribution factor is 0.845 lane.

From (11):
The fatigue limit state shear distribution factor is 0.704 lane

Table 5.1-1 - Summary of Service and Strength Limit State Distribution Factors

|  | Load Case | Moment <br> interior <br> beams | Moment <br> exterior <br> beams | Shear <br> interior <br> beams | Shear <br> exterior <br> beams |
| :--- | :--- | :---: | :---: | :---: | :---: |
| Distribution <br> factors from <br> Tables in <br> S4.6.2.2.2 | Multiple <br> lanes <br> loaded | 0.796 | 0.772 | 0.973 | 0.762 |
| Single lane <br> loaded | 0.542 | 0.806 | 0.782 | 0.845 |  |
| Additional <br> check for <br> rigidly <br> loonnected <br> girders | Multiple <br> lanes <br> loaded | NA | 0.776 | NA | 0.776 |
| Single lane <br> loaded | NA | 0.572 | NA | 0.572 |  |
| Design value |  | 0.796 | 0.806 | 0.973 | 0.845 |

Table 5.1-2 - Summary of Fatigue Limit State Distribution Factors

|  | Load Case | Moment <br> interior <br> beams | Moment <br> exterior <br> beams | Shear <br> interior <br> beams | Shear <br> exterior <br> beams |
| :--- | :--- | :---: | :---: | :---: | :---: |
| Distribution <br> factors from | Multiple <br> lanes <br> loaded | NA | NA | NA | NA |
| Singles in <br> S4.6.2.2.2 | Single lane <br> loaded | 0.452 | 0.672 | 0.652 | 0.704 |
| Additional <br> check for <br> rigidly <br> connected <br> girders | Multiple <br> lanes <br> loaded | NA | NA | NA | NA |
| Single lane <br> loaded | NA | 0.477 | NA | 0.477 |  |
| Design value |  | 0.452 | 0.672 | 0.652 | 0.704 |

## Design Step DEAD LOAD CALCULATION

5.2

Calculate the dead load of the bridge superstructure components for the controlling interior girder. Values for the exterior girder have also been included for reference. The girder, slab, haunch, and exterior diaphragm loads are applied to the noncomposite section; the parapets and future wearing surface are applied to the composite section.

## Interior girder

## Girder weight

$$
\mathrm{DC}_{\text {girder (I) }}=\mathrm{A}_{\mathrm{g}}\left(\gamma_{\text {girder }}\right)
$$

where:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{g}} & =\text { beam cross-sectional area }\left(\mathrm{in}^{2}\right) \\
& =1,085 \mathrm{in}^{2} \\
\gamma & =\text { unit weight of beam concrete }(\mathrm{kcf}) \\
& =0.150 \mathrm{kcf} \\
& \\
\mathrm{DC}_{\text {girder }}(\mathrm{I}) & =(1,085 / 144)(0.150) \\
& =1.13 \mathrm{k} / \mathrm{ft} / \text { girder }
\end{aligned}
$$

Deck slab weight
The total thickness of the slab is used in calculating the weight.
Girder spacing $=9.667 \mathrm{ft}$.
Slab thickness $=8$ in.

$$
\begin{aligned}
\mathrm{DC}_{\text {slab (I) }} & =9.667(8 / 12)(0.150) \\
& =0.967 \mathrm{k} / \mathrm{ft} / \text { girder }
\end{aligned}
$$

## Exterior girder

Girder weight
$\mathrm{DC}_{\text {girder }}(\mathrm{E})=1.13 \mathrm{k} / \mathrm{ft} /$ girder

Deck slab weight
Slab width $\quad=$ overhang width $+1 / 2$ girder spacing

$$
=3.521+1 / 2(9.667)
$$

$$
=8.35 \mathrm{ft} .
$$

Slab thickness $=8$ in.

$$
\begin{aligned}
\mathrm{DC}_{\text {slab (E) }} & =8.35(8 / 12)(0.150) \\
& =0.835 \mathrm{k} / \mathrm{ft} / \text { girder }
\end{aligned}
$$

## Haunch weight

$$
\begin{aligned}
\text { Width } & =42 \mathrm{in} . \\
\text { Thickness } & =4 \mathrm{in} . \\
& \\
\text { DC }_{\text {haunch }} & =[42(4) / 144](0.150) \\
& =0.175 \mathrm{k} / \mathrm{ft} / \text { girder }
\end{aligned}
$$

Notice that the haunch weight in this example is assumed as a uniform load along the full length of the beam. This results in a conservative design as the haunch typically have a variable thickness that decreases toward the middle of the span length. Many jurisdictions calculate the haunch load effects assuming the haunch thickness to vary parabolically along the length of the beam. The location of the minimum thickness varies depending on the grade of the roadway surface at bridge location and the presence of a vertical curve. The use of either approach is acceptable and the difference in load effects is typically negligible. However, when analyzing existing bridges, it may be necessary to use the variable haunch thickness in the analysis to accurately represent the existing situation

## Concrete diaphragm weight

A concrete diaphragm is placed at one-half the noncomposite span length.
Location of the diaphragms:
Span $1=54.5 \mathrm{ft}$. from centerline of end bearing
Span $2=55.5 \mathrm{ft}$. from centerline of pier
For this example, arbitrarily assume that the thickness of the diaphragm is 10 in . The diaphragm spans from beam to beam minus the web thickness and has a depth equal to the distance from the top of the beam to the bottom of the web. Therefore, the concentrated load to be applied at the locations above is:

$$
\begin{aligned}
\mathrm{DC}_{\text {diaphragm }} & =0.15(10 / 12)[9.667-(8 / 12)](72-18) / 12 \\
& =5.0625 \mathrm{k} / \text { girder }
\end{aligned}
$$

The exterior girder only resists half of this loading.

## Parapet weight

According to the S4.6.2.2.1, the parapet weight may be distributed equally to all girders in the cross section.

Parapet cross-sectional area $=4.33 \mathrm{ft}^{2}$

$$
\begin{aligned}
\mathrm{DC}_{\text {parapet }} & =4.33(0.150)=0.650 \mathrm{k} / \mathrm{ft} \\
& =0.650 / 6 \text { girders } \\
& =0.108 \mathrm{k} / \mathrm{ft} / \text { girder for one parapet }
\end{aligned}
$$

Therefore, the effect of two parapets yields:

$$
\mathrm{DC}_{\text {parapet }}=0.216 \mathrm{k} / \mathrm{ft} \text { per girder }
$$

Future wearing surface
Interior girder

$$
\begin{aligned}
\text { Weight/ft }^{2} & =0.030 \mathrm{k} / \mathrm{ft}^{2} \\
\text { Width } & =9.667 \mathrm{ft} . \\
& \\
\text { DWF }_{\text {FWS (I) }} & =0.030(9.667) \\
& =0.290 \mathrm{k} / \mathrm{ft} / \text { girder }
\end{aligned}
$$

## Exterior Girder

$$
\begin{aligned}
\text { Weight/ft } & =0.030 \mathrm{k} / \mathrm{ft}^{2} \\
\text { Width } & =\text { slab width }- \text { parapet width } \\
& =8.35-1.6875 \\
& =6.663 \mathrm{ft} . \\
& \\
\text { DW }_{\text {FWS (E) }} & =0.030(6.663) \\
& =0.200 \mathrm{k} / \mathrm{ft} / \text { girder }
\end{aligned}
$$

Notice that some jurisdictions divide the weight of the future wearing surface equally between all girders (i.e. apply a uniform load of $0.26 \mathrm{k} / f t$ to all girders). Article S4.6.2.2.1 states that permanent loads of and on the deck may be distributed uniformly among the beams. This method would also be acceptable and would minimally change the moments and shears given in the tables in Design Step 5.3.

## Design Step

 5.3
## Design Step

 5.3.1UNFACTORED AND FACTORED LOAD EFFECTS

## Summary of loads

The dead load moments and shears were calculated based on the loads shown in Design Step 5.2. The live load moments and shears were calculated using a generic live load analysis computer program. The live load distribution factors from Design Step 5.1 are applied to these values.

Table 5.3-1 - Summary of Unfactored Moments
Interior girder, Span 1 shown, Span 2 mirror image

| Location* | Noncomposite |  |  |  |  | Composite |  | Live Load + IM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girder |  | $\begin{gathered} \text { Slab } \\ \text { and } \\ \text { Haunch } \end{gathered}$ | Exterior Diaphragm | Total Noncomp. | Parapet | FWS | Positive HL-93 | Negative HL-93 |
|  | ** | *** |  |  |  |  |  |  |  |
| (ft.) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) |
| 0 | 47 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1.0 | 108 | 61 | 62 | 3 | 125 | 9 | 12 | 92 | -11 |
| 5.5 | 368 | 322 | 325 | 14 | 661 | 46 | 62 | 476 | -58 |
| 11.0 | 656 | 609 | 615 | 28 | 1,252 | 85 | 114 | 886 | -116 |
| 16.5 | 909 | 863 | 871 | 42 | 1,776 | 118 | 158 | 1,230 | -174 |
| 22.0 | 1,128 | 1,082 | 1,093 | 56 | 2,230 | 144 | 193 | 1,509 | -233 |
| 27.5 | 1,313 | 1,267 | 1,279 | 70 | 2,616 | 164 | 220 | 1,724 | -291 |
| 33.0 | 1,464 | 1,417 | 1,432 | 84 | 2,933 | 177 | 237 | 1,882 | -349 |
| 38.5 | 1,580 | 1,534 | 1,549 | 98 | 3,181 | 183 | 246 | 1,994 | -407 |
| 44.0 | 1,663 | 1,616 | 1,633 | 111 | 3,360 | 183 | 246 | 2,047 | -465 |
| 49.5 | 1,711 | 1,664 | 1,681 | 125 | 3,471 | 177 | 237 | 2,045 | -523 |
| 54.5 | 1,725 | 1,679 | 1,696 | 138 | 3,512 | 165 | 222 | 2,015 | -576 |
| 55.0 | 1,725 | 1,678 | 1,695 | 137 | 3,511 | 164 | 220 | 2,010 | -581 |
| 60.5 | 1,705 | 1,658 | 1,675 | 123 | 3,456 | 144 | 194 | 1,927 | -640 |
| 66.0 | 1,650 | 1,604 | 1,620 | 109 | 3,333 | 118 | 159 | 1,794 | -698 |
| 71.5 | 1,562 | 1,515 | 1,531 | 95 | 3,141 | 86 | 115 | 1,613 | -756 |
| 77.0 | 1,439 | 1,392 | 1,407 | 81 | 2,880 | 46 | 62 | 1,388 | -814 |
| 82.5 | 1,282 | 1,236 | 1,248 | 67 | 2,551 | 1 | 1 | 1,124 | -872 |
| 88.0 | 1,091 | 1,044 | 1,055 | 53 | 2,152 | -52 | -69 | 825 | -1,124 |
| 93.5 | 865 | 819 | 827 | 39 | 1,686 | -110 | -148 | 524 | -1,223 |
| 99.0 | 606 | 560 | 565 | 25 | 1,150 | -176 | -236 | 297 | -1,371 |
| 104.5 | 312 | 266 | 268 | 11 | 546 | -248 | -332 | 113 | -1,663 |
| 108.0 | 110 | 61 | 62 | 3 | 125 | -297 | -398 | 33 | -1,921 |
| 109.0 | 47 | 0 | 0 | 0 | 0 | -311 | -418 | 15 | -2,006 |
| Span 2-0 | - | 0 | 0 | 0 | 0 | -326 | -438 | 0 | -2,095 |

* Distance from the centerline of the end bearing
** Based on the simple span length of 110.5 ft . and supported at the ends of the girders. These values are used to calculate stresses at transfer.
*** Based on the simple span length of 109 ft . and supported at the centerline of bearings. These values are used to calculate the final stresses.

Table 5.3-2 - Summary of Factored Moments
Interior girder, Span 1 shown, Span 2 mirror image

| Location* | Strength I | Service I ** |  | Service III ** |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | NC | Comp. | NC | Comp. |
| (ft.) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 1.0 | 346 | 125 | 112 | 125 | 94 |
| 5.5 | 1,809 | 661 | 584 | 661 | 488 |
| 11.0 | 3,394 | 1,252 | 1,085 | 1,252 | 908 |
| 16.5 | 4,756 | 1,776 | 1,506 | 1,776 | 1,260 |
| 22.0 | 5,897 | 2,230 | 1,846 | 2,230 | 1,544 |
| 27.5 | 6,821 | 2,616 | 2,108 | 2,616 | 1,763 |
| 33.0 | 7,536 | 2,933 | 2,296 | 2,933 | 1,920 |
| 38.5 | 8,063 | 3,181 | 2,423 | 3,181 | 2,024 |
| 44.0 | 8,381 | 3,360 | 2,477 | 3,360 | 2,067 |
| 49.5 | 8,494 | 3,471 | 2,459 | 3,471 | 2,050 |
| 54.5 | 8,456 | 3,512 | 2,402 | 3,512 | 1,999 |
| 55.0 | 8,440 | 3,511 | 2,394 | 3,511 | 1,992 |
| 60.5 | 8,163 | 3,456 | 2,265 | 3,456 | 1,880 |
| 66.0 | 7,690 | 3,333 | 2,070 | 3,333 | 1,712 |
| 71.5 | 7,027 | 3,141 | 1,813 | 3,141 | 1,490 |
| 77.0 | 6,181 | 2,880 | 1,497 | 2,880 | 1,219 |
| 82.5 | 5,158 | 2,551 | 1,126 | 2,551 | 901 |
| 88.0 | 3,967 | 2,152 | -1,245 | 2,152 | -1,020 |
| 93.5 | 2,664 | 1,686 | -1,481 | 1,686 | -1,237 |
| 99.0 | -1,535 | 1,150 | -1,783 | 1,150 | -1,509 |
| 104.5 | -3,035 | 546 | -2,242 | 546 | -1,910 |
| 108.0 | -4,174 | 125 | -2,616 | 125 | -2,232 |
| 109.0 | -4,525 | 0 | -2,734 | 0 | -2,333 |
| Span 2-0 | -4,729 | 0 | -2,858 | 0 | -2,439 |

## Load Factor Combinations

Strength I $=1.25(\mathrm{DC})+1.5(\mathrm{DW})+1.75(\mathrm{LL}+\mathrm{IM})$
Service I $=1.0[\mathrm{DC}+\mathrm{DW}+(\mathrm{LL}+\mathrm{IM})]$
Service $\mathrm{III}=1.0(\mathrm{DC}+\mathrm{DW})+0.8(\mathrm{LL}+\mathrm{IM})$

* Distance from the centerline of the end bearing
** For service limit states, moments are applied to the section of the girder, i.e. noncomposite or composite, that resists these moments. Hence, noncomposite and composite moments have to be separated for service load calculations.

Table 5.3-3 - Summary of Unfactored Shear
Interior girder, Span 1 shown, Span 2 mirror image

| Location* | Noncomposite |  |  |  |  | Composite |  | Live Load + IM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girder | Slab and <br> Haunch | Exterior <br> Diaphragm | Total <br> Noncomp. | Parapet | FWS | Positive <br> HL-93 | Negative <br> HL-93 |  |
| $(\mathrm{ft}$. ) | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ |  |
| 0 | 61.6 | 62.2 | 2.5 | 126.4 | 8.9 | 12.0 | 113.3 | -12.9 |  |
| 1.0 | 60.5 | 61.1 | 2.5 | 124.1 | 8.7 | 11.7 | 111.7 | -12.9 |  |
| 5.5 | 55.4 | 55.9 | 2.5 | 113.9 | 7.7 | 10.4 | 104.3 | -13.0 |  |
| 11.0 | 49.2 | 49.7 | 2.5 | 101.4 | 6.5 | 8.8 | 95.5 | -13.4 |  |
| 16.5 | 43.0 | 43.4 | 2.5 | 88.9 | 5.4 | 7.2 | 86.9 | -15.9 |  |
| 22.0 | 36.7 | 37.1 | 2.5 | 76.4 | 4.2 | 5.6 | 78.7 | -20.6 |  |
| 27.5 | 30.5 | 30.8 | 2.5 | 63.9 | 3.0 | 4.0 | 70.8 | -26.0 |  |
| 33.0 | 24.3 | 24.6 | 2.5 | 51.4 | 1.8 | 2.4 | 63.1 | -32.8 |  |
| 38.5 | 18.1 | 18.3 | 2.5 | 38.9 | 0.6 | 0.8 | 55.9 | -39.8 |  |
| 44.0 | 11.9 | 12.0 | 2.5 | 26.4 | -0.6 | -0.8 | 48.9 | -46.8 |  |
| 49.5 | 5.7 | 5.7 | 2.5 | 13.9 | -1.8 | -2.4 | 42.4 | -54.0 |  |
| 54.5 | 0 | 0 | -2.5 | -2.5 | -2.9 | -3.8 | 36.8 | -60.5 |  |
| 55.0 | -0.6 | -0.6 | -2.5 | -3.7 | -3.0 | -4.0 | 36.2 | -61.2 |  |
| 60.5 | -6.8 | -6.9 | -2.5 | -16.2 | -4.2 | -5.6 | 30.4 | -68.4 |  |
| 66.0 | -13.0 | -13.1 | -2.5 | -28.7 | -5.3 | -7.2 | 25.0 | -75.7 |  |
| 71.5 | -19.2 | -19.4 | -2.5 | -41.2 | -6.5 | -8.8 | 20.0 | -82.9 |  |
| 77.0 | -25.4 | -25.7 | -2.5 | -53.7 | -7.7 | -10.4 | 15.4 | -90.1 |  |
| 82.5 | -31.7 | -32.0 | -2.5 | -66.1 | -8.9 | -12.0 | 11.3 | -97.3 |  |
| 88.0 | -37.9 | -38.3 | -2.5 | -78.6 | -10.1 | -13.6 | 8.2 | -104.3 |  |
| 93.5 | -44.1 | -44.5 | -2.5 | -91.1 | -11.3 | -15.1 | 5.5 | -111.3 |  |
| 99.0 | -50.3 | -50.8 | -2.5 | -103.6 | -12.5 | -16.7 | 3.2 | -118.0 |  |
| 104.5 | -56.5 | -57.1 | -2.5 | -116.1 | -13.7 | -18.3 | 1.2 | -124.7 |  |
| 108.0 | -60.5 | -61.1 | -2.5 | -124.1 | -14.4 | -19.4 | 0.4 | -128.7 |  |
| 109.0 | -61.6 | -62.2 | -2.5 | -126.4 | -14.6 | -19.6 | 0.2 | -129.9 |  |
| Span $2-0$ | 0 | 0 | 0 | 0 | -14.8 | -19.9 | 0 | -131.1 |  |

* Distance from the centerline of the end bearing

Table 5.3-4 - Summary of Factored Shear
Interior girder, Span 1 shown, Span 2 mirror image

| Location* | Strength I | Service I | Service III |
| :---: | :---: | :---: | :---: |
| $(\mathrm{ft}$. ) | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ |
| 0 | 385.4 | 260.6 | 237.9 |
| 1.0 | 379.0 | 256.2 | 233.8 |
| 5.5 | 350.0 | 236.2 | 215.4 |
| 11.0 | 315.1 | 212.1 | 193.0 |
| 16.5 | 280.7 | 188.3 | 170.9 |
| 22.0 | 246.8 | 164.8 | 149.1 |
| 27.5 | 213.4 | 141.6 | 127.5 |
| 33.0 | 180.6 | 118.7 | 106.1 |
| 38.5 | 148.3 | 96.2 | 85.0 |
| 44.0 | 116.7 | 74.0 | 64.2 |
| 49.5 | 85.7 | 52.1 | 43.6 |
| 54.5 | -118.4 | -69.7 | -57.6 |
| 55.0 | -121.3 | -71.8 | -59.6 |
| 60.5 | -153.5 | -94.3 | -80.6 |
| 66.0 | -185.7 | -116.9 | -101.7 |
| 71.5 | -217.9 | -139.4 | -122.8 |
| 77.0 | -250.0 | -161.8 | -143.8 |
| 82.5 | -282.0 | -184.3 | -164.8 |
| 88.0 | -313.8 | -206.6 | -185.7 |
| 93.5 | -345.4 | -228.8 | -206.6 |
| 99.0 | -376.8 | -250.9 | -227.3 |
| 104.5 | -407.9 | -272.8 | -247.8 |
| 108.0 | -427.4 | -286.6 | -260.8 |
| 109.0 | -433.0 | -290.5 | -264.5 |
| Span $2-0$ | -277.8 | -165.8 | -139.6 |
|  |  |  |  |

Load Factor Combinations
Strength $\mathrm{I}=1.25(\mathrm{DC})+1.5(\mathrm{DW})+1.75(\mathrm{LL}+\mathrm{IM})$
Service I $=1.0[\mathrm{DC}+\mathrm{DW}+(\mathrm{LL}+\mathrm{IM})]$
Service III $=1.0(\mathrm{DC}+\mathrm{DW})+0.8(\mathrm{LL}+\mathrm{IM})$

* Distance from the centerline of the end bearing

Table 5.3-5 - Summary of Unfactored Moments
Exterior girder, Span 1 shown, Span 2 mirror image

| Location* | Noncomposite |  |  |  |  | Composite |  | Live Load + IM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girder |  | Slab and Haunch | Exterior Diaphragm | Total Noncomp. | Parapet | FWS | PositiveHL-93 | Negative <br> HL-93 |
|  | ** | *** |  |  |  |  |  |  |  |
| (ft.) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) |
| 0 | 47 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1.0 | 108 | 61 | 55 | 1 | 117 | 9 | 8 | 93 | -11 |
| 5.5 | 368 | 322 | 288 | 7 | 616 | 46 | 41 | 482 | -59 |
| 11.0 | 656 | 609 | 545 | 14 | 1,168 | 85 | 77 | 897 | -118 |
| 16.5 | 909 | 863 | 771 | 21 | 1,655 | 118 | 106 | 1,245 | -177 |
| 22.0 | 1,128 | 1,082 | 967 | 28 | 2,076 | 144 | 130 | 1,528 | -236 |
| 27.5 | 1,313 | 1,267 | 1,132 | 35 | 2,434 | 164 | 148 | 1,746 | -294 |
| 33.0 | 1,464 | 1,417 | 1,267 | 42 | 2,726 | 177 | 160 | 1,906 | -353 |
| 38.5 | 1,580 | 1,534 | 1,371 | 49 | 2,954 | 183 | 165 | 2,019 | -412 |
| 44.0 | 1,663 | 1,616 | 1,445 | 56 | 3,117 | 183 | 166 | 2,073 | -471 |
| 49.5 | 1,711 | 1,664 | 1,488 | 63 | 3,215 | 177 | 160 | 2,071 | -530 |
| 54.5 | 1,725 | 1,679 | 1,501 | 69 | 3,248 | 165 | 149 | 2,041 | -583 |
| 55.0 | 1,725 | 1,678 | 1,501 | 68 | 3,247 | 164 | 148 | 2,035 | -589 |
| 60.5 | 1,705 | 1,658 | 1,482 | 61 | 3,202 | 144 | 130 | 1,951 | -648 |
| 66.0 | 1,650 | 1,604 | 1,434 | 54 | 3,092 | 118 | 107 | 1,816 | -706 |
| 71.5 | 1,562 | 1,515 | 1,355 | 48 | 2,917 | 86 | 77 | 1,633 | -765 |
| 77.0 | 1,439 | 1,392 | 1,245 | 41 | 2,678 | 46 | 42 | 1,406 | -824 |
| 82.5 | 1,282 | 1,236 | 1,105 | 34 | 2,374 | 1 | 1 | 1,139 | -883 |
| 88.0 | 1,091 | 1,044 | 934 | 27 | 2,005 | -52 | -47 | 836 | -1,138 |
| 93.5 | 865 | 819 | 732 | 20 | 1,571 | -110 | -100 | 531 | -1,238 |
| 99.0 | 606 | 560 | 500 | 13 | 1,072 | -176 | -159 | 300 | -1,389 |
| 104.5 | 312 | 266 | 238 | 6 | 509 | -248 | -224 | 114 | -1,683 |
| 108.0 | 110 | 61 | 55 | 1 | 117 | -297 | -268 | 33 | -1,945 |
| 109.0 | 47 | 0 | 0 | 0 | 0 | -311 | -281 | 15 | -2,031 |
| Span 2-0 | - | 0 | 0 | 0 | 0 | -326 | -294 | 0 | -2,121 |

* Distance from the centerline of the end bearing
** Based on the simple span length of 110.5 ft . and supported at the ends of the girders. These values are used to calculate stresses at transfer.
*** Based on the simple span length of 109 ft . and supported at the centerline of bearings. These values are used to calculate the final stresses.

Table 5.3-6 - Summary of Factored Moments
Exterior girder, Span 1 shown, Span 2 mirror image

|  |  | Service I ** |  | Service III ** |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Location* $^{*}$ Strength I | NC | Comp. | NC | Comp. |  |
| $(\mathrm{ft})$. | $(\mathrm{k}-\mathrm{ft})$ | $(\mathrm{k}-\mathrm{ft})$ | $(\mathrm{k}-\mathrm{ft})$ | $(\mathrm{k}-\mathrm{ft})$ | $(\mathrm{k}-\mathrm{ft})$ |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 1.0 | 331 | 117 | 110 | 117 | 91 |
| 5.5 | 1,734 | 616 | 570 | 616 | 473 |
| 11.0 | 3,251 | 1,168 | 1,059 | 1,168 | 879 |
| 16.5 | 4,554 | 1,655 | 1,469 | 1,655 | 1,220 |
| 22.0 | 5,644 | 2,076 | 1,801 | 2,076 | 1,496 |
| 27.5 | 6,524 | 2,434 | 2,057 | 2,434 | 1,708 |
| 33.0 | 7,203 | 2,726 | 2,242 | 2,726 | 1,861 |
| 38.5 | 7,702 | 2,954 | 2,368 | 2,954 | 1,964 |
| 44.0 | 8,001 | 3,117 | 2,422 | 3,117 | 2,007 |
| 49.5 | 8,103 | 3,215 | 2,407 | 3,215 | 1,993 |
| 54.5 | 8,061 | 3,248 | 2,355 | 3,248 | 1,947 |
| 55.0 | 8,047 | 3,247 | 2,347 | 3,247 | 1,940 |
| 60.5 | 7,793 | 3,202 | 2,226 | 3,202 | 1,836 |
| 66.0 | 7,351 | 3,092 | 2,041 | 3,092 | 1,678 |
| 71.5 | 6,727 | 2,917 | 1,796 | 2,917 | 1,469 |
| 77.0 | 5,928 | 2,678 | 1,494 | 2,678 | 1,213 |
| 82.5 | 4,961 | 2,374 | 1,140 | 2,374 | 912 |
| 88.0 | 3,834 | 2,005 | $-1,237$ | 2,005 | $-1,009$ |
| 93.5 | 2,605 | 1,571 | $-1,448$ | 1,571 | $-1,201$ |
| 99.0 | $-1,547$ | 1,072 | $-1,723$ | 1,072 | $-1,445$ |
| 104.5 | $-2,954$ | 509 | $-2,154$ | 509 | $-1,818$ |
| 108.0 | $-4,031$ | 117 | $-2,510$ | 117 | $-2,121$ |
| 109.0 | $-4,364$ | 0 | $-2,623$ | 0 | $-2,217$ |
| Span $2-0$ | $-4,560$ | 0 | $-2,741$ | 0 | $-2,317$ |

Load Factor Combinations
Strength $\mathrm{I}=1.25(\mathrm{DC})+1.5(\mathrm{DW})+1.75(\mathrm{LL}+\mathrm{IM})$
Service I $=1.0[\mathrm{DC}+\mathrm{DW}+(\mathrm{LL}+\mathrm{IM})]$
Service $\mathrm{III}=1.0(\mathrm{DC}+\mathrm{DW})+0.8(\mathrm{LL}+\mathrm{IM})$

* Distance from the centerline of the end bearing
** For service limit states, moments are applied to the section of the girder, i.e. noncomposite or composite, that resists these moments. Hence, noncomposite and composite moments have to be separated for service load calculations.

Table 5.3-7 - Summary of Unfactored Shear
Exterior girder, Span 1 shown, Span 2 mirror image

| Location* | Noncomposite |  |  |  | Composite |  | Live Load + IM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Girder | Slab <br> and <br> Haunch | Exterior <br> Diaphragm | Total <br> Noncomp. | Parapet | FWS | Positive <br> HL-93 | Negative <br> HL-93 |
| (ft.) | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ |
| 0 | 61.6 | 55.1 | 1.3 | 117.9 | 8.9 | 8.1 | 98.4 | -11.2 |
| 1.0 | 60.5 | 54.1 | 1.3 | 115.8 | 8.7 | 7.9 | 97.0 | -11.2 |
| 5.5 | 55.4 | 49.5 | 1.3 | 106.2 | 7.7 | 7.0 | 90.6 | -11.3 |
| 11.0 | 49.2 | 44.0 | 1.3 | 94.4 | 6.5 | 5.9 | 82.9 | -11.6 |
| 16.5 | 43.0 | 38.4 | 1.3 | 82.6 | 5.4 | 4.8 | 75.5 | -13.8 |
| 22.0 | 36.7 | 32.8 | 1.3 | 70.8 | 4.2 | 3.8 | 68.3 | -17.9 |
| 27.5 | 30.5 | 27.3 | 1.3 | 59.1 | 3.0 | 2.7 | 61.4 | -22.6 |
| 33.0 | 24.3 | 21.7 | 1.3 | 47.3 | 1.8 | 1.6 | 54.8 | -28.5 |
| 38.5 | 18.1 | 16.2 | 1.3 | 35.5 | 0.6 | 0.5 | 48.5 | -34.5 |
| 44.0 | 11.9 | 10.6 | 1.3 | 23.7 | -0.6 | -0.5 | 42.5 | -40.7 |
| 49.5 | 5.7 | 5.1 | 1.3 | 12.0 | -1.8 | -1.6 | 36.8 | -46.9 |
| 54.5 | 0 | 0 | -1.3 | -1.3 | -2.9 | -2.6 | 31.9 | -52.6 |
| 55.0 | -0.6 | -0.5 | -1.3 | -2.3 | -3.0 | -2.7 | 31.4 | -53.1 |
| 60.5 | -6.8 | -6.1 | -1.3 | -14.1 | -4.2 | -3.8 | 26.4 | -59.4 |
| 66.0 | -13.0 | -11.6 | -1.3 | -25.9 | -5.3 | -4.8 | 21.7 | -65.7 |
| 71.5 | -19.2 | -17.2 | -1.3 | -37.7 | -6.5 | -5.9 | 17.4 | -72.0 |
| 77.0 | -25.4 | -22.7 | -1.3 | -49.4 | -7.7 | -7.0 | 13.4 | -78.3 |
| 82.5 | -31.7 | -28.3 | -1.3 | -61.2 | -8.9 | -8.0 | 9.8 | -84.5 |
| 88.0 | -37.9 | -33.9 | -1.3 | -73.0 | -10.1 | -9.1 | 7.2 | -90.6 |
| 93.5 | -44.1 | -39.4 | -1.3 | -84.8 | -11.3 | -10.2 | 4.8 | -96.6 |
| 99.0 | -50.3 | -45.0 | -1.3 | -96.5 | -12.5 | -11.3 | 2.8 | -102.5 |
| 104.5 | -56.5 | -50.5 | -1.3 | -108.3 | -13.7 | -12.3 | 1.0 | -108.3 |
| 108.0 | -60.5 | -54.1 | -1.3 | -115.8 | -14.4 | -13.0 | 0.4 | -111.8 |
| 109.0 | -61.6 | -55.1 | -1.3 | -117.9 | -14.6 | -13.2 | 0.2 | -112.8 |
| Span $2-0$ | 0 | 0 | 0 | 0 | -14.8 | -13.4 | 0 | -113.8 |

* Distance from the centerline of the end bearing

Table 5.3-8 - Summary of Factored Shear
Exterior girder, Span 1 shown, Span 2 mirror image

| Location* | Strength I | Service I | Service III |
| :---: | :---: | :---: | :---: |
| $(\mathrm{ft})$. | $(\mathrm{k})$ | $(\mathrm{k})$ | $(\mathrm{k})$ |
| 0 | 342.9 | 233.3 | 213.7 |
| 1.0 | 337.2 | 229.4 | 210.0 |
| 5.5 | 311.3 | 211.4 | 193.3 |
| 11.0 | 280.1 | 189.7 | 173.2 |
| 16.5 | 249.3 | 168.3 | 153.2 |
| 22.0 | 219.0 | 147.1 | 133.4 |
| 27.5 | 189.1 | 126.2 | 113.9 |
| 33.0 | 159.7 | 105.5 | 94.6 |
| 38.5 | 130.9 | 85.2 | 75.5 |
| 44.0 | 102.5 | 65.1 | 56.6 |
| 49.5 | 74.8 | 45.4 | 38.0 |
| 54.5 | -101.0 | -59.3 | -48.7 |
| 55.0 | -103.6 | -61.1 | -50.5 |
| 60.5 | -132.4 | -81.4 | -69.5 |
| 66.0 | -161.3 | -101.8 | -88.6 |
| 71.5 | -190.1 | -122.1 | -107.7 |
| 77.0 | -218.8 | -142.4 | -126.7 |
| 82.5 | -247.5 | -162.6 | -145.7 |
| 88.0 | -276.0 | -182.8 | -164.7 |
| 93.5 | -304.4 | -202.8 | -183.5 |
| 99.0 | -332.5 | -222.8 | -202.2 |
| 104.5 | -360.4 | -242.5 | -220.9 |
| 108.0 | -377.9 | -255.0 | -232.7 |
| 109.0 | -382.9 | -258.6 | -236.0 |
| Span $2-0$ | -237.8 | -142.1 | -119.3 |

Load Factor Combinations
Strength $\mathrm{I}=1.25(\mathrm{DC})+1.5(\mathrm{DW})+1.75(\mathrm{LL}+\mathrm{IM})$
Service $\mathrm{I}=1.0[\mathrm{DC}+\mathrm{DW}+(\mathrm{LL}+\mathrm{IM})]$
Service $\mathrm{III}=1.0(\mathrm{DC}+\mathrm{DW})+0.8(\mathrm{LL}+\mathrm{IM})$

* Distance from the centerline of the end bearing

Based on the analysis results, the interior girder controls the design. The remaining sections covering the superstructure design are based on the interior girder analysis. The exterior girder calculations would be identical.

## Design Step

5.3.2

## Design Step

5.3.2.1

## ANALYSIS OF CREEP AND SHRINKAGE EFFECTS

## Creep effects

The compressive stress in the beams due to prestressing causes the prestressed beams to creep. For simple span pretensioned beams under dead loads, the highest compression in the beams is typically at the bottom, therefore, creep causes the camber to increase, i.e., causes the upward deflection of the beam to increase. This increased upward deflection of the simple span beam is not accompanied by stresses in the beam since there is no rotational restraint of the beam ends. When simple span beams are made continuous through a connection at the intermediate support, the rotation at the ends of the beam due to creep taking place after the connection is established are restrained by the continuity connection. This results in the development of fixed end moments (FEM) that maintain the ends of the beams as flat. As shown schematically in Figure 5.3-1 for a two-span bridge, the initial deformation is due to creep that takes place before the continuity connection is established. If the beams were left as simple spans, the creep deformations would increase; the deflected shape would appear as shown in part " $b$ " of the figure. However, due to the continuity connection, fixed end moments at the ends of the beam will be required to restrain the end rotations after the continuity connection is established as shown in part " $c$ " of the figure. The beam is analyzed under the effects of the fixed end moments to determine the final creep effects.

Similar effects, albeit in the opposite direction, take place under permanent loads. For ease of application, the effect of the dead load creep and the prestressing creep are analyzed separately. Figures 5.3-2 and 5.3-3 show the creep moment for a two-span bridge with straight strands. Notice that the creep due to prestressing and the creep due to dead load result in restrained moments of opposite sign. The creep from prestressing typically has a larger magnitude than the creep from dead loads.

b) Final "Free" Deformation (simple-span)

c) Final Deformation and Associated Restraint Moments for Simple Spans Made Continuous

Figure 5.3-1 - Prestressed Creep Deformations and Restraint Moments


Figure 5.3-2 - Dead Load Creep Moment


## Figure 5.3-3 - Prestressed Creep Moment

## Shrinkage effects

The shrinkage of the pretensioned beams is different from the shrinkage of the deck slab. This is due to the difference in the age, concrete strength, and method of curing of the two concretes. Unlike creep, differential shrinkage induces stresses in all prestressed composite beams, including simple spans. The larger shrinkage of the deck causes the composite beams to sag as shown in Figure 5.3-4. The restraint and final moments are also shown schematically in the figure.


Figure 5.3-4 - Shrinkage Moment

## Calculations of creep and shrinkage effects

The effect of creep and shrinkage may be determined using the method outlined in the publication entitled "Design of Continuous Highway Bridges with Precast, Prestressed Concrete Girders" published by the Portland Cement Association (PCA) in August 1969. This method is based on determining the fixed end moments required to restrain the ends of the simple span beam after the continuity connection is established. The continuous beam is then analyzed under the effect of these fixed end moments. For creep effects, the result of this analysis is the final result for creep effects. For shrinkage, the result of this analysis is added to the constant moment from shrinkage to determine the final shrinkage effects. Based on the PCA method, Table 5.3-9 gives the value of the fixed end moments for the continuous girder exterior and interior spans with straight strands as a function of the length and section properties of each span. The fixed end moments for dead load creep and shrinkage are also applicable to beams with draped strands. The PCA publication has formulas that may be used to determine the prestress creep fixed end moments for beams with draped strands.

Table 5．3－9－Fixed End Actions for Creep and Shrinkage Effects


|  | DL Creep |  |  | P／S Creep |  |  | Shrinkage |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{array}{\|l\|} \hline \text { Left } \\ \text { End } \\ \text { Span } \\ \hline \end{array}$ | Interior Span | $\begin{array}{\|c\|} \hline \text { Right } \\ \text { End } \\ \text { Span } \end{array}$ | Left End Span | Interior Span | $\begin{aligned} & \text { Right } \\ & \text { End } \\ & \text { Span } \end{aligned}$ | Left End Span | Interior Span | $\begin{aligned} & \hline \text { Right } \\ & \text { End } \\ & \text { Span } \\ & \hline \hline \end{aligned}$ |
| Left Moment（1） | 0 | $2 / 3\left(\mathrm{M}_{\mathrm{D}}\right)$ | MD | 0 | 2Eİ／L | 3EI日／L | 0 | $M_{s}$ | 1.5 Ms |
| Right Moment（2） | －MD | －2／3（MD） | 0 | －3EI日／L | －2EI日／L | 0 | $-1.5 \mathrm{M}_{\mathrm{s}}$ | $-\mathrm{Ms}_{s}$ | 0 |
| Left Shear（3） | －MD／L | 0 | Mo／L | $-3 E 1 \theta / L^{2}$ | 0 | $3 \mathrm{El} \theta / L^{2}$ | －3Ms／2L | 0 | $3 M_{s} / 2 \mathrm{~L}$ |
| Right Shear（4） | Mo／L | 0 | －MD／L | $3 E 1 \theta / L^{2}$ | 0 | $-3 E I \theta / L^{2}$ | $3 \mathrm{M}_{s} / 2 \mathrm{~L}$ | 0 | $-3 \mathrm{M}_{\mathrm{s}} / 2 \mathrm{~L}$ |

Notation for Fixed End Actions：
$\mathrm{M}_{\mathrm{D}}=$ maximum non－composite dead load moment
$\mathrm{L}=$ simple span length
$\mathrm{E}_{\mathrm{c}}=$ modulus of elasticity of beam concrete（final）
I＝moment of inertia of composite section
$\theta=$ end rotation due to eccentric P／S force
$M_{s}=$ applied moment due to differential shrinkage between slab and beam

## Design Step

Effect of beam age at the time of the continuity connection application
5．3．2．3
The age of the beam at the time of application of the continuity connection has a great effect on the final creep and shrinkage moments．As the age of the beam increases before pouring the deck and establishing the continuity connection，the amount of creep，and the resulting creep load effects，that takes place after the continuity connection is established gets smaller．The opposite happens to the shrinkage effects as a larger amount of beam shrinkage takes place before establishing the continuity connection leading to larger differential shrinkage between the beam and the deck．

Due to practical considerations, the age of the beam at the time the continuity connection is established can not be determined with high certainty at the time of design. In the past, two approaches were followed by bridge owners to overcome this uncertainty:

1) Ignore the effects of creep and shrinkage in the design of typical bridges. (The jurisdictions following this approach typically have lower stress limits at service limit states to account for the additional loads from creep and shrinkage.)
2) Account for creep and shrinkage using the extreme cases for beam age at the time of establishing the continuity connection. This approach requires determining the effect of creep and shrinkage for two different cases: a deck poured over a relatively "old" beam and a deck poured over a relatively "young" beam. One state that follows this approach is Pennsylvania. The two ages of the girders assumed in the design are 30 and 450 days. In case the beam age is outside these limits, the effect of creep and shrinkage is reanalyzed prior to construction to ensure that there are no detrimental effects on the structure.

For this example, creep and shrinkage effects were ignored. However, for reference purposes, calculations for creep and shrinkage are shown in Appendix C.

# Design Step $\mid$ LOSS OF PRESTRESS 

5.4
(S5.9.5)
Design Step
General
5.4.1

Loss of prestress can be characterized as that due to instantaneous loss and timedependent loss. Losses due to anchorage set, friction and elastic shortening are instantaneous. Losses due to creep, shrinkage and relaxation are time-dependent.

For pretensioned members, prestress loss is due to elastic shortening, shrinkage, creep of concrete and relaxation of steel. For members constructed and prestressed in a single stage, relative to the stress immediately before transfer, the loss may be taken as:

$$
\begin{equation*}
\Delta f_{p T}=\Delta f_{p E S}+\Delta f_{p S R}+\Delta f_{p C R}+\Delta f_{p R 2} \tag{S5.9.5.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\Delta f_{p E S} & =\text { loss due to elastic shortening (ksi) } \\
\Delta f_{p S R} & =\text { loss due to shrinkage (ksi) } \\
\Delta f_{p C R} & =\text { loss due to creep of concrete (ksi) } \\
\Delta f_{p R 2} & =\text { loss due to relaxation of steel after transfer (ksi) }
\end{aligned}
$$

Notice that an additional loss occurs during the time between jacking of the strands and transfer. This component is the loss due to the relaxation of steel at transfer, $\Delta f_{p R I}$.

The stress limit for prestressing strands of pretensioned members given in S5.9.3 is for the stress immediately prior to transfer. To determine the jacking stress, the loss due to relaxation at transfer, $\Delta f_{p R 1}$, needs to be added to the stress limits in S5.9.3. Practices differ from state to state as what strand stress is to be shown on the contract drawings. The Specifications assume that the designer will determine the stress in the strands immediately before transfer. The fabricator is responsible for determining the jacking force by adding the relaxation loss at transfer, jacking losses and seating losses to the Engineer-determined stress immediately prior to transfer. The magnitude of the jacking and seating losses depends on the jacking equipment and anchorage hardware used in the precasting yard. It is recommended that the Engineer conduct preliminary calculations to determine the anticipated jacking stress.

Accurate estimation of the total prestress loss requires recognition that the timedependent losses resulting from creep and relaxation are interdependent. If required, rigorous calculation of the prestress losses should be made in accordance with a method supported by research data. However, for conventional construction, such a refinement is seldom warranted or even possible at the design stage, since many of the factors are either unknown or beyond the designer's control. Thus, three methods of estimating time-dependent losses are provided in the LRFD Specifications: (1) the approximate
lump sum estimate, (2) a refined estimate, and (3) the background necessary to perform a rigorous time-step analysis.

The Lump Sum Method for calculating the time-dependent losses is presented in S5.9.5.3. The values obtained from this method include the loss due to relaxation at transfer, $\Delta f_{p R I}$. To determine the time-dependent loss after transfer for pretensioned members, $\Delta f_{p R I}$ needs to be estimated and deducted from the total time-dependent losses calculated using S5.9.5.3. The refined method of calculating time-dependent losses is presented in S5.9.5.4. The method described above is used in this example.

A procedure for estimating the losses for partially prestressed members, which is analogous to that for fully prestressed members, is outlined in SC5.9.5.1.

## Design Step

5.4.2

## Design Step <br> 5.4.3

Calculate the initial stress in the tendons immediately prior to transfer (S5.9.3).

$$
\begin{aligned}
\mathrm{f}_{\mathrm{pt}}+\Delta \mathrm{f}_{\mathrm{pES}} & =0.75 \mathrm{f}_{\mathrm{pu}} \\
& =0.75(270) \\
& =202.5 \mathrm{ksi}
\end{aligned}
$$

## Determine the instantaneous losses (S5.9.5.2)

## Friction (S5.9.5.2.2)

The only friction loss possible in a pretensioned member is at hold-down devices for draping or harping tendons. The LRFD Specifications specify the consideration of these losses.

For this example, all strands are straight strands and hold-down devices are not used.

## Elastic Shortening, $\Delta_{\text {fpES }}$ (S5.9.5.2.3)

The prestress loss due to elastic shortening in pretensioned members is taken as the concrete stress at the centroid of the prestressing steel at transfer, $f_{c g p}$, multiplied by the ratio of the modulus of elasticities of the prestressing steel and the concrete at transfer. This is presented in Eq. S5.9.5.2.3a-1.

$$
\begin{equation*}
\Delta f_{p E S}=\left(E_{p} / E_{c i}\right) f_{c g p} \tag{S5.9.5.2.3a-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
f_{c g p}= & \begin{array}{l}
\text { sum of concrete stresses at the center of gravity of prestressing } \\
\text { tendons due to the prestressing force at transfer and the self- }
\end{array} \\
& \text { weight of the member at the sections of maximum moment }(k s i)
\end{aligned}
$$

Applying this equation requires estimating the stress in the strands after transfer. Proposed estimates for pretensioned members are given in S5.9.5.2.3a.

Alternatively, the loss due to elastic shortening may be calculated using Eq. C5.9.5.2.3a1:

$$
\begin{equation*}
\Delta f_{p E S}=\frac{A_{p s} f_{p b t}\left(I_{g}+e_{545^{\prime}}^{2} A_{g}\right)-e_{545^{\prime}} \cdot M_{g} A_{g}}{A_{p s}\left(I_{g}+e_{545^{\prime}}^{2} A_{g}\right)+\frac{A_{g} I_{g} E_{c i}}{E_{p}}} \tag{SC5.9.5.2.3a-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
e_{54.5}= & \text { average eccentricity of prestressing steel at midspan (in.) } \\
f_{p b t}= & \text { stress in prestressing steel immediately prior to transfer as } \\
& \text { specified in Table S5.9.3-1;0.75 } f_{p u}(\text { ksi }) \\
M_{g}= & \text { midspan moment due to member self-weight (k-in) }
\end{aligned}
$$

The alternative approach is used for this example.

$$
\begin{aligned}
\Delta \mathrm{f}_{\mathrm{pES}} & =\frac{44(0.153)[0.75(270)]\left[733,320+31.38^{2}(1,085)\right]-31.38(20,142)(1,085)}{44(0.153)\left[733,320+31.38^{2}(1,085)\right]+\frac{1,085(733,320)(4,200)}{28,500}} \\
\Delta \mathrm{f}_{\mathrm{pES}} & =13.7 \mathrm{ksi}
\end{aligned}
$$

Design Step
5.4.4

Calculate the prestressing stress at transfer

$$
\begin{aligned}
\mathrm{f}_{\mathrm{pt}} \quad & =\text { Stress immediately prior to transfer }-\Delta \mathrm{f}_{\mathrm{pES}} \\
& =202.5-13.7 \\
& =188.8 \mathrm{ksi}
\end{aligned}
$$

## Design Step Calculate the prestressing force at transfer

$$
\begin{aligned}
\mathrm{P}_{\mathrm{t}} & =\mathrm{N}_{\mathrm{strands}}\left(\mathrm{~A}_{\mathrm{ps}}\right)\left(\mathrm{f}_{\mathrm{pt}}\right) \\
& =44(0.153)(188.8) \\
& =1,271 \mathrm{kips} \quad \text { (initial loss }=6.77 \%)
\end{aligned}
$$

Time-dependent losses after transfer, refined method (S5.9.5.4)
Refined estimated time-dependent losses are specified in S5.9.5.4. The refined method can provide a better estimate of total losses than the Lump Sum Method of S5.9.5.3.

## Design Step $\mid \underline{\text { Shrinkage Losses (S5.9.5.4.2) }}$

5.4.6.1

The expression for prestress loss due to shrinkage is a function of the average annual ambient relative humidity, $H$, and is given as Equation S5.9.5.4.2-1 for pretensioned members.

$$
\begin{equation*}
\Delta f_{p S R}=(17.0-0.15 H)(k s i) \tag{S5.9.5.4.2-1}
\end{equation*}
$$

where:

$$
H=\text { the average annual ambient relative humidity (\%) }
$$

The average annual ambient relative humidity may be obtained from local weather statistics or taken from the map of Figure S5.4.2.3.3-1 shown below.


Figure S5.4.2.3.3-1 - Annual Average Ambient Relative Humidity in Percent
Calculate the loss due to shrinkage, $\Delta \mathrm{f}_{\mathrm{pSR}}$
For the Atlanta, Georgia area, where the example bridge is assumed, the average relative humidity may be taken as $70 \%$.

$$
\begin{aligned}
\Delta \mathrm{f}_{\mathrm{pSR}} & =17.0-0.15(70) \\
& =6.5 \mathrm{ksi}
\end{aligned}
$$

## Design Step

## Creep losses (S5.9.5.4.3)

The expression for prestress losses due to creep is a function of the concrete stress at the centroid of the prestressing steel at transfer, $f_{\text {cgp }}$, and the change in concrete stress at the
centroid of the prestressing steel due to all permanent loads except those at transfer, $\Delta f_{c d p}$, and is given by the Eq. S5.9.5.4.3-1.

$$
\begin{equation*}
\Delta f_{p C R}=12.0 f_{c g p}-7.0 \Delta f_{c d p} \geq 0 \tag{S5.9.5.4.3-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
f_{c g p}= & \text { concrete stress at the center of gravity of the prestressing steel at } \\
& \text { transfer }(k s i)
\end{aligned}
$$

$\Delta f_{c d p}=$ change in concrete stress at center of gravity of prestressing steel due to permanent loads, except the load acting at the time the prestressing force is applied. Values of $\Delta f_{\text {cdp }}$ should be calculated at the same section or at sections for which $f_{\text {cgp }}$ is calculated (ksi)

The value of $\Delta f_{c d p}$ includes the effect of the weight of the diaphragm, slab and haunch, parapets, future wearing surface, utilities and any other permanent loads, other than the loads existing at transfer at the section under consideration, applied to the bridge.

Calculate the loss due to creep, $\Delta \mathrm{f}_{\mathrm{pCR}}$
Determine the concrete stress at the center of gravity of prestressing steel at transfer, $\mathrm{f}_{\mathrm{cgp}}$.

$$
\begin{aligned}
& \mathrm{f}_{\mathrm{cgp}}=\frac{\frac{\mathrm{A}_{\mathrm{ps}}\left(0.75 \mathrm{f}_{\mathrm{pu}}\right.}{\mathrm{A}_{\mathrm{g}}}\left(1+\frac{\mathrm{e}_{545^{\prime}}^{2} \mathrm{~A}_{\mathrm{g}}}{\mathrm{I}_{\mathrm{g}}}\right)-\frac{\mathrm{M}_{\mathrm{g}} \mathrm{e}_{545^{\prime}}}{\mathrm{I}_{\mathrm{g}}}}{1+\frac{\mathrm{A}_{\mathrm{ps}}}{\mathrm{~A}_{\mathrm{g}}}\left(\frac{\mathrm{E}_{\mathrm{p}}}{\mathrm{E}_{\mathrm{ci}}}\left(1+\frac{\mathrm{e}_{545^{\prime}}^{2} \mathrm{~A}_{\mathrm{g}}}{\mathrm{I}_{\mathrm{g}}}\right)\right.} \\
& \mathrm{f}_{\mathrm{cgp}} \quad=\frac{\frac{44(0.153)(0.75(270))}{1,085}\left(1+\frac{31.38^{2}(1,085)}{733,320}\right)-\frac{20,142(31.38)}{733,320}}{1+\frac{44(0.153)}{1,085}\left(\frac{28,500}{4,200}\right)\left(1+\frac{31.38^{2}(1,085)}{733,320}\right)} \\
& \mathrm{f}_{\mathrm{cgp}} \quad=[1.256(2.457)-0.862] / 1.103 \\
& \\
& =2.016 \mathrm{ksi}
\end{aligned}
$$

Notice that the second term in both the numerator and denominator in the above equation for $f_{c g p}$ makes this calculation based on the transformed section properties. Calculating $f_{\text {cgp }}$ using the gross concrete section properties of the concrete section is also acceptable, but will result in a higher concrete stress and, consequently, higher calculated losses. Deleting the second term from both the numerator and denominator of the above equation gives the stress based on the gross concrete section properties.

The value of $\mathrm{f}_{\mathrm{cgp}}$ may also be determined using two other methods:

1) Use the same equation above and set the stress in the strands equal to the stress after transfer ( 188.8 ksi ) instead of the stress immediately prior to transfer $\left(0.75 \mathrm{f}_{\mathrm{pu}}=202.5 \mathrm{ksi}\right)$ and let the value of the denominator be 1.0.
2) Since the change in the concrete strain during transfer (strain immediately prior to transfer minus strain immediately after transfer) is equal to the change in strain in the prestressing strands during transfer, the change in concrete stress is equal to the change in prestressing sress during transfer divided by the modular ratio between prestressing steel and concrete at transfer. Noticing that the concrete stress immediately prior to transfer is 0.0 and that the change in prestressing stress during transfer is the loss due to elastic shortening $=13.7 \mathrm{ksi}$, $\mathrm{fgp}_{\mathrm{gp}}$ can be calculated as:

$$
\begin{aligned}
\mathrm{f}_{\mathrm{cgp}} & =13.7 /(28,500 / 4,200) \\
& =2.019 \mathrm{ksi} \cong 2.016 \mathrm{ksi} \text { calculated above (difference due to rounding) }
\end{aligned}
$$

Determine $\Delta \mathrm{f}_{\text {cdp }}$ as defined above.

$$
\begin{aligned}
& \Delta \mathrm{f}_{\mathrm{cdp}}=\left[\left(\mathrm{M}_{\text {dia }}+\mathrm{M}_{\text {slab }}\right) \mathrm{e}_{54.5^{\prime}}\right] / \mathrm{I}_{\mathrm{g}}+\left[\left(\mathrm{M}_{\text {parapet }+}+\mathrm{M}_{\mathrm{FWS}}\right)\left(\mathrm{N} . \mathrm{A}_{\text {beambot }}-\mathrm{CGS}_{\mathrm{ps}}\right)\right] / \mathrm{I}_{\mathrm{c}} \\
& \Delta \mathrm{f}_{\mathrm{cdp}}=[(138+1,696)(12) 31.38] / 733,320+[(165+222)(12)(51.54-5.0)] / 1,384,254 \\
& \Delta \mathrm{f}_{\mathrm{cdp}}=1.10 \mathrm{ksi}
\end{aligned}
$$

Solving,

$$
\begin{aligned}
\Delta \mathrm{f}_{\mathrm{pCR}} & =12.0(2.016)-7.0(1.10) \\
& =16.49 \mathrm{ksi}
\end{aligned}
$$

## Design Step

5.4.6.3

## Relaxation (S5.9.5.4.4)

The total relaxation at any time after transfer is composed of two components: relaxation at transfer and relaxation after transfer.

After Transfer (S5.9.5.4.4c):

Article S5.9.5.4.4c provides equations to estimate relaxation after transfer for pretensioned members with stress-relieved or low relaxation strands.

For pretensioning with stress-relieved strands:

$$
\Delta f_{p R 2}=20.0-0.4 \Delta f_{p E S}-0.2\left(\Delta f_{p S R}+\Delta f_{p C R}\right) \quad(k s i) \quad(\text { S5.9.5.4.4c-1 })
$$

where:

$$
\begin{aligned}
& \Delta f_{p E S}=\text { loss due to elastic shortening }(k s i) \\
& \Delta f_{p S R}=\text { loss due to shrinkage (ksi) } \\
& \Delta f_{p C R}=\text { loss due to creep of concrete (ksi) }
\end{aligned}
$$

For prestressing steels with low relaxation properties conforming to AASHTO M 203 (ASTM A 416 or $E 328$ ) use $30 \%$ of $\Delta f_{p R 2}$ given by the above equation.

Relaxation losses increase with increasing temperatures. The expressions given for relaxation are appropriate for normal temperature ranges only.

Losses due to relaxation should be based on approved test data. If test data is not available, the loss may be assumed to be 3.0 ksi.

Calculate the loss due to relaxation after transfer, $\Delta \mathrm{f}_{\mathrm{pR} 2}$

$$
\begin{aligned}
\Delta \mathrm{f}_{\mathrm{pR} 2} & =20.0-0.4(13.7)-0.2(6.5+16.49) \\
& =9.92 \mathrm{ksi}
\end{aligned}
$$

For low relaxation strands, multiply $\Delta \mathrm{f}_{\mathrm{pR} 2}$ by $30 \%$.

$$
\begin{aligned}
\Delta \mathrm{f}_{\mathrm{pR} 2} & =0.3(9.92) \\
& =2.98 \mathrm{ksi}
\end{aligned}
$$

Design Step
5.4.7

## Design Step <br> 5.4.8

Calculate total loss after transfer

$$
\begin{aligned}
\Delta \mathrm{f}_{\mathrm{pT}} & =\Delta \mathrm{f}_{\mathrm{pES}}+\Delta \mathrm{f}_{\mathrm{pSR}}+\Delta \mathrm{f}_{\mathrm{pCR}}+\Delta \mathrm{f}_{\mathrm{pR} 2} \\
& =13.7+6.5+16.49+2.98 \\
& =39.67 \mathrm{ksi}
\end{aligned}
$$

Calculate the final effective prestress responses

$$
\begin{aligned}
\text { Max } \mathrm{f}_{\mathrm{pe}} & =0.80 \mathrm{f}_{\mathrm{py}} \quad \text { (Table S5.9.3-1 - Stress Limits for Presstressing Tendons at } \\
& \text { the Service Limit State after all losses) } \\
& =0.8(243) \\
& =194.4 \mathrm{ksi}
\end{aligned}
$$

Calculate the actual effective prestress stress after all losses

$$
\begin{aligned}
\mathrm{f}_{\mathrm{pe}} & =0.75 \mathrm{f}_{\mathrm{pu}}-\Delta \mathrm{f}_{\mathrm{pT}} \\
& =0.75(270)-39.67 \\
& =162.83 \mathrm{ksi}<194.4 \mathrm{ksi} \text { OK }
\end{aligned}
$$

Calculate the actual effective prestress force after all losses

$$
\begin{aligned}
\mathrm{P}_{\mathrm{e}} & =\mathrm{N}_{\mathrm{strands}}\left(\mathrm{~A}_{\mathrm{ps}}\right)\left(\mathrm{f}_{\mathrm{pe}}\right) \\
& =44(0.153)(162.83) \\
& =1,096 \text { kips }(\text { total loss }=19.59 \%)
\end{aligned}
$$

## Design Step

As indicated earlier, the Fabricator is responsible for calculation of the jacking force. The calculations presented below are for reference purposes.

As shown earlier, the stress in the prestressing strands immediately prior to transfer is 202.5 ksi.

The Jacking Stress, $\mathrm{f}_{\mathrm{pj}}=$ Stress immediately prior to transfer + Relaxation loss at transfer
Relaxation at transfer (S5.9.5.4.4b) - time-dependent loss
Generally, the initial relaxation loss is now determined by the Fabricator. Where the Engineer is required to make an independent estimate of the initial relaxation loss, or chooses to do so as provided in S5.9.5.1, the provisions of this article may be used as a guide. If project-specific information is not available, the value of $f_{p j}$ may be taken as $0.80 f_{p u}$ for the purpose of this calculation. For this example, $f_{p j}$ will be taken as $0.75 f_{p u}$.

Article S5.9.5.4.4b provides equations to estimate relaxation at transfer for pretensioned members, initially stressed in excess of $50 \%$ of the tendon's tensile strength, $f_{p u}$.

For low-relaxation strands:

$$
\begin{equation*}
\Delta f_{p R I}=\frac{\log (24.0 t)}{40.0}\left[\frac{f_{p j}}{f_{p y}}-0.55\right] f_{p j} \tag{S5.9.5.4.4b-2}
\end{equation*}
$$

where:
$t=$ time estimated in days from stressing to transfer (days) assumed to be 1 day for this example
$f_{p j}=$ initial stress in the tendon at the end of stressing (ksi) assumed to be 205.0 ksi for this example
$f_{p y}=$ specified yield strength of prestressing steel (ksi)
$\Delta \mathrm{f}_{\mathrm{pR} 1}=\frac{\log (24.0(1))}{40.0}\left[\frac{205.0}{243}-0.55\right] 205.0$
$\Delta \mathrm{f}_{\mathrm{pR} 1}=2.08 \mathrm{ksi}$

Therefore,
Jacking stress, $\mathrm{f}_{\mathrm{pj}}=202.5+2.08$

$$
=204.58 \mathrm{ksi}
$$

## Design Step

 5.5Design Step 5.5.1

## STRESS IN PRESTRESSING STRANDS

## Stress in prestressing strands at nominal flexural resistance

The stress in prestressing steel at nominal flexural resistance may be determined using stress compatibility analysis. In lieu of such analysis a simplified method is presented in S5.7.3.1.1. This method is applicable to rectangular or flanged sections subjected to flexure about one axis where the Whitney stress block stress distribution specified in S5.7.2.2 is used and for which $f_{\text {pe }}$, the effective prestressing steel stress after losses, is not less than $0.5 f_{p u}$. The average stress in prestressing steel, $f_{p s,}$ may be taken as:

$$
\begin{equation*}
\mathrm{f}_{\mathrm{ps}}=\mathrm{f}_{\mathrm{pu}}\left[1-\mathrm{k}\left(\mathrm{c} / \mathrm{d}_{\mathrm{p}}\right)\right] \tag{S5.7.3.1.1-1}
\end{equation*}
$$

where:

$$
\begin{equation*}
\mathrm{k}=2\left(1.04-\mathrm{f}_{\mathrm{py}} / \mathrm{f}_{\mathrm{pu}}\right) \tag{S5.7.3.1.1-2}
\end{equation*}
$$

The value of " $k$ " may be calculated using the above equation based on the type and properties of prestressing steel used or it may be obtained from Table SC5.7.3.1.1-1.

The distance from the neutral axis to the compression face of the member may be determined as follows:
for T-section behavior (Eq. S5.7.3.1.1-3):

$$
\mathrm{c}=\frac{\mathrm{A}_{\mathrm{ps}} \mathrm{f}_{\mathrm{pu}}+\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}-\mathrm{A}_{\mathrm{s}}^{\prime} \mathrm{f}_{\mathrm{y}}^{\prime}-0.85 \beta_{1} \mathrm{f}_{\mathrm{c}}^{\prime}\left(\mathrm{b}-\mathrm{b}_{\mathrm{w}}\right) \mathrm{h}_{\mathrm{f}}}{0.85 \mathrm{f}_{\mathrm{c}}^{\prime} \beta_{1} \mathrm{~b}_{\mathrm{w}}+k \mathrm{~A}_{\mathrm{ps}} \frac{\mathrm{f}_{\mathrm{pu}}}{\mathrm{~d}_{\mathrm{p}}}}
$$

for rectangular section behavior (Eq. S5.7.3.1.1-4):

$$
\mathrm{c}=\frac{\mathrm{A}_{\mathrm{ps}} \mathrm{f}_{\mathrm{pu}}+\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}-\mathrm{A}_{\mathrm{s}}^{\prime} \mathrm{f}_{\mathrm{y}}^{\prime}}{0.85 \mathrm{f}_{\mathrm{c}}^{\prime} \beta_{1} \mathrm{~b}+\mathrm{kA}_{\mathrm{ps}} \frac{\mathrm{f}_{\mathrm{pu}}}{\mathrm{~d}_{\mathrm{p}}}}
$$

T-sections where the neutral axis lies in the flange, i.e., "c" is less than the slab thickness, are considered rectangular sections.

From Table SC5.7.3.1.1-1:

$$
\mathrm{k}=0.28 \text { for low relaxation strands }
$$

Assuming rectangular section behavior with no compression steel or mild tension reinforcement:

$$
\mathrm{c}=\mathrm{A}_{\mathrm{ps}} \mathrm{f}_{\mathrm{pu}} /\left[0.85 \mathrm{f}_{\mathrm{c}} \beta_{1} \mathrm{~b}+\mathrm{kA} \mathrm{~A}_{\mathrm{ps}}\left(\mathrm{f}_{\mathrm{pu}} / \mathrm{d}_{\mathrm{p}}\right)\right]
$$

## For the midspan section

Total section depth, $\mathrm{h}=$ girder depth + structural slab thickness

$$
\begin{aligned}
& =72+7.5 \\
& =79.5 \mathrm{in} .
\end{aligned}
$$

$\mathrm{d}_{\mathrm{p}}=\mathrm{h}-$ (distance from bottom of beam to location of P/S steel force)
$=79.5-5.0$
$=74.5 \mathrm{in}$.
$\beta_{1}=0.85$ for 4 ksi slab concrete (S5.7.2.2)
b = effective flange width (calculated in Section 2 of this example)
$=111 \mathrm{in}$.
$\mathrm{c}=6.73(270) /[0.85(4)(0.85)(111)+0.28(6.73)(270 / 74.5)]$
$=5.55 \mathrm{in} .<$ structural slab thickness $=7.5 \mathrm{in}$.
The assumption of the section behaving as a rectangular section is correct.
Notice that if " $c$ " from the calculations above was greater than the structural slab thickness (the integral wearing surface is ignored), the calculations for " $c$ " would have to be repeated assuming a $T$-section behavior following the steps below:

1) Assume the neutral axis lies within the precast girder flange thickness and calculate " $c$ ". For this calculation, the girder flange width and area should be converted to their equivalent in slab concrete by multiplying the girder flange width by the modular ratio between the precast girder concrete and the slab concrete. The web width in the equation for " $c$ " will be substituted for using the effective converted girder flange width. If the calculated value of " $c$ " exceeds the sum of the deck thickness and the precast girder flange thickness, proceed to the next step. Otherwise, use the calculated value of " $c$ ".
2) Assume the neutral axis is below the flange of the precast girder and calculate " $c$ ". The term " $0.85 f^{\prime}{ }_{c} \beta_{l}\left(b-b_{w}\right)$ " in the calculations should be broken into two terms, one refers to the contribution of the deck to the composite section flange and the second refers to the contribution of the precast girder flange to the composite girder flange.

$$
\begin{align*}
\mathrm{f}_{\mathrm{ps}} & =\mathrm{f}_{\mathrm{pu}}\left[1-\mathrm{k}\left(\mathrm{c} / \mathrm{d}_{\mathrm{p}}\right)\right]  \tag{S5.7.3.1.1-1}\\
& =270[1-0.28(5.55 / 74.5)] \\
& =264.4 \mathrm{ksi}
\end{align*}
$$

Development Length $=\left.\right|_{d} \geq \kappa\left[f_{p s}-(2 / 3) f_{p e}\right] d_{b}$
From earlier calculations:

$$
\begin{aligned}
& \mathrm{f}_{\mathrm{ps}}=264.4 \mathrm{ksi}(\text { Design Step 5.4.8) } \\
& \mathrm{f}_{\mathrm{pe}}=162.83 \mathrm{ksi} \text { (Design Step 5.5.1) }
\end{aligned}
$$

From S5.11.4.2, $\kappa=1.6$ for fully bonded strands
From S5.11.4.3, $\kappa=2.0$ for partially debonded strands

For fully bonded strands (32 strands):

$$
\left.\right|_{\mathrm{d}} \geq 1.6[264.4-(2 / 3) 162.83](0.5)=124.7 \mathrm{in} .\left(10.39 \mathrm{ft} \text {. or } 10^{\prime}-411 / 16^{\prime \prime}\right)
$$

For partially debonded strands (two groups of 6-strands each):

$$
\left.\right|_{d} \geq 2.0[264.4-(2 / 3) 162.83](0.5)=155.8 \mathrm{in} .\left(12.98 \mathrm{ft} \text {. or } 12^{\prime}-113 / 4^{\prime \prime}\right)
$$

Design Step
5.5.3

Variation in stress in prestressing steel along the length of the girders
According to S5.11.4.1, the prestressing force, $f_{p e}$, may be assumed to vary linearly from 0.0 at the point where bonding commences to a maximum at the transfer length. Between the transfer length and the development length, the strand force may be assumed to increase in a parabolic manner, reaching the tensile strength of the strand at the development length.

To simplify the calculations, many jurisdictions assume that the stress increases linearly between the transfer and the development lengths. This assumption is used in this example.

As shown in Figures 2-5 and 2-6, each beam contains three groups of strands:
Group 1: 32 strands fully bonded, i.e., bonded length starts 9 in . outside the centerline of bearings of the noncomposite beam

Group 2: 6 strands. Bonded length starts 10 ft . from the centerline of bearings of the noncomposite beam, i.e., 10'-9" from the end of the beam

Group 3: 6 strands. Bonded length starts 22 ft . from the centerline of bearings of the noncomposite beam, i.e., 22 '- 9 " from the end of the beam

For each group, the stress in the prestressing strands is assumed to increase linearly from 0.0 at the point where bonding commences to $f_{\mathrm{pe}}$, over the transfer length, i.e., over 30 inches. The stress is also assumed to increase linearly from $\mathrm{f}_{\mathrm{pe}}$ at the end of the transfer length to $\mathrm{f}_{\mathrm{ps}}$ at the end of the development length. Table 5.5-1 shows the strand forces at the service limit state (maximum strand stress $=\mathrm{f}_{\mathrm{pe}}$ ) and at the strength limit state (maximum strand stress $=\AA_{\mathrm{s}}$ ) at different sections along the length of the beams. To facilitate the calculations, the forces are calculated for each of the three groups of strands separately and sections at the points where bonding commences, end of transfer length and end of development length for each group are included in the tabulated values. Figure 5.5-1 is a graphical representation of Table 5.5-1.

Table 5.5-1 - Prestressing Strand Forces

| Dist. from Grdr End | Dist. from CL of Brg | Initial Prestressing Force at Transfer |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Group 1 | Group 2 | Group 3 | Total |
| (ft) | (ft) | (k) | (k) | (k) | (k) |
| 0 * | $-0.75{ }^{*}$ | 0.0 |  |  | 0.0 |
| 0.75 | 0.00 | 277.3 |  |  | 277.3 |
| 2.50 | 1.75 | 924.4 |  |  | 924.4 |
| 7.75 | 7.00 | 924.4 |  |  | 924.4 |
| 10.39 | 9.64 | 924.4 |  |  | 924.4 |
| $10.75{ }^{* *}$ | $10.00^{* *}$ | 924.4 | 0.0 |  | 924.4 |
| 11.75 | 11.00 | 924.4 | 69.3 |  | 993.7 |
| 13.25 | 12.50 | 924.4 | 173.3 |  | 1,097.7 |
| 17.25 | 16.50 | 924.4 | 173.3 |  | 1,097.7 |
| $22.75{ }^{* * *}$ | $22.00^{* * *}$ | 924.4 | 173.3 | 0.0 | 1,097.7 |
| 23.73 | 22.98 | 924.4 | 173.3 | 67.9 | 1,165.6 |
| 25.25 | 24.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 28.25 | 27.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 33.75 | 33.00 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 35.73 | 34.98 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 39.25 | 38.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 44.75 | 44.00 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 50.25 | 49.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 55.25 | 54.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 55.75 | 55.00 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 61.25 | 60.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 66.75 | 66.00 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 72.25 | 71.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 74.77 | 74.02 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 77.75 | 77.00 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 83.25 | 82.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 85.25 | 84.50 | 924.4 | 173.3 | 173.3 | 1,271.0 |
| 86.77 | 86.02 | 924.4 | 173.3 | 67.9 | 1,165.6 |
| $87.75{ }^{+++}$ | $87.00^{+++}$ | 924.4 | 173.3 | 0.0 | 1,097.7 |
| 88.75 | 88.00 | 924.4 | 173.3 |  | 1,097.7 |
| 94.25 | 93.50 | 924.4 | 173.3 |  | 1,097.7 |
| 97.25 | 96.50 | 924.4 | 173.3 |  | 1,097.7 |
| $99.75^{++}$ | $99.00^{++}$ | 924.4 | 0.0 |  | 924.4 |
| 100.11 | 99.36 | 924.4 |  |  | 924.4 |
| 103.25 | 102.50 | 924.4 |  |  | 924.4 |
| 108.00 | 107.25 | 924.4 |  |  | 924.4 |
| 109.75 | 109.00 | 277.3 |  |  | 277.3 |
| $110.5{ }^{+}$ | $109.75^{+}$ | 0.0 |  |  | 0.0 |

*, **, $^{* * *}$ - Point where bonding commences for strand Groups 1, 2, and 3, respectively
,,++++++- Point where bonding ends for strand Groups 1, 2, and 3, respectively

Table 5.5-1 (cont.) - Presstressing Strand Forces

| Dist. from | Dist. from | Prestressing Force After Losses |  |  |  | Force at the Nominal Flexural Resistance |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Grdr End | CL of Brg | Group 1 | Group 2 | Group 3 | Total | Group 1 | Group 2 | Group 3 | Total |
| (ft) | (ft) | (k) | (k) | (k) | (k) | (k) | (k) | (k) | (k) |
| 0 * | $-0.75{ }^{*}$ | 0.0 |  |  | 0.0 | 0.0 |  |  | 0.0 |
| 0.75 | 0.00 | 239.0 |  |  | 239.0 | 239.0 |  |  | 239.0 |
| 2.50 | 1.75 | 797.2 |  |  | 797.2 | 797.2 |  |  | 797.2 |
| 7.75 | 7.00 | 797.2 |  |  | 797.2 | 1,128.1 |  |  | 1,128.1 |
| 10.39 | 9.64 | 797.2 |  |  | 797.2 | 1,294.5 |  |  | 1,294.5 |
| $10.75{ }^{* *}$ | $10.00^{* *}$ | 797.2 | 0.0 |  | 797.2 | 1,294.5 | 0.0 |  | 1,294.5 |
| 11.75 | 11.00 | 797.2 | 59.8 |  | 857.0 | 1,294.5 | 59.8 |  | 1,354.3 |
| 13.25 | 12.50 | 797.2 | 149.5 |  | 946.7 | 1,294.5 | 149.5 |  | 1,444.0 |
| 17.25 | 16.50 | 797.2 | 149.5 |  | 946.7 | 1,294.5 | 185.1 |  | 1,479.6 |
| $22.75{ }^{* * *}$ | $22.00^{* * *}$ | 797.2 | 149.5 | 0.0 | 946.7 | 1,294.5 | 234.0 | 0.0 | 1,528.5 |
| 23.73 | 22.98 | 797.2 | 149.5 | 58.6 | 1,005.3 | 1,294.5 | 242.7 | 58.6 | 1,595.8 |
| 25.25 | 24.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 149.5 | 1,686.7 |
| 28.25 | 27.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 176.2 | 1,713.4 |
| 33.75 | 33.00 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 225.1 | 1,762.3 |
| 35.73 | 34.98 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 39.25 | 38.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 44.75 | 44.00 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 50.25 | 49.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 55.25 | 54.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 55.75 | 55.00 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 61.25 | 60.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 66.75 | 66.00 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 72.25 | 71.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 74.77 | 74.02 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 242.7 | 1,779.9 |
| 77.75 | 77.00 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 216.2 | 1,753.4 |
| 83.25 | 82.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 167.3 | 1,704.5 |
| 85.25 | 84.50 | 797.2 | 149.5 | 149.5 | 1,096.2 | 1,294.5 | 242.7 | 149.5 | 1,686.7 |
| 86.77 | 86.02 | 797.2 | 149.5 | 58.6 | 1,005.3 | 1,294.5 | 242.7 | 58.6 | 1,595.8 |
| $87.75{ }^{+++}$ | $87.00^{+++}$ | 797.2 | 149.5 | 0.0 | 946.7 | 1,294.5 | 234.0 | 0.0 | 1,528.5 |
| 88.75 | 88.00 | 797.2 | 149.5 |  | 946.7 | 1,294.5 | 225.1 |  | 1,519.6 |
| 94.25 | 93.50 | 797.2 | 149.5 |  | 946.7 | 1,294.5 | 176.2 |  | 1,470.7 |
| 97.25 | 96.50 | 797.2 | 149.5 |  | 946.7 | 1,294.5 | 149.5 |  | 1,444.0 |
| $99.75{ }^{++}$ | $99.00^{++}$ | 797.2 | 0.0 |  | 797.2 | 1,294.5 | 0.0 |  | 1,294.5 |
| 100.11 | 99.36 | 797.2 |  |  | 797.2 | 1,294.5 |  |  | 1,294.5 |
| 103.25 | 102.50 | 797.2 |  |  | 797.2 | 1,096.6 |  |  | 1,096.6 |
| 108.00 | 107.25 | 797.2 |  |  | 797.2 | 797.2 |  |  | 797.2 |
| 109.75 | 109.00 | 239.0 |  |  | 239.0 | 239.0 |  |  | 239.0 |
| $110.5^{+}$ | $109.75{ }^{+}$ | 0.0 |  |  | 0.0 | 0.0 |  |  | 0.0 |

*, **, *** - Point where bonding commences for strand Groups 1, 2, and 3, respectively
,,++++++- Point where bonding ends for strand Groups 1, 2, and 3, respectively


At Transfer

Figure 5.5-1 - Prestressing Strand Forces Shown Graphically


Transfer length $=30 \mathrm{in}$.
Development length, fully bonded $=124.7$ in.
Development length, debonded $=155.8$ in.
Figure 5.5-1 (cont.) - Prestressing Strand Forces Shown Graphically

## Design Step $\mid$ Sample strand stress calculations <br> 5.5.4 <br> Prestress force at centerline of end bearing after losses under Service or Strength <br> Only Group 1 strands are bonded at this section. Ignore Group 2 and 3 strands. <br> Distance from the point bonding commences for Group 1 strands $=0.75 \mathrm{ft}<$ transfer length <br> Percent of prestressing force developed in Group 1 strands $=0.75 /$ transfer length <br> $$
=(0.75 / 2.5)(100)=30 \%
$$

Stress in strands $=0.3(162.83)=48.8 \mathrm{ksi}$

Force in strands at the section $=32(0.153)(48.8)=239 \mathrm{kips}$
Prestress force at a section 11 ft . from the centerline of end bearing after losses under Service conditions

Only strands in Group 1 and 2 are bonded at this section. Ignore Group 3 strands.
The bonded length of Group 1 strands before this section is greater than the transfer length. Therefore, the full prestressing force exists in Group 1 strands.

Force in Group 1 strands $=32(0.153)(162.83)=797.2 \mathrm{kips}$
Distance from the point bonding commences for Group 2 strands $=1.0 \mathrm{ft} .<\operatorname{transfer}$ length

Percent of prestressing force developed in Group 2 strands $=1.0 /$ transfer length

$$
=(1.0 / 2.5)(100)=40 \%
$$

Stress in Group 2 strands $=0.4(162.83)=65.1 \mathrm{ksi}$
Force in Group 2 strands at the section $=6(0.153)(65.1)=59.8 \mathrm{kips}$
Total prestressing force at this section $=$ force in Group $1+$ force in Group 2

$$
=797.2+59.8=857 \mathrm{kips}
$$

Strands maximum resistance at nominal flexural capacity at a section 7.0 ft . from the centerline of end bearing

Only Group 1 strands are bonded at this section. Ignore Group 2 and 3 strands.
Distance from the point bonding commences for Group 1 strands, i.e., distance from end of beam $=7.75 \mathrm{ft}$. (7'-9")

This distance is greater than the transfer length ( 2.5 ft .) but less than the development length of the fully bonded strands ( 10.39 ft .). Therefore, the stress in the strand is assumed to reach $\mathrm{f}_{\mathrm{pe}}, 162.83 \mathrm{ksi}$, at the transfer length then increases linearly from $\mathrm{f}_{\mathrm{pe}}$ to $\mathrm{f}_{\mathrm{ps}}, 264.4$ ksi, between the transfer length and the development length.

Stress in Group 1 strands $=162.83+(264.4-162.83)[(7.75-2.5) /(10.39-2.5)]$

$$
=230.41 \mathrm{ksi}
$$

Force in Group 1 strands $=32(0.153)(230.41)$

$$
=1,128.1 \mathrm{kips}
$$

Strands maximum resistance at nominal flexural capacity at a section 22 ft . from centerline of end bearing

Only strands in Group 1 and 2 are bonded at this section. Ignore Group 3 strands.
The bonded length of Group 1 strands before this section is greater than the development length for Group 1 (fully bonded) strands. Therefore, the full force exists in Group 1 strands.

Force in Group 1 strands $=32(0.153)(264.4)=1,294.5 \mathrm{kips}$
The bonded length of Group 2 at this section $=22-10=12 \mathrm{ft}$.
Stress in Group 2 strands $=162.83+(264.4-162.83)[(12-2.5) /(12.98-2.5)]$

$$
=254.9 \mathrm{ksi}
$$

Force in Group 2 strands $=6(0.153)(254.9)=234.0$ kips
Total prestressing force at this section $=$ force in Group $1+$ force in Group 2

$$
\begin{aligned}
& =1,294.5+234.0 \\
& =1,528.5 \mathrm{kips}
\end{aligned}
$$

## Design Step <br> 5.6 <br> Design Step 5.6.1 <br> Design Step <br> 5.6.1.1

## FLEXURE DESIGN

Flexural stress at transfer
Stress limits at transfer
Compression stress:
The allowable compression stress limit for pretensioned concrete components is calculated according to S5.9.4.1.1.

$$
\begin{aligned}
\mathrm{f}_{\text {Compression }} & =-0.60\left(\mathrm{f}_{\mathrm{ci}}\right) \\
& =-0.60(4.8 \mathrm{ksi}) \\
& =-2.88 \mathrm{ksi}
\end{aligned}
$$

Tension stress:
From Table S5.9.4.1.2-1, the stress limit in areas with bonded reinforcement sufficient to resist $120 \%$ of the tension force in the cracked concrete computed on the basis of an uncracked section is calculated as:

$$
\begin{aligned}
\mathrm{f}_{\text {Tension }} & =0.22 \sqrt{\mathrm{f}_{\mathrm{ci}}^{\prime}} \\
& =0.22 \sqrt{4.8} \\
& =0.48 \mathrm{ksi}
\end{aligned}
$$

## Design Step $\mid$ Stress calculations at transfer

5.6.1.2

Table 5.6-1 - Stresses at Top and Bottom of Beam at Transfer

| Location | Girder <br> self weight moment | $\begin{gathered} \mathrm{F}_{\mathrm{ps}} \text { at } \\ \text { transfer } \end{gathered}$ | Stress at transfer |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Top of beam | Bottom of beam |
| (ft.) ${ }^{(1)}$ | $(\mathrm{k}-\mathrm{ft})^{(2)}$ | (kips) ${ }^{(3)}$ | (ksi) | (ksi) |
| 0 | 47 | 277.3 | 0.135 | -0.654 |
| 1.75 | 153 | 924.4 | 0.451 | -2.183 |
| 5.5 | 368 | 924.4 | 0.326 | -2.055 |
| 11.0 | 656 | 993.7 | 0.209 | -2.065 |
| 16.5 | 909 | 1,097.7 | 0.123 | -2.171 |
| 22.0 | 1,128 | 1,097.7 | -0.005 | -2.040 |
| 27.5 | 1,313 | 1,271.0 | -0.009 | -2.358 |
| 33.0 | 1,464 | 1,271.0 | -0.097 | -2.269 |
| 38.5 | 1,580 | 1,271.0 | -0.155 | -2.209 |
| 44.0 | 1,663 | 1,271.0 | -0.203 | -2.160 |
| 49.5 | 1,711 | 1,271.0 | -0.231 | -2.132 |
| 54.5 | 1,725 | 1,271.0 | -0.240 | -2.120 |
| 55.0 | 1,725 | 1,271.0 | -0.240 | -2.123 |
| 60.5 | 1,705 | 1,271.0 | -0.228 | -2.135 |
| 66.0 | 1,650 | 1,271.0 | -0.196 | -2.168 |
| 71.5 | 1,562 | 1,271.0 | -0.144 | -2.220 |
| 77.0 | 1,439 | 1,271.0 | -0.083 | -2.284 |
| 82.5 | 1,282 | 1,271.0 | 0.009 | -2.377 |
| 88.0 | 1,091 | 1,097.7 | 0.017 | -2.063 |
| 93.5 | 865 | 1,097.7 | 0.149 | -2.197 |
| 99.0 | 606 | 924.4 | 0.197 | -1.923 |
| 104.5 | 312 | 924.4 | 0.358 | -2.105 |
| 107.25 | 153 | 924.4 | 0.451 | -2.200 |
| 109.0 | 47 | 277.3 | 0.135 | -0.660 |

## Notes:

1 - Distance measured from the centerline of the bearing of the simple span girder
2 - See Section 5.3, based on 110.5 ft . length
3 - See Section 5.5 for prestressing forces

## Sample Calculations for Flexural Stresses at Transfer

Definitions:
$\mathrm{P}_{\mathrm{t}} \quad=$ Initial prestressing force taken from Table 5.5-1 (kips)
$\mathrm{A}_{\mathrm{g}}=$ Gross area of the basic beam (in ${ }^{2}$ )
e = Distance between the neutral axis of the noncomposite girder and the center of gravity of the prestressing steel (in.)

$$
\begin{aligned}
& S_{t}=\text { Section moduli, top of noncomposite beam }\left(\mathrm{in}^{3}\right) \\
& \mathrm{S}_{\mathrm{b}}=\text { Section moduli, bottom of noncomposite beam }\left(\mathrm{in}^{3}\right) \\
& \mathrm{M}_{\mathrm{g}}=\text { Moment due to the girder self weight only }(\mathrm{k}-\mathrm{ft})
\end{aligned}
$$

See Section 2.2 for section properties.
Sample Calculations at $1 \mathrm{ft} .-9 \mathrm{in}$. From CL of Bearing ( $2 \mathrm{ft} .-6 \mathrm{in}$. From Girder End)
Girder top stress:

$$
\begin{aligned}
\mathrm{f}_{\mathrm{top}} \quad & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{0} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{g}} / \mathrm{S}_{\mathrm{t}} \\
& =\frac{-924.4}{1,085}+\frac{924.4(31.005)}{20,588}-\frac{153(12)}{20,588} \\
& =0.451 \mathrm{ksi}<\text { Stress limit for tension }(0.48 \mathrm{ksi}) \mathbf{O K}
\end{aligned}
$$

Girder bottom stress:

$$
\begin{aligned}
\mathrm{f}_{\text {bottom }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{0} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{g}} / \mathrm{S}_{\mathrm{b}} \\
& =\frac{-924.4}{1,085}-\frac{924.4(31.005)}{20,157}+\frac{153(12)}{20,157} \\
& =-2.183 \mathrm{ksi}<\text { Stress limit for compression }(-2.88 \mathrm{ksi}) \mathbf{O K}
\end{aligned}
$$

$\underline{\text { Sample Calculations at } 11 \mathrm{ft} \text {. From the CL of Bearing ( } 11 \mathrm{ft} .-9 \mathrm{in} \text {. From Girder End) }}$
Girder top stress:

$$
\begin{aligned}
\mathrm{f}_{\mathrm{top}} \quad & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} \cdot / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{g}} / \mathrm{S}_{\mathrm{t}} \\
& =\frac{-993.7}{1,085}+\frac{993.7(31.222)}{20,588}-\frac{656(12)}{20,588} \\
& =0.209 \mathrm{ksi}<\text { Stress limit for tension }(0.48 \mathrm{ksi}) \text { OK }
\end{aligned}
$$

Girder bottom stress:

$$
\begin{aligned}
\mathrm{f}_{\text {bottom }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} \cdot / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{g}} / \mathrm{S}_{\mathrm{b}} \\
& =\frac{-993.7}{1,085}-\frac{993.7(31.222)}{20,157}+\frac{656(12)}{20,157} \\
& =-2.064 \mathrm{ksi}<\text { Stress limit for compression }(-2.88 \mathrm{ksi}) \quad \text { OK }
\end{aligned}
$$

## Sample Calculations at 54 ft . -6 in . From the CL of Bearing ( $55 \mathrm{ft} .-3 \mathrm{in}$. From Girder End) - Midspan of Noncomposite Beam

Girder top stress:

$$
\begin{aligned}
\mathrm{f}_{\text {top }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{g}} / \mathrm{S}_{\mathrm{t}} \\
& =\frac{-1,271.0}{1,085}+\frac{1,271.0(31.38)}{20,588}-\frac{1,725(12)}{20,588} \\
& =-0.239 \mathrm{ksi}<\text { Stress limit for compression }(-2.88 \mathrm{ksi}) \mathbf{O K}
\end{aligned}
$$

Girder bottom stress:

$$
\begin{aligned}
\mathrm{f}_{\text {bottom }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{g}} / \mathrm{S}_{\mathrm{b}} \\
& =\frac{-1,271.0}{1,085}-\frac{1,271.0(31.38)}{20,157}+\frac{1,725(12)}{20,157} \\
& =-2.123 \mathrm{ksi}<\text { Stress limit for compression }(-2.88 \mathrm{ksi}) \quad \mathbf{O K}
\end{aligned}
$$

## Design Step

Maximum compression is checked under Service I limit state and maximum tension is checked under Service III limit state. The difference between Service I and Service III limit states is that Service I has a load factor of 1.0 for live load while Service III has a load factor of 0.8 .

As indicated in Section 5.3, many jurisdictions do not include creep and shrinkage effects in designing a pretensioned girder bridge. The calculations presented herein do not include creep and shrinkage moments. If creep and shrinkage are required by a specific jurisdiction, then their effects should be included. See Section 5.3 and Appendix $C$ for calculations and values of creep and shrinkage effects for the example bridge.

## Design Step

5.6.2.1

Final flexural stress under Service I limit state

Stress limits

Compression stress:
From Table S5.9.4.2.1-1, the stress limit due to the sum of the effective prestress, permanent loads, and transient loads and during shipping and handling is taken as $0.6 \varphi_{w} f_{c}$ (where $\varphi_{w}$ is equal to 1.0 for solid sections).

For prestressed concrete beams $\left(f_{c}=6.0 \mathrm{ksi}\right)$

$$
\begin{aligned}
\mathrm{f}_{\text {Comp, beam1 }} & =-0.6(6.0 \mathrm{ksi}) \\
& =-3.6 \mathrm{ksi}
\end{aligned}
$$

For deck slab ( $\left.f_{c}=4.0 \mathrm{ksi}\right)$

$$
\begin{aligned}
\mathrm{f}_{\text {Comp, slab }} & =-0.6(4.0 \mathrm{ksi}) \\
& =-2.4 \mathrm{ksi}
\end{aligned}
$$

From Table S5.9.4.2.1-1, the stress limit in prestressed concrete at the service limit state after losses for fully prestressed components in bridges other than segmentally constructed due to the sum of effective prestress and permanent loads shall be taken as:

$$
\begin{aligned}
\mathrm{f}_{\text {Comp, beam } 2} & =-0.45\left(\mathrm{f}_{\mathrm{c}}\right) \\
& =-0.45(6.0) \\
& =-2.7 \mathrm{ksi}
\end{aligned}
$$

From Table S5.9.4.2.1-1, the stress limit in prestressed concrete at the service limit state after losses for fully prestressed components in bridges other than segmentally constructed due to live load plus one-half the sum of the effective prestress and permanent loads shall be taken as:

$$
\begin{aligned}
\mathrm{f}_{\text {Comp, beam } 3} & =-0.40\left(f_{c}^{\prime}\right) \\
& =-0.40(6.0) \\
& =-2.4 \mathrm{ksi}
\end{aligned}
$$

Tension stress:
From Table S5.9.4.2.2-1, the stress limit in prestressed concrete at the service limit state after losses for fully prestressed components in bridges other than segmentally constructed, which include bonded prestressing tendons and are subjected to not worse than moderate corrosion conditions shall be taken as the following:

$$
\begin{aligned}
\mathrm{f}_{\text {Tensile }} & =0.19 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \\
& =0.19 \sqrt{6} \\
& =0.465 \mathrm{ksi}
\end{aligned}
$$

Table 5.6-2 - Stresses in the Prestressed Beam

| Location | Girder noncomposite moment | $\begin{gathered} \mathrm{F}_{\mathrm{ps}} \\ \text { after } \\ \text { losse } \end{gathered}$ | Composite dead load moment | Live load positive moment |
| :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{ft} .)^{(1)}$ | $(\mathrm{k}-\mathrm{ft})^{(2)}$ | (kips) ${ }^{(3)}$ | $(\mathrm{k}-\mathrm{ft})^{(2)}$ | $(\mathrm{k}-\mathrm{ft})^{(2)}$ |
| 0 | 0 | 239.0 | 0 | 0 |
| 1.75 | 217 | 797.2 | 36 | 170 |
| 5.5 | 661 | 797.0 | 108 | 476 |
| 11.0 | 1,252 | 857.0 | 199 | 886 |
| 16.5 | 1,776 | 946.7 | 276 | 1,230 |
| 22.0 | 2,230 | 946.7 | 337 | 1,509 |
| 27.5 | 2,616 | 1,092.1 | 384 | 1,724 |
| 33.0 | 2,933 | 1,092.1 | 414 | 1,882 |
| 38.5 | 3,181 | 1,096.2 | 429 | 1,994 |
| 44.0 | 3,360 | 1,096.2 | 429 | 2,047 |
| 49.5 | 3,471 | 1,096.2 | 414 | 2,045 |
| 54.5 | 3,512 | 1,096.2 | 387 | 2,015 |
| 55.0 | 3,511 | 1,096.2 | 384 | 2,010 |
| 60.5 | 3,456 | 1,096.2 | 338 | 1,927 |
| 66.0 | 3,333 | 1,096.2 | 277 | 1,794 |
| 71.5 | 3,141 | 1,096.2 | 201 | 1,613 |
| 77.0 | 2,880 | 1,096.2 | 108 | 1,388 |
| 82.5 | 2,551 | 1,096.2 | 2 | 1,124 |
| 88.0 | 2,152 | 946.7 | -121 | 825 |
| 93.5 | 1,686 | 946.7 | -258 | 524 |
| 99.0 | 1,150 | 797.2 | -452 | 297 |
| 104.5 | 546 | 797.2 | -580 | 113 |
| 107.25 | 217 | 797.2 | -670 | 58 |
| 109.0 | 0 | 239.0 | -729 | 15 |

Table 5.6-2 - Stresses in the Prestressed Beam (cont.)

| Location | Final stress under PS \& DL |  | Stress under$\begin{gathered} 1 / 2(\mathrm{DL}+\mathrm{P} / \mathrm{S}) \\ + \text { live load } \end{gathered}$ | Final stress under all loads |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Top of beam | Bottom of beam |  | Top of beam | Bottom of beam | Top of slab |
| (ft.) ${ }^{(1)}$ | $(\mathrm{ksi})^{(4)}$ | (ksi) ${ }^{(4)}$ | (ksi) ${ }^{(4)}$ | (ksi) ${ }^{(4)}$ | (ksi) ${ }^{(5)}$ | $(\mathrm{ksi})^{(4)}$ |
| 0 | 0.140 | -0.588 | 0.070 | 0.140 | -0.588 | 0.000 |
| 1.75 | 0.333 | -1.816 | 0.136 | 0.303 | -1.755 | -0.041 |
| 5.5 | 0.061 | -1.519 | -0.054 | -0.023 | -1.349 | -0.116 |
| 11.0 | -0.255 | -1.283 | -0.285 | -0.412 | -0.966 | -0.215 |
| 16.5 | -0.521 | -1.158 | -0.479 | -0.739 | -0.719 | -0.298 |
| 22.0 | -0.796 | -0.861 | -0.666 | -1.064 | -0.321 | -0.365 |
| 27.5 | -0.943 | -0.969 | -0.777 | -1.249 | -0.353 | -0.417 |
| 33.0 | -1.133 | -0.767 | -0.900 | -1.467 | -0.094 | -0.454 |
| 38.5 | -1.270 | -0.631 | -0.988 | -1.623 | 0.081 | -0.479 |
| 44.0 | -1.374 | -0.525 | -1.050 | -1.737 | 0.207 | -0.490 |
| 49.5 | -1.436 | -0.465 | -1.081 | -1.799 | 0.266 | -0.487 |
| 54.5 | -1.455 | -0.453 | -1.085 | -1.812 | 0.267 | -0.475 |
| 55.0 | -1.454 | -0.455 | -1.083 | -1.810 | 0.263 | -0.474 |
| 60.5 | -1.414 | -0.508 | -1.049 | -1.756 | 0.180 | -0.448 |
| 66.0 | -1.331 | -0.609 | -0.984 | -1.649 | 0.032 | -0.410 |
| 71.5 | -1.206 | -0.757 | -0.889 | -1.492 | -0.181 | -0.359 |
| 77.0 | -1.046 | -0.945 | -0.769 | -1.292 | -0.449 | -0.296 |
| 82.5 | -0.835 | -1.189 | -0.617 | -1.034 | -0.787 | -0.223 |
| 88.0 | -0.670 | -1.112 | -0.481 | -0.816 | -0.817 | -0.139 |
| 93.5 | -0.374 | -1.450 | -0.280 | -0.467 | -1.263 | -0.053 |
| 99.0 | -0.116 | -1.487 | -0.111 | -0.169 | -1.381 | 0.031 |
| 104.5 | 0.250 | -1.910 | 0.105 | 0.230 | -1.870 | 0.092 |
| 107.25 | 0.458 | -2.146 | 0.219 | 0.448 | -2.125 | 0.121 |
| 109.0 | 0.269 | -0.918 | 0.132 | 0.266 | -0.913 | 0.141 |

Notes:
1 - Distance measured from the centerline of the bearing of the end abutment
2 - See Section 5.3 for load effects
3 - See Section 5.5 for prestressing forces
4 - Service I limit state for compression
5 - Service III limit state for tension

Definitions:
$\mathrm{P}_{\mathrm{t}} \quad=$ Final prestressing force taken from Design Step 5.4 (kips)
$\mathrm{S}_{\mathrm{tc}} \quad=$ Section moduli, top of the beam of the composite section - gross section (in ${ }^{3}$ )
$\mathrm{S}_{\mathrm{bc}} \quad=$ Section moduli, bottom of the beam of the composite section - gross section (in ${ }^{3}$ )
$S_{\mathrm{tsc}}=$ Section moduli, top of slab of the composite beam (in ${ }^{3}$ )

$$
\begin{aligned}
\mathrm{M}_{\mathrm{DNC}}= & \text { Moment due to the girder, slab, haunch and interior diaphragm }(\mathrm{k}-\mathrm{ft}) \\
\mathrm{M}_{\mathrm{DC}}= & \text { Total composite dead load moment, includes parapets and future } \\
& \quad \text { wearing surface }(\mathrm{k}-\mathrm{ft}) \\
\mathrm{M}_{\mathrm{LLC}}= & \text { Live load moment }(\mathrm{k}-\mathrm{ft})
\end{aligned}
$$

All tension stresses and allowables use positive sign convention. All compression stresses and allowables use negative sign convention. All loads are factored according to Table 3.4.1-1 in the AASHTO LRFD Specifications for Service I and Service III limit states as applicable.

## Design Step

Sample Calculations at 11 ft . From the CL of Bearing ( $11 \mathrm{ft} .-9 \mathrm{in}$. From Girder End)
5.6.2.2

Girder top stress after losses under sum of all loads (Service I):

$$
\begin{aligned}
& \mathrm{f}_{\text {top }}=-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tc}}-\mathrm{M}_{\mathrm{LLC}} / \mathrm{S}_{\mathrm{tc}} \\
&=\frac{-857}{1,085}+\frac{857(31.222)}{20,588}-\frac{1,252(12)}{20,588}-\frac{199(12)}{67,672}-\frac{886(12)}{67,672} \\
&=-0.790+1.300-0.730-0.035-0.157 \\
&=-0.412 \mathrm{ksi}<\quad \begin{array}{l}
\text { Stress limit for compression under full } \\
\quad \\
\\
\end{array} \quad \begin{array}{l}
\text { load }(-3.6 \text { ksi }) \\
\mathbf{O K}
\end{array}
\end{aligned}
$$

Girder top stress under prestressing and dead load after losses:

$$
\begin{aligned}
& \mathrm{f}_{\text {top }}=-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} \cdot / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DN}} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tc}} \\
&=\frac{-857}{1,085}+\frac{857(31.222)}{20,588}-\frac{1,252(12)}{20,588}-\frac{199(12)}{67,672} \\
&=-0.790+1.300-0.730-0.035 \\
&=-0.255 \mathrm{ksi}<\quad \begin{array}{l}
\text { Stress limit for compression under permanent } \\
\\
\\
\end{array} \\
& \text { load }(-2.7 \mathrm{ksi}) \mathbf{O K}
\end{aligned}
$$

Girder top stress under LL $+1 / 2(\mathrm{PS}+\mathrm{DL})$ after losses:

$$
\begin{aligned}
\mathrm{f}_{\mathrm{top}} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} \cdot / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tc}}-\mathrm{M}_{\mathrm{LL}} / \mathrm{S}_{\mathrm{tc}} \\
& =\frac{-857}{1,085(2)}+\frac{857(31.222)}{20,588(2)}-\frac{1,252(12)}{20,588(2)}-\frac{199(12)}{67,672(2)}-\frac{886(12)}{67,672} \\
& =-0.395+0.650-0.365-0.018-0.157
\end{aligned}
$$

$$
\begin{aligned}
=-0.285 \mathrm{ksi}< & \begin{array}{l}
\text { Stress limit for compression under } \mathrm{LL}+1 / 2(\mathrm{DL}+\mathrm{PS}) \\
\\
\\
\text { load }(-2.4 \mathrm{ksi}) \text { OK }
\end{array}
\end{aligned}
$$

Girder bottom stress under all loads (Service III):

$$
\begin{aligned}
\mathrm{f}_{\text {bottom }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{bc}}+\mathrm{M}_{\mathrm{LLC}} / \mathrm{S}_{\mathrm{bc}} \\
& =\frac{-857}{1,085}-\frac{857(31.222)}{20,157}+\frac{1,252(12)}{20,157}+\frac{199(12)}{26,855}+\frac{0.8(886)(12)}{26,855} \\
& =-0.790-1.327+0.745+0.089+0.317 \\
& =-0.966 \mathrm{ksi}<\begin{array}{l}
\text { Stress limit for compression under full } \\
\quad \text { load }(-2.7 \text { ksi }) \mathbf{O K}
\end{array}
\end{aligned}
$$

Notice that the gross concrete composite section properties are typically used for the stress calculations due to all load components. However, some jurisdictions use the transformed section properties in calculating the stress due to live load. The transformed section properties are listed in Section 2. In this example, the gross section properties are used for this calculation.

Girder bottom stress under prestressing and dead load after losses:

$$
\begin{aligned}
\mathrm{f}_{\text {bottom }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{11} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{bc}} \\
& =\frac{-857}{1,085}-\frac{857(31.222)}{20,157}+\frac{1,252(12)}{20,157}+\frac{199(12)}{26,855} \\
& =-0.790-1.327+0.745+0.089 \\
& =-1.283 \mathrm{ksi}<\quad \begin{array}{l}
\text { Stress limit for compression under prestress and } \\
\text { permanent loads }(-2.7 \text { ksi }) \mathbf{O K}
\end{array}
\end{aligned}
$$

Sample Calculations at 54 ft . -6 in. From the CL of Bearing ( $55 \mathrm{ft} .-3 \mathrm{in}$. From Girder End) - Midspan of Noncomposite Girder

Girder top stress after losses under sum of all loads (Service I):

$$
\begin{aligned}
\mathrm{f}_{\mathrm{top}} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tc}}-\mathrm{M}_{\mathrm{LLC}} / \mathrm{S}_{\mathrm{tc}} \\
& =\frac{-1,096.2}{1,085}+\frac{1,096.2(31.38)}{20,588}-\frac{3,512(12)}{20,588}-\frac{387(12)}{67,672}-\frac{2,015(12)}{67,672} \\
& =-1.010+1.671-2.047-0.069-0.357
\end{aligned}
$$

$$
\begin{array}{r}
=-1.812 \mathrm{ksi}< \\
\text { Stress limit for compression } \\
\text { under full load }(-3.6 \mathrm{ksi}) \text { OK }
\end{array}
$$

Girder top stress after losses under prestress and permanent loads:

$$
\begin{aligned}
\mathrm{f}_{\text {top }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tc}} \\
& =\frac{-1,096.2}{1,085}+\frac{1,096.2(31.38)}{20,588}-\frac{3,512(12)}{20,588}-\frac{387(12)}{67,672} \\
& =-1.010+1.671-2.047-0.069 \\
& =-1.455 \mathrm{ksi}<\begin{array}{l}
\text { Stress limit for compression under prestress and } \\
\quad \text { permanent loads }(-2.7 \mathrm{ksi}) \mathbf{O K}
\end{array}
\end{aligned}
$$

Girder top stress under LL $+1 / 2(\mathrm{PS}+\mathrm{DL})$ after losses:

$$
\begin{aligned}
& \mathrm{f}_{\text {top }}=-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}+\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{t}}-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tc}}-\mathrm{M}_{\mathrm{LL}} / \mathrm{S}_{\mathrm{tc}} \\
&= \frac{-1,096.2}{1,085(2)}+\frac{1,096.2(31.38)}{20,588(2)}-\frac{3,512(12)}{20,588(2)}-\frac{387(12)}{67,672(2)}-\frac{2,015(12)}{67,672} \\
&=-0.505+0.835-1.024-0.034-0.357 \\
&=-1.085 \mathrm{ksi}<\quad \begin{array}{l}
\text { Stress limit for compression under } \mathrm{LL}+1 / 2(\mathrm{DL}+\mathrm{PS}) \\
\\
\quad \text { load }(-2.4 \mathrm{ksi}) \mathrm{OK}
\end{array}
\end{aligned}
$$

Girder bottom stress (Service III):

$$
\begin{aligned}
\mathrm{f}_{\mathrm{bottom}} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{bc}}+\mathrm{M}_{\mathrm{LLC}} / \mathrm{S}_{\mathrm{bc}} \\
& =\frac{-1,096.2}{1,085}-\frac{1,096.2(31.38)}{20,157}+\frac{3,512(12)}{20,157}+\frac{387(12)}{26,855}+\frac{0.8(2,015)(12)}{26,855} \\
& =-1.010-1.707+2.091+0.173+0.720 \\
& =0.267 \mathrm{ksi}<\text { Stress limit for tension }(0.465 \mathrm{ksi}) \mathbf{O K}
\end{aligned}
$$

Notice that the stresses are calculated without including creep and shrinkage. Jurisdictions that do not include creep and shrinkage typically design the girders for a reduced tensile stress limit or for zero tension at final condition. Including creep and shrinkage would normally result in additional tensile stress at the bottom of the beam at the midspan section.

Girder bottom stress after losses under prestress and dead load:

$$
\begin{aligned}
\mathrm{f}_{\text {bottom }} & =-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{54.5} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{bc}} \\
& =\frac{-1,096.2}{1,085}-\frac{1,096.2(31.38)}{20,157}+\frac{3,512(12)}{20,157}+\frac{387(12)}{26,855} \\
& =-1.010-1.707+2.091+0.173 \\
& =-0.453 \mathrm{ksi}<\text { Stress limit for compression }(-2.7 \mathrm{ksi}) \quad \mathbf{O K}
\end{aligned}
$$

Deck slab top stress under full load:

$$
\begin{aligned}
\mathrm{f}_{\text {top slab }} & =\left(-\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{tsc}}-\mathrm{M}_{\mathrm{LLC}} / \mathrm{S}_{\mathrm{tsc}}\right) / \text { modular ratio between beam and slab } \\
& =\left(-\frac{387(12)}{49,517}-\frac{1.0(2,015)(12)}{49,517}\right) /\left(\frac{4,696}{3,834}\right) \\
& =(-0.094-0.488) / 1.225 \\
& =-0.475 \mathrm{ksi}<\text { Stress limit for compression in slab }(-2.4 \mathrm{ksi}) \mathbf{O K}
\end{aligned}
$$

## Stresses at service limit state for sections in the negative moment region

Sections in the negative moment region may crack under service limit state loading due to high negative composite dead and live loads. The cracking starts in the deck and as the loads increase the cracks extend downward into the beam. The location of the neutral axis for a section subject to external moments causing compressive stress at the side where the prestressing force is located may be determined using a trial and error approach as follows:

1. Assume the location of the neutral axis.
2. Assume a value for the compressive strain at the extreme compression fiber (bottom of the beam). Calculate the tensile strain in the longitudinal reinforcement of the deck assuming the strain varies linearly along the height of the section and zero strain at the assumed location of the neutral axis.
3. Calculate the corresponding tension in the deck reinforcement based on the assumed strain.
4. Calculate the compressive force in the concrete.
5. Check the equilibrium of the forces on the section (prestressing, tension in deck steel and compression in the concrete). Change the assumed strain at the bottom of beam until the force equilibrium is achieved.
6. After the forces are in equilibrium, check the equilibrium of moments on the section (moment from prestressing, external moment and moment from internal compression and tension).
7. If moment equilibrium is achieved, the assumed location of the neutral axis and
strains are correct. If the moments are not in equilibrium, change the assumed location of the neutral axis and go to Step 2 above.
8. After both force and moment equilibriums are achieved, calculate the maximum stress in the concrete as the product of the maximum concrete strain and the concrete modulus of elasticity.

Notice that when additional compression is introduced into the concrete due to external applied forces, the instantaneous stress in the prestressing steel is decreased by the modular ratio multiplied by the additional compressive stress in the surrounding concrete. The change in the prestressing steel force is typically small and was ignored in the following calculations.

Sample Calculations for a Section in the Negative Moment Region Under Service Limit State, Section at $107 \mathrm{ft} .-3 \mathrm{in}$. From the CL of End Bearing ( 108 ft . From Girder End)

From Table 5.3-1,

|  | Noncomposite |  |  |  | Composite |  | Live Load + IM |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Location | Girder* | $\begin{array}{c}\text { Slab and } \\ \text { Haunch }\end{array}$ | $\begin{array}{c}\text { Exterior } \\ \text { Diaphragm }\end{array}$ | $\begin{array}{c}\text { Total } \\ \text { Noncomp. }\end{array}$ |  |  | Parapet | FWS \(\left.\begin{array}{c}Positive <br>

HL-93\end{array} $$
\begin{array}{c}\text { Negative } \\
\text { HL-93 }\end{array}
$$\right]\)

* Based on the simple span length of 109 ft .

Maximum negative moment at the section at $104.5 \mathrm{ft}=546-248-332-1,663$

$$
=-1,697 \mathrm{k}-\mathrm{ft}
$$

Maximum negative moment at the section at $108.0 \mathrm{ft}=125-297-398-1,921$

$$
=-2,491 \mathrm{k}-\mathrm{ft}
$$

By interpolation, the maximum Service I negative moment at the section under consideration is:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{neg}} & =-2,491-(-2,491+1,697)[(108-107.25) /(108-104.5)] \\
& =-2,321 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Trial and error approach (see above) was applied to determine the location of the neutral axis. The calculations of the last cycle of the process are shown below.

## Referring to Figure 5.6-1:

Assume neutral axis at 32.5 inches from the bottom of beam

Assume maximum concrete compressive strain $=0.00079$ in./in.
Tensile strain in deck reinforcement $=0.00079(75.52-32.5) / 32.5=0.001046$ in./in.
Modulus of elasticity of concrete beam $=4,696 \mathrm{ksi}($ see Section 2$)$

Concrete stress at bottom of beam $=0.00079(4,696)=3.71 \mathrm{ksi}$
Area of deck longitudinal reinforcement $=14.65 \mathrm{in}^{2}($ see Section 5.6.5.1 for calculation $)$
Force in deck steel $=14.65(0.001046)(29,000)=444.4 \mathrm{k}$
Force in prestressing steel $=797.2 \mathrm{k}$ (see Table 5.5-1)

## Compressive forces in the concrete:

Considering Figure 5.6-1, by calculating the forces acting on different areas as the volume of the stress blocks for areas A1, A2 and A3 as the volume of a wedge, prism or pyramid, as appropriate, the forces in Table 5.6-3 may be calculated. Recall that the centers of gravity of a wedge, a prism with all rectangular faces, a prism with a triangular vertical face and a pyramid are at one-third, one-half, one-third and one-quarter the height, respectively. The location of the centers of gravity shown in the figure may also be calculated. The moment from internal compressive concrete forces shown in Table $5.6-3$ is equal to the force multiplied by the distance from the neutral axis to the location of the force.

Table 5.6-3 - Forces in Concrete Under Service Load in Negative Moment Regions (Section at 107'-3" from the end bearing)

| Area <br> designation | Force <br> designation | Area | Stress | Force | Distance <br> from bot. <br> of beam | Distance <br> to N/A | Moment <br> at N/A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\left(\mathrm{in}^{2}\right)$ | $(\mathrm{ksi})$ | $(\mathrm{kips})$ | $(\mathrm{in})$ | $(\mathrm{in})$ | $(\mathrm{k}-\mathrm{ft})$ |
| A 1 | $\mathrm{P}_{1}$ | 260 | 3.71 | 482.3 | 10.83 | 21.67 | 871.0 |
| A 2 | $\mathrm{P}_{2} \mathrm{a}$ | 160 | 2.80 | 448.0 | 4.00 | 28.50 | $1,064.0$ |
| A 2 | $\mathrm{P}_{2} \mathrm{~b}$ | 160 | 0.91 | 72.8 | 2.67 | 29.83 | 181.0 |
| $\mathrm{~A} 3^{*}$ | $\mathrm{P}_{3} \mathrm{a}$ | 100 | 1.66 | 166.0 | 11.33 | 21.17 | 292.9 |
| $\mathrm{~A}{ }^{*}$ | $\mathrm{P}_{3} \mathrm{~b}$ | 100 | 1.14 | 76.0 | 10.50 | 22.00 | 139.3 |
| Total |  |  |  | $1,245.1$ |  |  | $2,548.2$ |



Figure 5.6-1 - Compressive Force in the Concrete

a) Rectangular Stress Distribution
b) Triangular Stress Distribution
*Figure 5.6-1a - Shapes Used in Determining Forces for A3

Sample force calculations for area A3.
Two components of stress act on area A3. The first component is a rectangular stress distribution with an intensity of 1.66 ksi . The second component is a triangular stress distribution with an intensity of 1.14 ksi .

Force due to the rectangular stress distribution:

$$
\begin{aligned}
\mathrm{F}_{\text {rect angular }} & =2[0.5(10)(10)](1.66) \\
& =166.0 \mathrm{k}
\end{aligned}
$$

The volume used to determine the effect of the triangular stress distribution is calculated using geometry of a pyramid.

$$
\begin{aligned}
\mathrm{F}_{\text {triangular }} & =2 \text { triangles }(1 / 3 \text { pyramid base })(\text { pyramid height }) \\
& =2(1 / 3)(10)(1.14)(10) \\
& =76.0 \mathrm{k}
\end{aligned}
$$

## Check force equilibrium:

Net force on section $=$ P/S steel force + concrete compressive force + deck steel force

$$
\begin{aligned}
& =797.2+(-1,245.1)+444.4 \\
& =-3.5 \mathrm{kips} \approx 0 \text { OK }
\end{aligned}
$$

## Check moment equilibrium:

Net M on the section $=$ external moment + prestressing force moment + deck slab force moment + concrete compression moment

$$
\begin{aligned}
& =2,321+797.2(32.5-5.375) / 12-444.4(75.52-32.5) / 12-2,548.2 \\
& =-18.4 \mathrm{k}-\mathrm{ft} \approx 0 \text { OK }
\end{aligned}
$$

From Table 5.6-3, the maximum stress in the concrete is 3.71 ksi . The stress limit for compression under all loads (Table S5.9.4.2.1-1) under service condition is $0.6 f_{c}$ (where $\mathrm{f}^{\prime}{ }_{\mathrm{c}}$ is the compressive strength of the girder concrete). For this example, the stress limit equals 3.6 ksi .

The calculated stress equals 3.71 ksi or is $3 \%$ overstressed. However, as explained above, the stress in the prestressing steel should decrease due to compressive strains in the concrete caused by external loads, i.e., prestressing steel force less than 797.2 k and the actual stress is expected to be lower than the calculated stress, and the above difference (3\%) is considered within the acceptable tolerance.

Notice that the above calculations may be repeated for other cases of loading in Table S5.9.4.2.1-1 and the resulting applied stress is compared to the respective stress limit. However, the case of all loads applied typically controls.

## Design Step Longitudinal steel at top of girder

### 5.6.3

The tensile stress limit at transfer used in this example requires the use of steel at the tension side of the beam to resist at least $120 \%$ of the tensile stress in the concrete calculated based on an uncracked section (Table S5.9.4.1.2-1). The sample calculations are shown for the section in Table 5.6-1 with the highest tensile stress at transfer, i.e., the section at 1.75 ft. from the centerline of the end bearing.

By integrating the tensile stress in Figure 5.6-2 over the corresponding area of the beam, the tens ile force may be calculated as:

$$
\begin{aligned}
\text { Tensile force }= & 5(42)(0.451+0.268) / 2+7.33(8.0)(0.268+0.0) / 2+2[4(3)](0.268+ \\
& 0.158) / 2+2[4(4) / 2][0.012+(0.158-0.012)(2 / 3)]+2[3(13) / 2][0.158+ \\
& (0.268-0.158)(2 / 3)] \\
= & 99.2 \mathrm{k}
\end{aligned}
$$

Required area of steel $=1.2(99.2) / \mathrm{f}_{\mathrm{y}}$

$$
\begin{aligned}
& =119.0 / 60 \\
& =1.98 \mathrm{in}^{2}
\end{aligned}
$$

Required number of \#5 bars $=1.98 / 0.31$

$$
=6.39 \mathrm{bars}
$$

Minimum allowable number of bars $=7$ \#5 bars
Use 8 \#5 bars as shown in Figure 5.6-3


Figure 5.6-2 - Stress at Location of Maximum Tensile Stress at Transfer


Figure 5.6-3 - Longitudinal Reinforcement of Girder Top Flange

Design Step 5.6.4

## Sample calculations at midspan

c = distance between the neutral axis and the compressive face at the nominal flexural resistance (in.)
c $=5.55$ in., which is less than the slab thickness, therefore, the neutral axis is in the slab and section is treated as a rectangular section. (See Design Step 5.5.1 for commentary explaining how to proceed if "c" is greater than the deck thickness.)
$\mathrm{f}_{\mathrm{ps}}=$ stress in the prestressing steel at the nominal flexural resistance (ksi) $\mathrm{f}_{\mathrm{ps}}=264.4 \mathrm{ksi}$

The factored flexural resistance, $M$, shall be taken as $\varphi M_{n}$, where $M_{n}$ is determined using Eq. S5.7.3.2.2-1.

Factored flexural resistance in flanged sections (S5.7.3.2.2)

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{ps}} \mathrm{f}_{\mathrm{ps}}\left(\mathrm{~d}_{\mathrm{p}}-\mathrm{a} / 2\right)+\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right)-\mathrm{A}_{\mathrm{s}}^{\prime} \mathrm{f}_{\mathrm{y}}^{\prime}\left(\mathrm{d}_{\mathrm{s}}^{\prime}-\mathrm{a} / 2\right)+0.85 \mathrm{f}_{\mathrm{c}}^{\prime}\left(\mathrm{b}-\mathrm{b}_{\mathrm{w}}\right) \beta_{1} \mathrm{~h}_{\mathrm{f}}\left(\mathrm{a} / 2-\mathrm{h}_{\mathrm{f}} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

The definition of the variables in the above equation and their values for this example are as follows:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{ps}} & =\text { area of prestressing steel }\left(\mathrm{in}^{2}\right) \\
& =6.73 \mathrm{in}^{2} \\
\mathrm{f}_{\mathrm{ps}} & =\text { average stress in prestressing steel at nominal bending resistance } \\
& \quad \text { specified in Eq. S5.7.3.1.1-1 (ksi) } \\
& =264.4 \mathrm{ksi}
\end{aligned}
$$

$d_{p}=$ distance from extreme compression fiber to the centroid of prestressing tendons (in.)

$$
=74.5 \mathrm{in} .
$$

$\mathrm{A}_{\mathrm{s}}=$ area of nonprestressed tension reinforcement $\left(\mathrm{in}^{2}\right)$
$=0.0 \mathrm{in}^{2}$
$\mathrm{f}_{\mathrm{y}}=$ specified yield strength of reinforcing bars (ksi)
$=60 \mathrm{ksi}$
$d_{s}=$ distance from extreme compression fiber to the centroid of nonprestressed tensile reinforcement (in.), NA

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}}^{\prime} & =\text { area of compression reinforcement }\left(\mathrm{in}^{2}\right) \\
& =0.0 \mathrm{in}^{2}
\end{aligned}
$$

$\mathrm{f}_{\mathrm{y}}^{\prime}=$ specified yield strength of compression reinforcement (ksi), NA
$\mathrm{d}_{\mathrm{s}}=$ distance from the extreme compression fiber to the centroid of compression reinforcement (in.), NA
$f_{c}^{\prime}=$ specified compressive strength of concrete at 28 days, unless another age is specified (ksi)
$=4.0 \mathrm{ksi}$ (slab)
$\mathrm{b}=$ width of the effective compression block of the member (in.)
$=$ width of the effective flange $=111 \mathrm{in}$. (See Design Step 5.5.1 for commentary for the determination of the effective width, $b$, when the calculations indicate that the compression block depth is larger than the flange thickness.)
$b_{w}=$ web width taken equal to the section width " $b$ " for a rectangular section (in.), NA
$\beta_{1}=$ stress block factor specified in S5.7.2.2, NA
$\mathrm{h}_{\mathrm{f}}=$ compression flange depth of an I or T member (in.), NA
a $=\beta_{1} \mathrm{c}$; depth of the equivalent stress block (in.)
$=0.85(5.55)$
$=4.72 \mathrm{in}$.

The second, third and fourth terms in Eq. S5.7.3.2.2-1 are equal to zero for this example.
Substituting,

$$
\begin{aligned}
\mathrm{M}_{\mathrm{n}} & =6.73(264.4)[74.5-(4.72 / 2)] \\
& =128,367 / 12 \\
& =10,697 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Therefore, the factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, shall be taken as:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\varphi= & \text { resistance factor as specified in S5.5.4.2 for flexure in prestressed } \\
& \text { concrete } \\
= & 1.0
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =1.0(10,697 \mathrm{k}-\mathrm{ft}) \\
& =10,697 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

The maximum factored applied moment for Strength I limit state is $8,456 \mathrm{k}-\mathrm{ft}$ (see Table 5.3-2)

$$
\mathrm{M}_{\mathrm{r}}=10,697 \mathrm{k}-\mathrm{ft}>\mathrm{M}_{\mathrm{u}}=8,456 \mathrm{k}-\mathrm{ft} \mathbf{O K}
$$

## Design Step

Check if section is over-reinforced
5.6.4.1

Limits for reinforcing (S5.7.3.3)
The maximum amount of prestressed and nonprestressed reinforcement must be such that:

$$
\begin{equation*}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \quad \leq 0.42 \tag{S5.7.3.3.1-1}
\end{equation*}
$$

where:
c $=5.55$ in. (see Section 5.5.1)
$d_{e}=74.5$ in. (same as $d_{p}$ since no mild steel is considered)
$\mathrm{c} / \mathrm{d}_{\mathrm{e}}=5.55 / 74.5$

$$
=0.074<0.42 \text { OK }
$$

## Design Step

5.6.4.2

Check minimum required reinforcement (S5.7.3.3.2)
Critical location is at the midspan of the continuous span $=55 \mathrm{ft}$. from the end bearing.
All strands are fully bonded at this location.
According to S5.7.3.3.2, unless otherwise specified, at any section of a flexural component, the amount of prestressed and nonprestressed tensile reinforcement shall be adequate to develop a factored flex ural resistance, $M_{b}$, at least equal to the lesser of:
1.2 times the cracking strength determined on the basis of elastic stress distribution and the modulus of rupture, $f_{1}$, on the concrete as specified in S5.4.2.6.
OR
1.33 times the factored moment required by the applicable strength load combinations specified in Table 3.4.1-1.

The cracking moment, $\mathrm{M}_{\mathrm{cr}}$, is calculated as the total moment acting on the beam when the maximum tensile stress equals the modulus of rupture.

$$
\mathrm{f}_{\mathrm{r}} \quad=-\mathrm{P}_{\mathrm{t}} / \mathrm{A}_{\mathrm{g}}-\mathrm{P}_{\mathrm{t}} \mathrm{e} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DNC}} / \mathrm{S}_{\mathrm{b}}+\mathrm{M}_{\mathrm{DC}} / \mathrm{S}_{\mathrm{bc}}+\mathrm{M} / \mathrm{S}_{\mathrm{bc}}
$$

where:

$$
\begin{aligned}
& \mathrm{M}_{\mathrm{DNC}}=\text { factored using Service I limit state, see Table 5.3-1 } \\
&=3,511 \mathrm{k}-\mathrm{ft} \\
& \mathrm{M}_{\mathrm{DC}}=\text { factored using Service I limit state, see Table 5.3-1 } \\
&=384 \mathrm{k}-\mathrm{ft} \\
& \mathrm{P}_{\mathrm{t}}=\mathrm{f}_{\mathrm{pf}} \mathrm{~A}_{\text {strand }} \mathrm{N}_{\text {strands }} \\
&=1,096.2 \mathrm{k} \text { (from Table 5.6-2) } \\
& \mathrm{A}_{\mathrm{g}}=1,085 \mathrm{in}^{2} \\
& \mathrm{e}_{54.5}=31.38 \mathrm{in.} \\
& \mathrm{~S}_{\mathrm{b}}=20,157 \mathrm{in}^{3} \\
& \mathrm{~S}_{\mathrm{bc}}=26,855 \mathrm{in}^{3} \\
& \mathrm{f}_{\mathrm{r}}=0.24 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \\
&=0.24 \sqrt{6} \\
&=0.587 \mathrm{ksi} \\
& 0.587=\frac{-1,096.2}{1,085}-\frac{1,096.2(31.38)}{20,157}+\frac{3,511(12)}{20,157}+\frac{384(12)}{26,855}+\frac{\mathrm{M}}{26,855}
\end{aligned}
$$

Solving for M, the additional moment required to cause cracking, in this equation:

$$
\begin{aligned}
\mathrm{M} & =27,983 / 12 \\
& =2,332 \mathrm{k}-\mathrm{ft} \\
\mathrm{M}_{\mathrm{cr}} & =\mathrm{M}_{\mathrm{DNC}}+\mathrm{M}_{\mathrm{DC}}+\mathrm{M} \\
& =3,511+384+2,332 \\
& =6,227 \mathrm{k}-\mathrm{ft} \\
1.2 \mathrm{M}_{\mathrm{cr}} & =1,2(6,227) \\
& =7,472 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

The applied factored moment, $\mathrm{M}_{\mathrm{u}}$, taken from Table 5.3-2 is 8,456 k-ft (Strength I)

$$
1.33(8,456)=11,246 \mathrm{k}-\mathrm{ft}
$$

$\mathrm{M}_{\mathrm{r}}$ has to be greater than the lesser of $1.2 \mathrm{M}_{\mathrm{cr}}$ and $1.33 \mathrm{M}_{\mathrm{u}}$, i.e., $7,472 \mathrm{k}-\mathrm{ft}$.
$\mathrm{M}_{\mathrm{r}}$ also has to be greater than the applied factored load $\mathrm{M}_{\mathrm{i}}=8,456 \mathrm{k}-\mathrm{ft}$ (strength requirement)
$\mathrm{M}_{\mathrm{r}}=10,697 \mathrm{k}-\mathrm{ft}$, therefore, both provisions are $\mathbf{O K}$

## Design Step 5.6.5 <br> Design Step <br> 5.6.5.1

## Continuity connection at intermediate support

Negative moment connection at the Strength limit state
Determine the deck steel at the intermediate pier.
Based on preliminary calculations, the top and bottom longitudinal reinforcement of the deck are assumed to be \#6 bars at 5.5 in . spacing and \#6 bars at 8.5 in . spacing, respectively (see Figure 5.6-5).

Calculate the total area of steel per unit width of slab:

$$
\mathrm{A}_{\mathrm{s}}=\mathrm{A}_{\text {bar }} / \text { spacing }\left(\mathrm{in}^{2} / \mathrm{in} .\right)
$$

For top row of bars: $\quad \mathrm{A}_{\text {s top }}=0.44 / 5.5$

$$
=0.08 \mathrm{in}^{2} / \mathrm{in} .
$$

For bottom row of bars: $\quad \mathrm{A}_{\text {s bot }}=0.44 / 8.5$

$$
=0.052 \mathrm{in}^{2} / \mathrm{in} .
$$

Therefore,

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}} & =0.08+0.052 \\
& =0.132 \mathrm{in}^{2} / \mathrm{in} .
\end{aligned}
$$

Calculate the center of gravity of the slab steel from the top of the slab. Calculations are made from the top of the total thickness and include the integral wearing surface in the total thickness of slab. (See Figure 4-16)

$$
\text { Top mat (B1): } \quad \begin{aligned}
\mathrm{CGS}_{\text {top }} & =\text { Cover }_{\text {top }}+\text { Dia }_{\# 5} \text { main rein. }+1 / 2 \text { Dia }_{\# 6} \\
& =2.5+0.625+1 / 2(0.75) \\
& =3.5 \mathrm{in} .
\end{aligned}
$$

Bot. mat (B2): $\mathrm{CGS}_{\text {bot }}=\mathrm{t}_{\text {slab }}-$ Cover $_{\text {bot }}-$ Dia\#5 main rein. $^{-1 / 2}$ Dia $_{\# 6}$

$$
=8-1-0.625-1 / 2(0.75)
$$

$$
=6 \mathrm{in} .
$$

Center of gravity of the deck longitudinal reinforcement from the top of the deck:

$$
\begin{aligned}
\mathrm{CGS} & =\left[\mathrm{A}_{\mathrm{s} \text { top }}\left(\mathrm{CGS}_{\text {top }}\right)+\mathrm{A}_{\mathrm{s} \text { bot }}\left(\mathrm{CGS}_{\text {bot }}\right)\right] / \mathrm{A}_{\mathrm{s}} \\
& =[0.08(3.5)+0.052(6)] / 0.132 \\
& =4.48 \text { in. from the top of slab } \quad \begin{array}{l}
\text { ( } 3.98 \text { in. from the top of the structural } \\
\text { thickness })
\end{array}
\end{aligned}
$$

Calculate the depth to the slab steel from the bottom of the beam. The haunch depth is ignored in the following calculations.

$$
\begin{aligned}
\mathrm{d}_{\mathrm{s}} & =\text { girder }+ \text { slab }- \text { CGS } \\
& =72+8-4.48 \\
& =75.52 \mathrm{in.} .
\end{aligned}
$$

The specification is silent about the strength of the concrete in the connection zone. Many jurisdictions use the girder concrete strength for these calculations. This reflects observations made during girder tests in the past. In these tests, the failure always occurred in the girder. This behavior is due to the confinement of the diaphragm concrete in the connection zone provided by the surrounding concrete. This confinement increases the apparent strength of the diaphragm concrete compared to the unconfined strength measured during typical testing of concrete cylinders.

Assume the neutral axis is in the bottom flange (rectangular behavior), therefore,

$$
\begin{aligned}
& f_{c}^{\prime}=f_{c}^{\prime}, \text { beam }=6.0 \mathrm{ksi} \\
& \beta_{1}=\beta_{1, \text { beam }}^{\prime}=0.75 \text { (corresponds to the } 6.0 \text { ksi concrete, S5.7.2.2) } \\
& \mathrm{b}=\text { width of section }=\text { width of girder bottom flange }=28 \mathrm{in} .
\end{aligned}
$$

Calculate c,

$$
\begin{equation*}
\mathrm{c}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \beta_{1} \mathrm{f}_{\mathrm{c}} \mathrm{~b} \tag{S5.7.3.1.1-4,modified}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}}= & \text { area of reinforcement within the effective flange } \\
& \text { width of } 111 \mathrm{in.}\left(\text { in }^{2}\right) \\
= & \mathrm{A}_{\mathrm{s}} \mathrm{~b}_{\mathrm{slab}} \\
& =(0.132)(111) \\
& =14.65 \mathrm{in}^{2} \\
\mathrm{f}_{\mathrm{y}} & =60 \mathrm{ksi} \\
\mathrm{f}_{\mathrm{c}}^{\prime} & =6.0 \mathrm{ksi} \\
\beta_{1} & =0.75 \\
\mathrm{~b} & =28 \mathrm{in} .
\end{aligned}
$$

$\mathrm{c}=14.65(60) /[0.85(0.75)(6.0)(28)]$
$=8.21$ in., which is approximately equal to the thickness of the bottom flange of the beam ( 8 in .), therefore, the section is checked as a rectangular section. If "c" was significantly larger than the thickness of the bottom flange, a reduction in the section width should be considered.

Calculate the nominal flexural resistance according to S5.7.3.2.1 and the provisions for a rectangular section.

$$
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right)
$$

where:

$$
\begin{aligned}
& \mathrm{a}=\beta_{1} \mathrm{c} \\
&=0.75(8.21) \\
&=6.16 \mathrm{in} . \\
& \mathrm{d}_{\mathrm{s}}=75.52 \mathrm{in} . \\
& \mathrm{M}_{\mathrm{n}}=14.65(60)[75.52-(6.16 / 2)] / 12 \\
&=5,306 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

The factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, is

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi_{\mathrm{f}} \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

where:
$\varphi_{\mathrm{f}}=0.9$ for flexure in reinforced concrete (S5.5.4.2.1)

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(5,306) \\
& =4,775 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Check moment capacity versus the maximum applied factored moment at the critical location

Critical location is at the centerline of pier.
Strength I limit state controls.

$$
\left|\mathrm{M}_{\mathrm{u}}\right|=4,729 \mathrm{k}-\mathrm{ft}(\text { see Table } 5.3-2)<\mathrm{M}_{\mathrm{r}}=4,775 \mathrm{k}-\mathrm{ft} \mathbf{O K}
$$

## Check service crack control (S5.5.2)

Actions to be considered at the service limit state are cracking, deformations, and concrete stresses, as specified in Articles S5.7.3.4, S5.7.3.6, and S5.9.4, respectively. The cracking stress is taken as the modulus of rupture specified in S5.4.2.6.

Components shall be so proportioned that the tensile stress in the mild steel reinforcement at the service limit state does not exceed $\mathrm{f}_{\mathrm{sa}}$, determined as:

$$
\mathrm{f}_{\mathrm{sa}} \quad=\mathrm{Z} /\left(\mathrm{d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3} \leq 0.6 \mathrm{f}_{\mathrm{y}}=0.6(60)=36 \mathrm{ksi}
$$

where:
$\mathrm{Z}=$ crack width parameter (kip/in.)
$=170 \mathrm{kip} / \mathrm{in}$. (for members in moderate exposure conditions; the example bridge is located in a warm climate (Atlanta) where the use of deicing salts is possible, but not likely)
$\mathrm{d}_{\mathrm{c}}=$ depth of concrete measured from extreme tension fiber to center of bar or wire located closest thereto (in.); for calculation purposes, the thickness of clear cover used to compute $d_{c}$ shall not be taken to be greater than 2.0 in .
$=$ concrete cover $+1 / 2$ secondary rein.
$=2.0+1 / 2(0.75)=2.375 \mathrm{in}$. $($ see Figure 5.6-4)
A = area of concrete having the same centroid as the principal tensile reinforcement and bounded by the surfaces of the cross-section and a straight line parallel to the neutral axis, divided by the number of bars or wires $\left(\mathrm{in}^{2}\right)$; for calculation purposes, the thickness of clear concrete cover used to compute "A" shall not be taken to be greater than 2.0 in .
$=[2(2.0)+0.75] 5.5 / 1 \mathrm{bar}=26.125 \mathrm{in}^{2} / \mathrm{bar}($ see Figure 5.6-4)


Figure 5.6-4 - Dimensions for Calculation of the Area, A

$$
\begin{aligned}
\mathrm{f}_{\mathrm{sa}} & =170 /[2.375(26.125)]^{1 / 3} \\
& =42.94 \mathrm{ksi}>0.6 \mathrm{f}_{\mathrm{y}}=36 \mathrm{ksi}, \text { therefore, use } \mathrm{f}_{\mathrm{sa}}=36 \mathrm{ksi}
\end{aligned}
$$

Connection moment at Service I limit state is $2,858 \mathrm{k}$ - ft (see Table 5.3-2)
Assuming: Section width is equal to beam bottom flange width $=28 \mathrm{in}$.
Modular ratio $=6$ for 6 ksi concrete
Area of steel $=14.65 \mathrm{in}^{2}$
At service limit state, the depth of the neutral axis and the transformed moment of inertia under service loads may be calculated using the same procedure used earlier in the example (Section 4). The neutral axis is 18.86 in . from the bottom of the beam.

Maximum service stress in the steel $=33.74 \mathrm{ksi}<36 \mathrm{ksi}$ OK

## Design Step

Positive moment connection
5.6.5.2

For jurisdictions that consider creep and shrinkage in the design, it is likely that positive moment will develop at intermediate piers under the effect of prestressing, permanent loads and creep and shrinkage. These jurisdictions provide reinforcement at the bottom of the beams at intermediate diaphragms to resist the factored positive moment at these locations.

For jurisdictions that do not consider creep and shrinkage in the design, it is unlikely that live load positive moments at intermediate supports will exceed the negative moments from composite permanent loads at these locations. This suggests that there is no need for the positive moment connection. However, in recognition of the presence of creep and shrinkage effects, most jurisdictions specify some reinforcement to resist positive moments.

Two forms of the connection have been in use:

1) Figure 5.6-5 shows one alternative that requires extending some of the prestressing strands at the end of the girder into the intermediate diaphragm. Due to the small space between girders, these strands are bent upwards into the diaphragm to provide adequate anchorage. Only strands that are fully bonded are used for the positive moment connection.
2) The second alternative requires adding mild reinforcement bars as shown in Figure 5.6-6. This alternative may lead to congestion at the end of the beam due to the presence of the prestressing strands at these locations.

Typical details of the top of the pier cap for expansion and fixed bearings are shown schematically in Figures 5.6-7 and 5.6-8.


Figure 5.6-5 - Continuity Connection Alternative 1: Strands Used for Positive Moment Connection


Figure 5.6-6 - Continuity Connection Alternative 2: Reinforcement Bars Used for Positive Moment Connection


Figure 5.6-7 - Typical Diaphragm at Intermediate Pier (Expansion Bearing)


Figure 5.6-8 - Typical Diaphragm at Intermediate Pier (Fixed Bearing)

## Design Step 5.6.6

Fatigue in prestressed steel (S5.5.3)
Article S5.5.3 states that fatigue need not be checked when the maximum tensile stress in the concrete under Service III limit state is taken according to the stress limits of Table S5.9.4.2.2-1. The stress limit in this table was used in this example and, therefore, fatigue of the prestressing steel need not be checked.

## Design Step Camber (S5.7.3.6)

5.6.7

The provisions of S2.5.2.6 shall be considered.
Deflection and camber calculations shall consider dead load, live load, prestressing, erection loads, concrete creep and shrinkage, and steel relaxation. For determining deflection and camber, the provisions of Articles S4.5.2.1, S4.5.2.2, and S5.9.5.5 shall apply.

Instantaneous deflections are computed using the modulus of elasticity for concrete as specified in S5.4.2.4 and taking the gross moment of inertia, $I_{g}$, as allowed by S5.7.3.6.2.

Deflection values are computed based on prestressing, girder self-weight, slab, formwork, exterior diaphragm weight, and superimposed dead load weight. Camber values are computed based on initial camber, initial camber adjusted for creep, and final camber. Typically, these calculations are conducted using a computer program. Detailed calculations are presented below.

Deflection due to initial prestressing is computed as:

$$
\begin{array}{lll}
\Delta_{\mathrm{P} / \mathrm{S}} & =-\left(\mathrm{P}_{\mathrm{t}} \mathrm{e}_{\mathrm{s}} \mathrm{~L}^{2}\right) /\left(8 \mathrm{E}_{\mathrm{ci}} \mathrm{I}_{\mathrm{g}}\right) & \text { (for straight bonded strands) } \\
\Delta_{\mathrm{P} / \mathrm{S}} & =-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{\mathrm{s}}\left[\mathrm{~L}^{2}-\left(\mathrm{L}_{\mathrm{t}}+2 \mathrm{~L}_{\mathrm{x}}\right)^{2}\right] /\left(8 \mathrm{E}_{\mathrm{Ci}} \mathrm{I}_{\mathrm{g}}\right) & \text { (for debonded strands) }
\end{array}
$$

where:
$\mathrm{P}_{\mathrm{t}}=$ applied load acting on the section (kips)
$e_{s}=$ eccentricity of the prestressing force with respect to the centroid of the cross section at the midspan of the beam (in.)
$\mathrm{L}=$ span length (ft.)
$\mathrm{L}_{t}=$ transfer length of the strands (in.)
$\mathrm{L}_{\mathrm{x}}=$ distance from end of beam to point where bonding commences (in.)
$\mathrm{E}_{\mathrm{ci}}=$ modulus of elasticity of concrete at transfer (ksi)
$\mathrm{I}_{\mathrm{g}}=$ moment of inertia $\left(\mathrm{in}^{4}\right)$
The negative sign indicates upward deflection.
Computer software is generally used to determine the deflections due to each loading. However, sample calculations are provided for this example.

See Table 5.5-1 for prestressing forces.
Group 1 strands: 32 fully bonded strands
Initial prestressing force $=924.4 \mathrm{k}$
Distance from bottom of the beam to the neutral axis $=36.38 \mathrm{in}$.
Distance from the bottom of the beam to the centroid of Group 1 strands $=5.375$ in.
Deflection due to Group 1 strands:

$$
\begin{aligned}
\Delta_{\mathrm{P} / \mathrm{S} 1} & =-\left(\mathrm{P}_{\mathrm{t}} \mathrm{e}_{\mathrm{s}} \mathrm{~L}^{2}\right) /\left(8 \mathrm{E}_{\mathrm{c} i} \mathrm{I}_{\mathrm{g}}\right) \\
& =-\left[924.4(36.38-5.375)[109(12)]^{2}\right] /[8(4,200)(733,320)] \\
& =-1.99 \mathrm{in.} \text { (upward deflection) }
\end{aligned}
$$

Group 2 strands: 6 strands debonded for 10 ft . from centerline of bearings
Transfer length $=30 \mathrm{in}$.
Initial prestressing force $=173.3 \mathrm{k}$
From Figures 2-5 and 2-6, the distance from the bottom of the beam to the centroid of Group 2 is 4.0 in .

Deflection due to Group 2 strands:

$$
\begin{aligned}
\Delta_{\mathrm{P} / \mathrm{S} 2} & =-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{\mathrm{s}}\left[\mathrm{~L}^{2}-\left(\mathrm{L}_{\mathrm{t}}+2 \mathrm{~L}_{\mathrm{x}}\right)^{2}\right] /\left(8 \mathrm{E}_{\mathrm{i}} \mathrm{I}_{\mathrm{g}}\right) \\
& =-173.3(36.38-4.0)\left[[109(12)]^{2}-[30+2(10)(12)]^{2}\right] /[8(4,200)(733,320)] \\
& =-0.37 \text { in. (upward deflection) }
\end{aligned}
$$

Group 3 strands: 6 strands debonded for 22 ft . from centerline of bearings
Transfer length $=30 \mathrm{in}$.
Initial prestressing force $=173.3 \mathrm{k}$
From Figures 2-5 and 2-6, the distance from the bottom of the beam to the centroid of Group 3 is 4.0 in .

Deflection due to Group 3 strands:

$$
\begin{aligned}
\Delta_{\mathrm{P} / \mathrm{S} 3} & =-\mathrm{P}_{\mathrm{t}} \mathrm{e}_{\mathrm{s}}\left[\mathrm{~L}^{2}-\left(\mathrm{L}_{\mathrm{t}}+2 \mathrm{~L}_{\mathrm{x}}\right)^{2}\right] /\left(8 \mathrm{E}_{\mathrm{i}} \mathrm{I}_{\mathrm{g}}\right) \\
& =-173.3(36.38-4.0)\left[[109(12)]^{2}-[30+2(22)(12)]^{2}\right] /[8(4,200)(733,320)] \\
& =-0.32 \text { in. (upward deflection) }
\end{aligned}
$$

Total initial deflection due to prestressing:

$$
\begin{aligned}
\Delta_{\mathrm{P} / \mathrm{S} \text { Tot }} & =-1.99-0.37-0.32 \\
& =-2.68 \text { in. (upward deflection) }
\end{aligned}
$$

Notice that for camber calculations, some jurisdictions assume that some of the prestressing force is lost and only consider a percentage of the value calculated above (e.g. Pennsylvania uses $90 \%$ of the above value). In the following calculations the full value is used. The user may revise these values to match any reduction required by the bridge owner's specification.

Using conventional beam theory to determine deflection of simple span beams under uniform load or concentrated loads and using the loads calculated in Section 5.2, using noncomposite and composite girder properties for loads applied before and after the slab is hardened, respectively, the following deflections may be calculated:
$\Delta_{\mathrm{sw}} \quad=$ deflection due to the girder self-weight
$=1.16 \mathrm{in}$.
$\Delta_{\mathrm{s}} \quad=$ deflection due to the slab, formwork, and exterior diaphragm weight $=1.12 \mathrm{in}$.
$\Delta_{\text {SDL }}=$ deflection due to the superimposed dead load weight $=0.104 \mathrm{in}$.

## Design Step

5.6.7.1

Initial camber, $\mathrm{C}_{\mathrm{i}}$ :

$$
\begin{aligned}
\mathrm{C}_{\mathrm{i}} & =\Delta_{\mathrm{P} / \mathrm{STot}}+\Delta_{\mathrm{sw}} \\
& =-2.68+1.16 \\
& =-1.52 \text { in. (upward deflection) }
\end{aligned}
$$

Initial camber adjusted for creep, $\mathrm{C}_{\mathrm{i} A}$ :

$$
\mathrm{C}_{\mathrm{iA}}=\mathrm{C}_{\mathrm{i}} \mathrm{C}_{\mathrm{r}}
$$

where:
$\mathrm{C}_{\mathrm{r}}=$ constant to account for creep in camber (S5.4.2.3.2)

$$
\begin{equation*}
=3.5 \mathrm{k}_{\mathrm{c}} \mathrm{k}_{\mathrm{f}}\left(1.58-\frac{\mathrm{H}}{120}\right) \mathrm{t}_{\mathrm{i}}^{-0.118} \frac{\left(\mathrm{t}-\mathrm{t}_{\mathrm{i}}\right)^{0.6}}{10.0+\left(\mathrm{t}-\mathrm{t}_{\mathrm{i}}\right)^{0.6}} \tag{S5.4.2.3.2-1}
\end{equation*}
$$

$\mathrm{k}_{\mathrm{c}}=$ factor for the effect of the volume-to-surface area ratio of the component as specified in Figure S5.4.2.3.2-1

In order to determine $\mathrm{k}_{\mathfrak{c}}$, the volume-to-surface area ratio needs to be calculated. See Figure 2-3 for girder dimensions.

$$
\begin{array}{ll}
\text { Beam area } & =1,085 \mathrm{in}^{2} \\
& \\
\text { Beam volume } & =1,085(12) \\
& =13,020 \mathrm{in}^{3} / \mathrm{ft} \\
\text { Surface area } & =2,955.38 \mathrm{in}^{2} / \mathrm{ft} \\
& \\
(\mathrm{~V} / \mathrm{S})_{\mathrm{b}} & =13,020 / 2,955.38 \\
& =4.406 \mathrm{in} .
\end{array}
$$

Using Figure S5.4.2.3.2-1 or SC5.4.2.3.2-1, the correction factor, $\mathrm{k}_{\mathrm{c}}$, is taken to be approximately 0.759 .
$\mathrm{k}_{\mathrm{f}}=$ factor for the effect of concrete strength

$$
\begin{aligned}
& =\frac{1}{0.67+\left(\frac{f_{c}^{\prime}}{9}\right)} \\
& =\frac{1}{0.67+\left(\frac{6.0}{9}\right)}=0.748
\end{aligned}
$$

$\mathrm{H}=$ relative humidity from Figure S5.4.2.3.3-1
= $70 \%$
$\mathrm{t}_{\mathrm{i}}=$ age of concrete when load is initially applied
$=1$ day
t = maturity of concrete
$=$ infinite

$$
\begin{aligned}
\mathrm{C}_{\mathrm{r}} & =3.5(0.759)(0.748)[1.58-(70 / 120)](1)^{-0.118} \\
& =1.98
\end{aligned}
$$

Therefore, the initial camber, $\mathrm{C}_{\mathrm{iA}}$ is:

$$
\begin{aligned}
\mathrm{C}_{\mathrm{iA}} & =-1.52(1.98) \\
& =-3.01 \text { in. (upward deflection) }
\end{aligned}
$$



Figure 5.6-9 - Schematic View of Haunch

Design Step
5.6.7.3

Camber to determine probable sag in bridge
To eliminate the possibility of sag in the bridge under permanent loads, some jurisdictions require that the above calculations for $C_{F}$ be repeated assuming a further reduction in the initial P/S camber. The final $C_{F}$ value after this reduction should show upward deflection.

## Design Step $\quad$ Optional live load deflection check

Service load deformations may cause deterioration of wearing surfaces and local cracking in concrete slabs and in metal bridges which could impair serviceability and durability, even if self limiting and not a potential source of collapse.

As early as 1905, attempts were made to avoid these effects by limiting the depth-to-span ratios of trusses and girders, and starting in the 1930's, live load deflection limits were prescribed for the same purpose. In a study of deflection limitations of bridges ASCE (1958), an ASCE committee, found numerous shortcomings in these traditional approaches and noted them. For example:
"The limited survey conducted by the Committee revealed no evidence of serious structural damage that could be attributed to excessive deflection. The few examples of damaged stringer connections or cracked concrete floors could probably be corrected more effectively by changes in design than by more restrictive limitations on deflection. On the other hand, both the historical study and the results from the survey indicate clearly that unfavorable psychological reaction to bridge deflection is probably the most frequent and important source of concern regarding the flexibility of bridges. However, those characteristics of bridge vibration which are considered objectionable by pedestrians or passengers in vehicles cannot yet be defined."

Since that time, there has been extensive research on human response to motion, and it is now generally agreed that the primary factor affecting human sensitivity is acceleration as opposed to deflection, velocity, or the rate of change of acceleration for bridge structures, but the problem is a difficult subjective one. Thus, to this point in history there are no simple definitive guidelines for the limits of tolerable static deflection or dynamic motion. Among current specifications, the Ontario Highway Bridge Design Code of 1983 contains the most comprehensive provisions regarding vibrations tolerable to humans.

The deflection criteria in S2.5.2.6.2 is considered optional. The bridge owner may select to invoke this criteria if desired. If an Owner chooses to invoke deflection control, the following principles may apply:

- when investigating the maximum absolute deflection, all design lanes should be loaded, and all supporting components should be assumed to deflect equally,
- for composite design, the design cross-section should include the entire width of the roadway and the structurally continuous portions of the railings, sidewalks and median barriers
- when investigating maximum relative displacements, the number and position of loaded lanes should be selected to provide the worst differential effect,
- the live load portion of load combination Service I of Table S3.4.1-1 should be used, including the dynamic load allowance, IM
- the live load shall be taken from S3.6.1.3.2,
- the provisions of S3.6.1.1.2 should apply,
- for skewed bridges, a right cross-section may be used; for curved and curved skewed bridges a radial cross-section may be used.

If the Owner invokes the optional live load deflection criteria, the deflection should be taken as the larger of:

- That resulting from the design truck alone, or
- That resulting from 25 percent of the design truck taken together with the design lane load.

According to S2.5.2.6.2, the deflection criteria for vehicular live load limits deflection to L/800.
$110(12) / 800=1.65 \mathrm{in}$.
The calculated live load deflection determined by using computer software is 0.324 in .
0.324 in. < 1.65 in. OK

## Design Step

SHEAR DESIGN
5.7
(S5.8)
Shear design in the AASHTO-LRFD Specifications is based on the modified compression field theory. This method takes into account the effect of the axial force on the shear behavior of the section. The angle of the shear cracking, ?, and the shear constant, $\beta$, are both functions of the level of applied shear stress and the axial strain of the section. Figure S5.8.3.4.2-1 (reproduced below) illustrates the shear parameters.


Figure S5.8.3.4.2-1 - Illustration of Shear Parameters for Section Containing at Least the Minimum Amount of Transverse Reinforcement, $\mathbf{V}_{\mathbf{p}}=0$.

The transverse reinforcement (stirrups) along the beam is shown in Figure 5.7-1. Table 5.7-1 lists the variables required to be calculated at several sections along the beam for shear analysis.

A sample calculation for shear at several sections follows the table.
Notice that many equations contain the term $V_{p}$, the vertical component of the prestressing force. Since draped strands do not exist in the example beams, the value of $V_{p}$ is taken as 0.

Table 5.7-1 Shear Analysis at Different Sections

| Dist. ${ }^{(1)}$ | $A_{p s}$ | $\mathrm{As}^{(3)}$ | CGS ${ }^{(4)}$ | $\mathrm{d}^{(5)}$ | c <br> (Rectangular behavior) ${ }^{(6)}$ | c (T-section behavior) (7) | $\begin{gathered} d_{e}- \\ \beta_{1} c / 2 \end{gathered}$ | 0.9de | $\mathrm{dv}^{(8)}$ | $\mathrm{V}_{u}{ }^{(9)}$ | $V_{p}{ }^{(9,10)}$ | $\mathrm{V}_{(11)} / \mathrm{f}^{\prime}{ }^{\text {c }}$ | $M_{u}{ }^{(9,12)}$ | $M_{u} / d_{v}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (ft.) | (in ${ }^{2}$ ) | (in ${ }^{2}$ ) | (in.) | (in.) | (in.) | (in.) | (in.) | (in.) | (in.) | (kips) | (kips) |  | (kip-ft) | (kips) |
| 7.00 | 4.90 |  | 5.375 | 74.13 | 4.06 | \#N/A | 72.40 | 66.71 | 72.40 | 340.4 | 0.00 | 0.1088 | 2,241 | 371.4 |
| 11.00 | 5.26 |  | 5.279 | 74.22 | 4.35 | \#N/A | 72.37 | 66.80 | 72.37 | 315.1 | 0.00 | 0.1008 | 3,393 | 562.6 |
| 16.50 | 5.81 |  | 5.158 | 74.34 | 4.80 | \#N/A | 72.30 | 66.91 | 72.30 | 280.7 | 0.00 | 0.0899 | 4,755 | 789.2 |
| 22.00 | 5.81 |  | 5.158 | 74.34 | 4.80 | \#N/A | 72.14 | 66.91 | 72.14 | 246.7 | 0.00 | 0.0790 | 5,897 | 978.7 |
| 27.50 | 6.73 |  | 5.000 | 74.50 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 213.4 | 0.00 | 0.0685 | 6,821 | 1,134.6 |
| 33.00 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 180.6 | 0.00 | 0.0579 | 7,535 | 1,253.3 |
| 38.50 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 148.3 | 0.00 | 0.0476 | 8,063 | 1,341.2 |
| 44.00 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 116.7 | 0.00 | 0.0374 | 8,381 | 1,394.1 |
| 49.50 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 85.7 | 0.00 | 0.0275 | 8,494 | 1,412.9 |
| 54.50 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 118.4 | 0.00 | 0.0380 | 8,456 | 1,406.5 |
| 55.00 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 121.3 | 0.00 | 0.0389 | 8,440 | 1,403.9 |
| 60.50 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 153.5 | 0.00 | 0.0492 | 8,163 | 1,357.8 |
| 66.00 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 185.7 | 0.00 | 0.0596 | 7,690 | 1,279.1 |
| 71.50 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 217.9 | 0.00 | 0.0699 | 7,027 | 1,168.8 |
| 77.00 | 6.73 |  | 5.000 | 68.37 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 250.0 | 0.00 | 0.0802 | 6,180 | 1,028.0 |
| 82.50 | 6.73 |  | 5.000 | 74.50 | 5.55 | \#N/A | 72.14 | 67.05 | 72.14 | 282.0 | 0.00 | 0.0905 | 5,158 | 858.0 |
| 88.00 | 5.81 |  | 5.158 | 74.34 | 4.80 | \#N/A | 72.30 | 66.91 | 72.30 | 313.8 | 0.00 | 0.1005 | 3,966 | 658.2 |
| 93.50 | $5.81{ }^{(2)}$ | 14.65 | 5.158 | 75.52 | 8.21 | \#N/A | 72.44 | 67.97 | 72.44 | 345.4 | 0.00 | 0.1104 | -393 | 65.1 |
| 99.00 | $4.90{ }^{(2)}$ | 14.65 | 5.375 | 75.52 | 8.21 | \#N/A | 72.44 | 67.97 | 72.44 | 376.8 | 0.00 | 0.1204 | -1,535 | 254.3 |
| 102.50 | $4.90{ }^{(2)}$ | 14.65 | 5.375 | 75.52 | 8.21 | \#N/A | 72.44 | 69.97 | 72.44 | 396.6 | 0.00 | 0.1267 | -2,489 | 412.3 |


| Dist. |  | $\underset{\substack{\text { (guess) } \\(14)}}{ }$ | $\begin{array}{\|c} 0.5\left(V_{u}\right. \\ \left.V_{p}\right) \\ \cot \theta \end{array}$ | Net Force | $\varepsilon_{x}{ }^{(15)}$ | $\underset{\varepsilon_{x}}{\text { Adjusted }}$ | $\underset{(17)}{\theta} \underset{(\underset{\text { comp. }}{ }}{ }$ | $\beta^{(17)}$ | $\mathrm{V}_{\mathrm{c}}$ | Max. Stirrup Spcg. | $\begin{gathered} \mathrm{V}_{\mathrm{s}} \\ \text { (comp.) } \end{gathered}$ | $\phi \mathbf{V}_{\mathrm{n}}$ | $\phi \mathbf{V}_{\mathbf{n}} / \mathbf{V}_{\mathbf{u}}$ | $\mathrm{T}^{(18)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (ft.) | (kips) |  | (kips) | (kips) | (strain) | (strain) |  |  | (kips) | (in.) | (kips) | (kips) |  | (kips) |
| 7.00 | 926.1 | 22.60 | 408.9 | -145.8 | -0.000520 | -0.000026 | 22.60 | 3.05 | 136.7 | 16.0 | 260.9 | 307.8 | 1.051 | 967 |
| 11.00 | 994.1 | 22.80 | 374.8 | -56.7 | -0.000190 | -0.000010 | 22.80 | 3.07 | 137.6 | 18.0 | 229.5 | 317.3 | 1.049 | 1,123 |
| 16.50 | 1,098.1 | 22.33 | 341.7 | 32.8 | 0.000100 | 0.000100 | 24.75 | 2.99 | 133.9 | 21.0 | 179.2 | 305.6 | 1.004 | 1,272 |
| 22.00 | 1,098.1 | 28.66 | 225.7 | 106.3 | 0.000320 | 0.000320 | 28.66 | 2.74 | 122.7 | 20.0 | 158.7 | 311.1 | 1.027 | 1,335 |
| 27.50 | 1,272.0 | 26.03 | 218.4 | 81.0 | 0.000210 | 0.000210 | 26.03 | 3.02 | 134.9 | 24.0 | 147.7 | 329.0 | 1.192 | 1,469 |
| 33.00 | 1,272.0 | 28.55 | 165.9 | 147.2 | 0.000380 | 0.000380 | 29.53 | 2.68 | 119.7 | 24.0 | 127.4 | 321.2 | 1.232 | 1,495 |
| 38.50 | 1,272.0 | 31.30 | 122.0 | 191.2 | 0.000500 | 0.000500 | 31.30 | 2.54 | 113.5 | 24.0 | 118.7 | 317.7 | 1.409 | 1,515 |
| 44.00 | 1,272.0 | 31.30 | 96.0 | 218.1 | 0.000570 | 0.000570 | 32.10 | 2.49 | 111.2 | 24.0 | 115.0 | 316.8 | 1.744 | 1,509 |
| 49.50 | 1,272.0 | 31.30 | 70.5 | 211.4 | 0.000550 | 0.000550 | 31.30 | 2.54 | 113.5 | 24.0 | 118.7 | 318.1 | 2.438 | 1,472 |
| 54.50 | 1,272.0 | 32.10 | 94.4 | 228.9 | 0.000600 | 0.000600 | 32.10 | 2.49 | 111.2 | 24.0 | 115.0 | 315.8 | 1.720 | 1,525 |
| 55.00 | 1,272.0 | 32.10 | 96.7 | 228.6 | 0.000600 | 0.000600 | 32.10 | 2.49 | 111.2 | 24.0 | 115.0 | 315.8 | 1.678 | 1,527 |
| 60.50 | 1,272.0 | 31.30 | 126.2 | 212.0 | 0.000550 | 0.000550 | 31.30 | 2.54 | 113.5 | 24.0 | 118.7 | 316.2 | 1.362 | 1,541 |
| 66.00 | 1,272.0 | 29.53 | 163.9 | 171.0 | 0.000450 | 0.000450 | 30.50 | 2.59 | 115.7 | 24.0 | 122.5 | 318.8 | 1.155 | 1,526 |
| 71.50 | 1,272.0 | 27.28 | 208.5 | 105.3 | 0.000270 | 0.000270 | 27.85 | 2.85 | 127.3 | 24.0 | 138.1 | 238.9 | 1.097 | 1,500 |
| 77.00 | 1,272.0 | 23.83 | 283.0 | 39.0 | 0.000100 | 0.000100 | 24.45 | 3.16 | 141.2 | 24.0 | 158.7 | 269.9 | 1.080 | 1,465 |
| 82.50 | 1,272.0 | 22.33 | 343.2 | -70.8 | -0.000180 | -0.000012 | 22.33 | 3.29 | 147.0 | 21.0 | 175.6 | 290.3 | 1.030 | 1,407 |
| 88.00 | 1,098.1 | 22.80 | 373.2 | -66.7 | -0.000200 | -0.000012 | 22.80 | 3.07 | 137.4 | 19.0 | 217.3 | 319.2 | 1.017 | 1,229 |
| 93.50 | 1,098.1 ${ }^{1}$ | 30.20 | 296.7 | 361.8 | 0.000430 | 0.000430 | 30.20 | 2.56 | 114.8 | 11.0 | 271.6 | 347.8 | 1.007 | \#N/A |
| 99.00 | $926.1^{(2)}$ | 33.65 | 283.0 | 537.3 | 0.000630 | 0.000630 | 33.65 | 2.30 | 103.2 | 8.0 | 326.5 | 386.7 | 1.026 | \#N/A |
| 102.50 | $926.1^{(2)}$ | 35.17 | 281.4 | 693.7 | 0.000820 | 0.000820 | 35.81 | 2.19 | 98.2 | 7.0 | 344.3 | 398.3 | 1.004 | \#N/A |

## Notes:

(1) Distance measured from the centerline of the end support. Calculations for Span 1 are shown. From symmetry, Span 2 is a mirror image of Span 1.
(2) Prestressing steel is on the compression side of the section in the negative moment region of the girder (intermediate pier region). This prestressing steel is ignored where the area of steel in an equation is defined as the area of steel on the tension side of the section.
(3) Area of continuity reinforcement, i.e., the longitudinal reinforcement of the deck slab within the effective flange width of the girder in the girder negative moment region.
(4) Distance from the centroid of the tension steel reinforcement to the extreme tension fiber of the section. In the positive moment region, this is the distance from the centroid of prestressing strands to the bottom of the prestressed beam. In the negative moment region, this is the distance from the centroid of the longitudinal deck slab reinforcement to the top of the structural deck slab (ignore the thickness of the integral wearing surface).
(5) Effective depth of the section equals the distance from the centroid of the tension steel reinforcement to the extreme compression fiber of the section. In the positive moment region, this is the distance from the centroid of the prestressing strands to the top of the structural deck slab (ignore the thickness of the integral wearing surface). In the negative moment region, this is the distance from the centroid of the longitudinal deck slab reinforcement the bottom of the prestressed beam. The effective depth is calculated as the total depth of the section (which equals the depth of precast section, $72 \mathrm{in} .+$ structural deck thickness, $7.5 \mathrm{in} .=79.5 \mathrm{in}$.) minus the quantity defined in note (4) above.
(6) Distance from the extreme compression fiber to the neutral axis calculated assuming rectangular behavior using Eq. S5.7.3.1.1-4. Prestressing steel, effective width of slab and slab compressive strength are considered in the positive moment region. The slab longitudinal reinforcement, width of the girder bottom (compression) flange and girder concrete strength are considered in the negative moment region.
(7) Distance from the extreme compression fiber to the neutral axis calculated assuming T-section behavior using Eq. S5.7.3.1.1-3. Only applicable if the rectangular section behavior proves untrue.
(8) Effective depth for shear calculated using S5.8.2.9.
(9) Maximum applied factored load effects obtained from the beam load analysis.
(10) Vertical component of prestressing which is 0.0 for straight strands
(11) The applied shear stress, $\mathrm{v}_{\mathrm{u}}$, calculated as the applied factored shear force divided by product of multiplying the web width and the effective shear depth.
(12) Only the controlling case (positive moment or negative moment) is shown.
(13) In the positive moment region, the parameter $f_{p o}$ is taken equal to $0.7 \mathrm{f}_{\mathrm{pu}}$ of the prestressing steel as allowed by S5.8.3.4.2. This value is reduced within the transfer length of the strands to account for the lack of full development.
(14) Starting (assumed) value of shear crack inclination angle, $\theta$, used to determine the parameter $\varepsilon_{x}$.
(15) Value of the parameter $\varepsilon_{\mathrm{x}}$ calculated using Eq. S5.8.3.4.2-1 which assumes that $\varepsilon_{\mathrm{x}}$ has a positive value.
(16) Value of the parameter $\varepsilon_{\mathrm{x}}$ recalculated using Eq. S5.8.3.4.2-3 when the value calculated using Eq. S5.8.3.4.2-1 is a negative value.
(17) Value of $\theta$ and $\beta$ determined from Table S5.8.3.4.2-1 using the calculated value of $\varepsilon_{\mathrm{x}}$ and $v_{u} / f^{\prime}{ }_{c}$. These values are determined using a step function to interpolate between the values in Table S5.8.3.4.2-1.
(18) Force in longitudinal reinforcement including the effect of the applied shear (S5.8.3.5)

## Design Step 5.7.1

# Critical section for shear near the end support 

According to S5.8.3.2, where the reaction force in the direction of the applied shear introduces compression into the end region of a member, the location of the critical section for shear is taken as the larger of $0.5 d_{v} \cot \theta$ or $d_{v}$ from the internal face of the
support ( $d_{v}$ and $\theta$ are measured at the critical section for shear). This requires the designer to estimate the location of the critical section first to be able to determine $d_{v}$ and $\theta$, so a more accurate location of the critical section may be determined.

Based on a preliminary analysis, the critical section near the end support is estimated to be at a distance 7.0 ft . from the centerline of the end bearing. This distance is used for analysis and will be reconfirmed after determining $\mathrm{d}_{\mathrm{v}}$ and $\theta$.

## Design Step <br> 5.7.2

Design Step
Shear analysis for a section in the positive moment region
Sample Calculations: Section 7.0 ft. from the centerline of the end bearing
Determine the effective depth for shear, $\mathrm{d}_{\mathrm{v}}$
$d_{v}=$ effective shear depth taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken to be less than the greater of $0.9 \mathrm{~d}_{\mathrm{e}}$ or 0.72 h (S5.8.2.9)
h = total depth of beam (in.)
$=$ depth of the precast beam + structural slab thickness
$=72+7.5=79.5 \mathrm{in}$. (notice that the depth of the haunch was ignored in this calculation)
$\mathrm{d}_{\mathrm{e}}=$ distance from the extreme compression fiber to the center of the prestressing steel at the section (in.). From Figure 2-6,
$=79.5-5.375=74.125 \mathrm{in}$.
Assuming rectangular section behavior with no compression steel or mild tension reinforcement, the distance from the extreme compression fiber to the neutral axis, c, may be calculated as:

$$
\begin{align*}
\mathrm{c} & =\mathrm{A}_{\mathrm{ps}} \mathrm{f}_{\mathrm{pu}} /\left[0.85 \mathrm{f}_{\mathrm{c}} \beta_{1} \mathrm{~b}+\mathrm{kA} \mathrm{ps}\left(\mathrm{f}_{\mathrm{pu}} / \mathrm{d}_{\mathrm{p}}\right)\right]  \tag{S5.7.3.1}\\
\beta_{1} & =0.85 \text { for } 4 \text { ksi slab concrete }  \tag{S5.7.2.2}\\
\mathrm{b} & =\text { effective flange width } \\
& =111 \text { in. (calculated in Section } 2.2)
\end{align*}
$$

Area of prestressing steel at the section $=32(0.153)=4.896 \mathrm{in}^{2}$

$$
\begin{aligned}
\mathrm{c}= & 4.896(270) /[0.85(4)(0.85)(111)+0.28(4.896)(270 / 74.125)] \\
= & 4.06 \text { in. }<\text { structural slab thickness }=7.5 \mathrm{in} . \\
& \text { The assumption of the section behaving as a rectangular section is correct. }
\end{aligned}
$$

Depth of compression block, $a=\beta_{1} c=0.85(4.06)=3.45 \mathrm{in}$.
Distance between the resultants of the tensile and compressive forces due to flexure:

$$
\begin{align*}
& =\mathrm{d}_{\mathrm{e}}-\mathrm{a} / 2 \\
& =74.125-3.45 / 2 \\
& =72.4 \mathrm{in} .  \tag{1}\\
0.9 \mathrm{~d}_{\mathrm{e}} & =0.9(74.125) \\
& =66.71 \mathrm{in} .  \tag{2}\\
0.72 \mathrm{~h} & =0.72(79.5) \\
& =57.24 \mathrm{in} .  \tag{3}\\
\mathrm{d}_{\mathrm{v}} & =\text { largest of }(1),(2) \text { and }(3)=72.4 \mathrm{in} .
\end{align*}
$$

Notice that 0.72 h is always less than the other two values for all sections of this beam. This value is not shown in Table 5.7-1 for clarity.

## Design Step

5.7.2.2

Shear stress on concrete
From Table 5.3-4, the factored shear stress at this section, $\mathrm{V}_{\mathrm{u}}=340.4 \mathrm{kips}$
$\varphi=$ resistance factor for shear is 0.9
$b_{v}=$ width of web $=8 \mathrm{in}$. (see S5.8.2.9 for the manner in which $b_{v}$ is determined for sections with post-tensioning ducts and for circular sections)

From Article S5.8.2.9, the shear stress on the concrete is calculated as:

$$
\begin{align*}
\mathrm{v}_{\mathrm{u}} & =\left(\mathrm{V}_{\mathrm{u}}-\varphi \mathrm{V}_{\mathrm{p}}\right) /\left(\varphi \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}}\right)  \tag{S5.8.2.9-1}\\
& =(340.4-0) /[0.9(8)(72.4)] \\
& =0.653 \mathrm{ksi}
\end{align*}
$$

Ratio of applied factored shear stress to concrete compressive strength:

$$
\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}}^{\prime}=0.653 / 6.0=0.1088
$$

Minimum required transverse reinforcement
5.7.2.3

Limits on maximum factored shear stresses for sections without transverse reinforcement are presented in S5.8.2.4. Traditionally, transverse reinforcement satisfying the minimum transverse reinforcement requirements of S5.8.2.5 is provided along the full length of the beam.

Minimum transverse reinforcement, $\mathrm{A}_{\mathrm{v}}$ :

$$
\begin{aligned}
& A_{v} \geq 0.0316 \sqrt{f^{\prime}}{ }_{c} \frac{b_{v} s}{f_{y}} \\
& f_{c}^{\prime}=\text { compressive strength of the web concrete }=6.0 \mathrm{ksi} \\
& f_{y}=\text { yield strength of the transverse reinforcement }=60 \mathrm{ksi}
\end{aligned}
$$

Assume that \#4 bars are used for the stirrups. $\mathrm{A}_{\mathrm{v}}=$ area of 2 legs of a \#4 bar = $0.4 \mathrm{in}^{2}$ Substitute $0.4 \mathrm{in}^{2}$ to determine " s ", the maximum allowable spacing of \#4 bars (2-leg stirrups).

$$
\begin{aligned}
& 0.4 \geq 0.0316(2.449)(8 / 60) \mathrm{s} \\
& \mathrm{~s} \quad \leq 38.77 \mathrm{in} .
\end{aligned}
$$

## Design Step

5.7.2.4

The maximum spacing of transverse reinforcement is determined in accordance with S5.8.2.7. Depending on the level of applied factored shear stress, $\mathrm{v}_{\mathrm{u}}$, the maximum permitted spacing, $\mathrm{s}_{\text {max }}$, is determined as:

- If $\mathrm{v}_{\mathrm{u}}<0.125 f^{\prime}$, then:

$$
\begin{equation*}
\mathrm{s}_{\max }=0.8 \mathrm{~d}_{\mathrm{v}}<24.0 \mathrm{in} . \tag{S5.8.2.7-1}
\end{equation*}
$$

- If $v_{u} \geq 0.125 f^{\prime}$, then:

$$
\begin{equation*}
\mathrm{s}_{\max }=0.4 \mathrm{~d}_{\mathrm{v}}<12.0 \mathrm{in} . \tag{S5.8.2.7-2}
\end{equation*}
$$

For the section under consideration, $v_{u}=0.1088 f^{\prime}{ }_{c}$. Therefore, the maximum permitted spacing,

$$
\begin{aligned}
\mathrm{s}_{\max } & =0.8 \mathrm{~d}_{\mathrm{v}} \\
& =0.8(72.4) \\
& =57.9 \mathrm{in} .>24.0 \mathrm{in} . \mathrm{NG}, \begin{array}{l}
\text { assume maximum permitted stirrup } \\
\text { spacing }=24 \mathrm{in} .
\end{array}
\end{aligned}
$$

## Design Step

5.7.2.5

Shear strength
The shear strength provided by the concrete, $V_{c}$, is calculated using the following equation:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \tag{S5.8.3.3-3}
\end{equation*}
$$

The values of $\beta$ and the shear cracking inclination angle, $\theta$, are determined using the procedure outlined in S5.8.3.4.2. This iterative procedure begins with assuming a value of the parameter $\varepsilon_{x}$, or the crack inclination angle $\theta$, then calculating a new $\varepsilon_{x}$ value which is subsequently compared to the assumed value.

If the two values match, or the assumed value is slightly greater than the calculated value, no further iterations are required. Otherwise, a new cycle of analysis is conducted using the calculated value.

The calculations shown below are based on assuming a value of the crack inclination angle $\theta$.

The flowcharts in Section 3 include two for shear analysis. The first flowchart is based on assuming the analyses are based on an assumed value of $\theta$ and the second flowchart is based on an assumed value of $\varepsilon_{x}$.

The parameter $\varepsilon_{x}$ is a measure of the strain in the concrete on the tension side of the section. For sections containing at least the minimum transverse reinforcement calculated above, $\varepsilon_{x}$ may be calculated using the following equations:

$$
\begin{equation*}
\varepsilon_{x}=\frac{\left(\frac{M_{u}}{d_{v}}+0.5 N_{u}+0.5\left(V_{u}-V_{p}\right) \cot ?-A_{p s} f_{p o}\right)}{2\left(E_{s} A_{s}+E_{p s} A_{p s}\right)} \leq 0.002 \tag{S5.8.3.4.2-1}
\end{equation*}
$$

If the value of $\varepsilon_{x}$ from Eqs. S5.8.3.4.2-1 or -2 is negative, the strain shall be taken as:

$$
\begin{equation*}
\varepsilon_{x}=\frac{\left(\frac{M_{u}}{d_{v}}+0.5 N_{u}+0.5\left(V_{u}-V_{p}\right) \cot ?-A_{p s} f_{p o}\right)}{2\left(E_{c} A_{c}+E_{s} A_{s}+E_{p s} A_{p s}\right)} \tag{S5.8.3.4.2-3}
\end{equation*}
$$

For this example, the value of both the applied factored axial load, $\mathrm{N}_{\mathrm{u}}$, and the vertical component of prestressing, $\mathrm{V}_{\mathrm{p}}$, are taken equal to 0 .

For the section under consideration:

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{u}}=\text { maximum applied factored shear }=340.4 \mathrm{kips} \\
& \mathrm{M}_{\mathrm{u}}=\text { maximum factored moment at the section }=2,241 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Notice that the maximum live load moment and the maximum live load shear at any section are likely to result from two different locations of the load along the length of the bridge. Conducting the shear analysis using the maximum factored shear and the concurrent factored moment is permitted. However, most computer programs list the
maximum values of the moment and the maximum value of the shear without listing the concurrent forces. Therefore, hand calculations and most design computer programs typically conduct shear analysis using the maximum moment value instead of the moment concurrent with the maximum shear. This results in a conservative answer.

According to S5.8.3.4.2, $f_{p o}$ is defined as follows:
$f_{p o}=a$ parameter taken as the modulus of elasticity of the prestressing tendons multiplied by the locked in difference in strain between the prestressing tendons and the surrounding concrete (ksi). For the usual levels of prestressing, a value of $0.7 f_{p u}$ will be appropriate for both pretensioned and posttensioned members.

For pretensioned members, multiplying the modulus of elasticity of the prestressing tendons by the locked in difference in strain between the prestressing tendons and the surrounding concrete yields the stress in the strands when the concrete is poured around them, i.e., the stress in the strands immediately prior to transfer. For pretensioned members, SC5.8.3.4.2 allows $f_{p o}$ to be taken equal to the jacking stress. This value is typically larger than $0.7 f_{p u}$. Therefore, using $0.7 f_{p u}$ is more conservative since it results in a larger value of $\varepsilon_{x}$.

For this example, $\mathrm{f}_{\mathrm{po}}$ is taken as $0.7 \mathrm{f}_{\mathrm{pu}}$
Notice that, as required by Article S5.8.3.4.2, within the transfer length, $f_{p o}$ shall be increased linearly from zero at the location where the bond between the strands and concrete commences to its full value at the end of the transfer length.

Assume that $\theta=23.0$ degrees (this value is based on an earlier cycle of calculations).

$$
\begin{aligned}
\mathrm{A}_{\mathrm{ps}} & =\text { area of prestressed steel at the section } \\
& =32(0.153) \\
& =4.896 \mathrm{in}^{2} \\
\mathrm{~d}_{\mathrm{v}} & =72.4 \mathrm{in} .(6.03 \mathrm{ft} .)
\end{aligned}
$$

$A_{s}, E_{s}, A_{p s}$ and $E_{p s}$ are the area of mild tension reinforcement (0.0), modulus of elasticity of mild reinforcement ( $29,000 \mathrm{ksi}$ ), area of prestressing steel ( $4.896 \mathrm{in}^{2}$ ) and modulus of elasticity of the prestressing strands ( $28,500 \mathrm{ksi}$ ), respectively.

Substitute these variables in Eq. S5.8.3.4.2-1 and recalculate $\varepsilon_{\mathrm{x}}$.

$$
\varepsilon_{\mathrm{x}}=-0.00055<0.0 \mathrm{NG} \text {, therefore, use Eq. S5.8.3.4.2-3 }
$$

The area of the concrete on the tension side of the beam is taken as the area of concrete on the tension side of the beam within half the total depth of the beam.

$$
\mathrm{H} / 2=\text { one half of the total composite beam depth }=79.5 / 2=39.75 \mathrm{in} .
$$

From Figure S5.8.3.4.2-1 (reproduced above), the concrete area on the tension side, the lower 39.75 in . of the beam, equals $578 \mathrm{in}^{2}$.

Modulus of elasticity of the beam concrete, $\mathrm{E}_{\mathrm{c}}=33,000 \mathrm{w}_{\mathrm{c}}^{1.5} \sqrt{\mathrm{f}^{\prime}{ }_{\mathrm{c}}}=4,696 \mathrm{ksi}$
Substitute these variables in Eq. S5.8.3.4.2-3 and recalculate $\varepsilon_{\mathrm{x}}$.

$$
\varepsilon_{\mathrm{x}}=-0.000027
$$

At the section under consideration $v_{\mathrm{u}} / \mathrm{f}^{\prime}{ }_{\mathrm{c}}=0.1088$ (from Design Step 5.7.2.2 above)
Table S5.8.3.4.2-1 is reproduced below. This table is used to determine the value of $\theta$ and $\beta$ at different sections.

Notice that:

- Linear interpolation between the rows of the table is permitted to account for the value of $v_{u} / f^{\prime}{ }_{c}$ at the section
- Linear interpolation between the columns of the table is allowed to account for the calculated value of $\varepsilon_{x}$
- In lieu of interpolating, using values of $\theta$ and $\beta$ from a cell that correspond to the values of $v_{l} / f^{\prime}{ }_{c}$ and $\varepsilon_{x}$ greater than the calculated values is permitted. This approach is preferred for hand calculations and will result in a conservative answer.

Using Table S5.8.3.4.2-1 for the above values of $\varepsilon_{\mathrm{x}}$ and $\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}}$ :
Use the row that corresponds to $\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}} \leq 0.125$ (this value is next greatest to the calculated value of $v_{u} / f_{c}$ )

Use the column corresponding to $\varepsilon_{\mathrm{x}} \leq 0.0$ (the value in Table S5.8.3.4.2-1 that is next larger to the assumed value of $\varepsilon_{\mathrm{x}}$ )

$$
\begin{aligned}
\theta & =23.7 \text { degrees } \\
\beta & =2.87
\end{aligned}
$$

Check the assumed value of $\theta$ :
For the purpose of calculating $\varepsilon_{\mathrm{x}}$, the value of $\theta$ was assumed to be 23.0 degrees. This value is close to the value obtained above. Therefore, the assumed value of $\theta$ was appropriate and there is no need for another cycle of calculations.

Notice that the assumed and calculated values of $\theta$ do not need to have the same exact value. A small difference will not drastically affect the outcome of the analysis and, therefore, does not warrant conducting another cycle of calculations. The assumed value may be accepted if it is larger than the calculated value.

Notice that the values in Table 5.7-1 are slightly different (22.60 and 3.05). This is true since the spreadsheet used to determine the table values uses a step function instead of linear interpolation.

Calculate the shear resistance provided by the concrete, $\mathrm{V}_{\mathrm{c}}$.

$$
\begin{align*}
& \mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{{ }_{\mathrm{C}}^{\mathrm{b}}} \mathrm{~d}_{\mathrm{v}}  \tag{S5.8.3.3-3}\\
& \mathrm{~V}_{\mathrm{c}}=0.0316(2.87)(2.449)(8)(72.4)=128.6 \mathrm{k}
\end{align*}
$$

Calculate the shear resistance provided by the transverse reinforcement (stirrups), $\mathrm{V}_{\mathrm{s}}$.

$$
\begin{equation*}
\mathrm{V}_{\mathrm{s}}=\left[\mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{~d}_{\mathrm{v}}(\cot \theta+\cot \alpha) \sin \alpha\right] / \mathrm{s} \tag{S5.8.3.3-4}
\end{equation*}
$$

Assuming the stirrups are placed perpendicular to the beam longitudinal axis at 16 in . spacing and are comprised of \#4 bars, each having two legs:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{v}} & =\text { area of shear reinforcement within a distance "s" }\left(\mathrm{in}^{2}\right) \\
& =2(\operatorname{area} \text { of \#4 bar) } \\
& =2(0.2) \\
& =0.4 \mathrm{in}^{2} \\
\mathrm{~s} & =16 \mathrm{in} . \\
\alpha & =\text { angle between the stirrups and the longitudinal axis of the beam } \\
& =90 \text { degrees } \\
\mathrm{V}_{\mathrm{s}} & =[0.4(60)(72.4)(\cot 23.0)] / 16=255.8 \mathrm{k}
\end{aligned}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is determined as the lesser of:

$$
\begin{align*}
& V_{\mathrm{n}}=\mathrm{V}_{\mathrm{c}}+\mathrm{V}_{\mathrm{s}}+\mathrm{V}_{\mathrm{p}}  \tag{S5.8.3.3-1}\\
& \mathrm{~V}_{\mathrm{n}}=0.25 f_{\mathrm{c}}^{\prime} \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}}+\mathrm{V}_{\mathrm{p}} \tag{S5.8.3.3-2}
\end{align*}
$$

Notice that the purpose of the limit imposed by Eq. S5.8.3.3-2 is intended to eliminate excessive shear cracking.
$\mathrm{V}_{\mathrm{p}}=0.0$ for straight strands
$\mathrm{V}_{\mathrm{n}}=$ lesser of:

$$
\mathrm{V}_{\mathrm{c}}+\mathrm{V}_{\mathrm{s}}+\mathrm{V}_{\mathrm{p}}=128.6+255.8+0.0=384.4 \mathrm{k}
$$

and

$$
0.25 f_{c}^{\prime} b_{v} d_{v}+V_{p}=0.25(6)(8)(72.4)+0.0=868.8 \mathrm{k}
$$

Therefore, $\mathrm{V}_{\mathrm{n}}=384.4 \mathrm{k}$
The resistance factor, $\varphi$, for shear in normal weight concrete is 0.9 (S5.5.4.2.1)

Shear factored resistance, $\mathrm{V}_{\mathrm{r}}$ :

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(384.4) \\
& =346.0 \mathrm{k}>\text { maximum applied factored shear, } \mathrm{V}_{\mathrm{u}}=340.4 \mathrm{k} \text { OK }
\end{aligned}
$$

Table S5.8.3.4.2-1 - Values of $\theta$ and $\beta$ for Sections with Transverse Reinforcement (Reproduced from the AASHTO-LRFD Specifications)

| $\mathrm{v} / \mathrm{f}_{\mathrm{c}}{ }^{\text {c }}$ | $\varepsilon_{\mathrm{x} \times 1,000}$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $=-0.20$ | $=-0.10$ | $=-0.05$ | $=0$ | $=0.125$ | $=0.25$ | $=0.50$ | $=0.75$ | $=1.00$ | $=1.50$ | $=2.00$ |
| $=0.075$ | 22.3 | 20.4 | 21.0 | 21.8 | 24.3 | 26.6 | 30.5 | 33.7 | 36.4 | 40.8 | 43.9 |
|  | 6.32 | 4.75 | 4.10 | 3.75 | 3.24 | 2.94 | 2.59 | 2.38 | 2.23 | 1.95 | 1.67 |
| $=0.100$ | 18.1 | 20.4 | 21.4 | 22.5 | 24.9 | 27.1 | 30.8 | 34.0 | 36.7 | 40.8 | 43.1 |
|  | 3.79 | 3.38 | 3.24 | 3.14 | 2.91 | 2.75 | 2.50 | 2.32 | 2.18 | 1.93 | 1.69 |
| $=0.125$ | 19.9 | 21.9 | 22.8 | 23.7 | 25.9 | 27.9 | 31.4 | 34.4 | 37.0 | 41.0 | 43.2 |
|  | 3.18 | 2.99 | 2.94 | 2.87 | 2.74 | 2.62 | 2.42 | 2.26 | 2.13 | 1.90 | 1.67 |
| $=0.150$ | 21.6 | 23.3 | 24.2 | 25.0 | 26.9 | 28.8 | 32.1 | 34.9 | 37.3 | 40.5 | 42.8 |
|  | 2.88 | 2.79 | 2.78 | 2.72 | 2.60 | 2.52 | 2.36 | 2.21 | 2.08 | 1.82 | 1.61 |
| $=0.175$ | 23.2 | 24.7 | 25.5 | 26.2 | 28.0 | 29.7 | 32.7 | 35.2 | 36.8 | 39.7 | 42.2 |
|  | 2.73 | 2.66 | 2.65 | 2.60 | 2.52 | 2.44 | 2.28 | 2.14 | 1.96 | 1.71 | 1.54 |
| $=0.200$ | 24.7 | 26.1 | 26.7 | 27.4 | 29.0 | 30.6 | 32.8 | 34.5 | 36.1 | 39.2 | 41.7 |
|  | 2.63 | 2.59 | 2.52 | 2.51 | 2.43 | 2.37 | 2.14 | 1.94 | 1.79 | 1.61 | 1.47 |
| $=0.225$ | 26.1 | 27.3 | 27.9 | 28.5 | 30.0 | 30.8 | 32.3 | 34.0 | 35.7 | 38.8 | 41.4 |
|  | 2.53 | 2.45 | 2.42 | 2.40 | 2.34 | 2.14 | 1.86 | 1.73 | 1.64 | 1.51 | 1.39 |
| $=0.250$ | 27.5 | 28.6 | 29.1 | 29.7 | 30.6 | 31.3 | 32.8 | 34.3 | 35.8 | 38.6 | 41.2 |
|  | 2.39 | 2.39 | 2.33 | 2.33 | 2.12 | 1.93 | 1.70 | 1.58 | 1.50 | 1.38 | 1.29 |

Check the location of the critical section for shear near the end support
According to S5.8.3.2, where the reaction force in the direction of the applied shear introduces compression into the end region of a member, the location of the critical section for shear shall be taken as the larger of $0.5 d_{v} \cot \theta$ or $d_{v}$ from the internal face of the support. For existing bridges, the width of the bearing is known and the distance is measured from the internal face of the bearings. For new bridges, the width of the
bearing is typically not known at this point of the design and one of the following two approaches may be used:

- Estimate the width of the bearing based on past experience.
- Measure the distance from the CL of bearing. This approach is slightly more conservative.

The second approach is used for this example.
For calculation purposes, the critical section for shear was assumed 7.0 ft . from the centerline of the bearing (see Design Step 5.7.1). The distance from the centerline of the support and the critical section for shear may be taken as the larger of $0.5 \mathrm{~d}_{\mathrm{v}} \cot \theta$ and $\mathrm{d}_{\mathrm{v}}$.

$$
\begin{aligned}
& 0.5 \mathrm{~d}_{\mathrm{v}} \cot \theta=0.5(72.4)(\cot 23.7)=82.5 \mathrm{in} .(6.875 \mathrm{ft} .) \\
& \mathrm{d}_{\mathrm{v}}=72.4 \mathrm{in} .(6.03 \mathrm{ft} .)
\end{aligned}
$$

The larger of $0.5 \mathrm{~d}_{\mathrm{v}} \cot \theta$ and $\mathrm{d}_{\mathrm{v}}$ is 82.5 in . ( 6.875 ft .)
The distance assumed in the analysis was 7.0 ft ., i.e., approximately 0.125 ft . ( $0.1 \%$ of the span length) further from the support than the calculated distance. Due to the relatively small distance between the assumed critical section location and the calculated section location, repeating the analysis based on the applied forces at the calculated location of the critical section is not warranted. In cases where the distance between the assumed location and the calculated location is large relative to the span length, another cycle of the analysis may be conducted taking into account the applied forces at the calculated location of the critical section.

## Design Step

The critical section for shear near the intermediate pier may be determined using the same procedure as shown in Design Steps 5.7.1 and 5.7.2 for a section near the end support. Calculations for a section in the negative moment region are illustrated below for the section at 99 ft . from the centerline of the end bearing. This section is not the critical section for shear and is used only for illustrating the design process.

## Sample Calculations: Section 99 ft . from the centerline of end bearings

## Design Step

Difference in shear analysis in the positive and negative moment regions
5.7.3.1

1) For the pier (negative moment) regions of precast simple span beams made continuous for live load, the prestressing steel near the piers is often in the compression side of the beam. The term $A_{p s}$ in the equations for $\varepsilon_{x}$ is defined as the area of prestressing steel on the tension side of the member. Since the
prestressing steel is on the compression side of the member, this steel is ignored in the analysis. This results in an increase in $\varepsilon_{x}$ and, therefore, a decrease in the shear resistance of the section. This approach gives conservative results and is appropriate for hand calculations.

A less conservative approach is to calculate $\varepsilon_{x}$ as the average longitudinal strain in the web. This requires the calculation of the strain at the top and bottom of the member at the section under consideration at the strength limit state. This approach is more appropriate for computer programs.

The difference between the two approaches is insignificant in terms of the cost of the beam. The first approach requires more shear reinforcement near the ends of the beam. The spacing of the stirrups in the middle portion of the beam is often controlled by the maximum spacing requirements and, hence, the same stirrup spacing is often required by both approaches.

It is beneficial to use the second approach in the following situations:

- Heavily loaded girders where the first approach results in congested shear reinforcement
- Analysis of existing structures where the first approach indicates a deficiency in shear resistance.

2) In calculating the distance from the neutral axis to the extreme compression fiber " $c$ ", the following factors need to be considered:

- The compression side is at the bottom of the beam. The concrete strength used to determine " $c$ " is that of the precast girder
- The width of the bottom flange of the beam is substituted for " $b$ ", the width of the member
- The area of the slab longitudinal reinforcement over the intermediate pier represents the reinforcement on the tension side of the member. The area and yield strength of this reinforcement should be determined in advance.

The first approach is used in this example.

## Design Step

5.7.3.2

Determine the effective depth for shear, $\mathrm{d}_{\underline{v}}$
$\mathrm{h}=72+7.5=79.5 \mathrm{in}$. (notice that the depth of the haunch was ignored in this calculation)

The center of gravity of the deck slab longitudinal reinforcement from the top of the structural thickness of the deck $=3.98$ in. (see Design Step 5.6.5.1)

$$
\mathrm{d}_{\mathrm{e}}=79.5-3.98=75.52 \mathrm{in} .
$$

The area of longitudinal slab reinforcement within the effective flange width of the beam is $14.65 \mathrm{in}^{2}$ (see Design Step 5.6.5.1)

Yield strength of the slab reinforcement $=60 \mathrm{ksi}$
Assuming rectangular section behavior with no compression or prestressing steel, the distance from the extreme compression fiber to the neutral axis, c , may be calculated as:

$$
\begin{equation*}
\mathrm{c}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} /\left(0.85 \mathrm{f}_{\mathrm{c}} \beta_{1} \mathrm{~b}\right) \tag{S5.7.3.1.1-4}
\end{equation*}
$$

where:
$\beta_{1}=0.75$ for 6 ksi beam concrete (S5.7.2.2)
$\mathrm{b}=$ precast beam bottom (compression) flange width (in.)
$=28 \mathrm{in}$.
$\mathrm{f}_{\mathrm{c}}^{\prime}=6 \mathrm{ksi}$
$\mathrm{c}=14.65(60) /[0.85(6)(0.75)(28)]$
$=8.21$ in. ${ }^{\sim}$ thickness of the beam bottom flange ( 8 in .)
Therefore, the assumption of the section behaving as a rectangular section is considered correct.

Notice that if the value of " $c$ " is significantly larger than the beam bottom flange thickness, a rectangular behavior may be used after adjusting the beam bottom flange width to account for the actual beam area in compression. However, if "c" is not significantly larger than the beam bottom flange thickness, the effect on the results will be minor and the analysis may be continued without adjusting the beam bottom flange width. This reasoning is used in this example.

Depth of compression block, $\mathrm{a}=\beta_{1} \mathrm{c}=0.75(8.21)=6.16 \mathrm{in}$.
Distance between the resultants of the tensile and compressive forces due to flexure:

$$
\begin{align*}
& =\mathrm{d}_{\mathrm{e}}-\mathrm{a} / 2 \\
& =75.52-6.16 / 2 \\
& =72.44 \mathrm{in} . \tag{1}
\end{align*}
$$

$$
\begin{align*}
0.9 \mathrm{~d}_{\mathrm{e}} & =0.9(75.52) \\
& =67.97 \mathrm{in} . \tag{2}
\end{align*}
$$

$$
\begin{align*}
0.72 \mathrm{~h} & =0.72(79.5) \\
& =57.24 \mathrm{in} . \tag{3}
\end{align*}
$$

$$
\mathrm{d}_{\mathrm{v}}=\text { largest of }(1),(2) \text { and }(3)=72.44 \mathrm{in.}
$$

Notice that 0.72 h is always less than the other two values for all sections of this beam. This value is not shown in Table 5.7-1 for clarity.

## Design Step <br> 5.7.3.3

From Table 5.3-4, the factored shear stress at this section, $\mathrm{V}_{\mathrm{u}}=376.8 \mathrm{kips}$

$$
\begin{align*}
& \varphi=0.9 \text { (shear) }  \tag{S5.5.4.2.1}\\
& \mathrm{b}_{\mathrm{v}}=\text { width of web }=8 \mathrm{in.}
\end{align*}
$$

From Article S5.8.2.9, the shear stress on the concrete is:

$$
\begin{aligned}
& \mathrm{v}_{\mathrm{u}}=\left(\mathrm{V}_{\mathrm{u}}-\varphi \mathrm{V}_{\mathrm{p}}\right) /\left(\varphi \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}}\right) \\
& \mathrm{v}_{\mathrm{u}}=(376.8-0) /[0.9(8)(72.44)]=0.722 \mathrm{ksi}
\end{aligned}
$$

Ratio of the applied factored shear stress to the concrete compressive strength:

$$
\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}}^{\prime}=0.722 / 6.0=0.1203
$$

## Design Step

5.7.3.4

Maximum allowable spacing for \#4 stirrups with two legs per stirrup was calculated in Design Step 5.7.2.2.
$\mathrm{s} \leq 38.77 \mathrm{in}$.

## Design Step

5.7.3.5

Minimum required transverse reinforcement

Maximum spacing for transverse reinforcement
The maximum spacing of transverse reinforcement is determined in accordance with S5.8.2.7. Depending on the level of applied factored shear stress, $\mathrm{v}_{\mathrm{u}}$, the maximum permitted spacing, $s_{\text {max }}$, is determined as:

- If $\mathrm{v}_{\mathrm{u}}<0.125 \mathrm{f}_{\mathrm{c}}{ }^{\prime}$, then:

$$
\begin{equation*}
\mathrm{s}_{\max }=0.8 \mathrm{~d}_{\mathrm{v}}<24.0 \mathrm{in} . \tag{S5.8.2.7-1}
\end{equation*}
$$

- If $v_{u} \geq 0.125 f_{c}^{\prime}$, then:

$$
\begin{equation*}
\mathrm{s}_{\max }=0.4 \mathrm{~d}_{\mathrm{v}}<12.0 \mathrm{in} . \tag{S5.8.2.7-2}
\end{equation*}
$$

For the section under consideration, $\mathrm{v}_{\mathrm{u}}=0.1203 \mathrm{f}^{\prime}{ }_{\mathrm{c}}$.

Therefore, the maximum permitted spacing,

$$
\begin{aligned}
\mathrm{s}_{\max } & =0.8 \mathrm{~d}_{\mathrm{v}} \\
& =0.8(72.44) \\
& =57.95 \mathrm{in} .>24.0 \mathrm{in} . \text { NG }
\end{aligned}
$$

Assume maximum permitted stirrup spacing $=24$ in.

## Design Step

5.7.3.6

Shear resistance
For sections in the negative moment region of the beam, calculate $\varepsilon_{x}$, using Eq. S5.8.3.4.2-1 and assume there is no prestressing steel.

$$
\begin{equation*}
\varepsilon_{x}=\frac{\left(\frac{M_{u}}{d_{v}}+0.5 N_{u}+0.5\left(V_{u}-V_{p}\right) \cot \theta-A_{p s} f_{p o}\right)}{2\left(E_{s} A_{s}+E_{p} A_{p s}\right)} \tag{S5.8.3.4.2-1}
\end{equation*}
$$

For this example, the value of both the applied factored axial load, $\mathrm{N}_{\mathrm{u}}$, and the vertical component of prestressing, $\mathrm{V}_{\mathrm{p}}$, are taken equal to 0 .

$$
\begin{aligned}
\mathrm{V}_{\mathrm{u}} & =\text { maximum applied factored shear from Table 5.3-4 } \\
& =376.8 \mathrm{kips}
\end{aligned}
$$

$\mathrm{M}_{\mathrm{u}}=$ maximum applied factored moment from Table 5.3-2
$=-1,535 \mathrm{k}-\mathrm{ft}$
Notice that the term $M_{u} / d_{v}$ represents the force in the tension reinforcement due to the applied factored moment. Therefore, $M_{u} / d_{v}$ is taken as a positive value regardless of the sign of the moment.

Assume that $\theta=35$ degrees

$$
\begin{aligned}
\mathrm{f}_{\mathrm{po}} & =0.0 \mathrm{ksi} \text { at this location (prestressing force ignored) } \\
\mathrm{A}_{\mathrm{s}} & =\text { area of longitudinal reinforcement in the deck at this section } \\
& =14.65 \mathrm{in}^{2}
\end{aligned}
$$

Notice that the area of deck longitudinal reinforcement used in this calculation is the area of the bars that extend at least one development length beyond the section under consideration. If the section lies within the development length of some bars, these bars may be conservatively ignored or the force in these bars be prorated based on the ratio between the full and available development length. Consideration should also be given to adjusting the location of the center of gravity of the reinforcement to account for the smaller force in the bars that are not fully developed.

$$
\begin{aligned}
& \mathrm{d}_{\mathrm{v}}=72.44 \mathrm{in} .(6.04 \mathrm{ft} .) \\
& \mathrm{E}_{\mathrm{s}}=29,000 \mathrm{ksi} \\
& \mathrm{E}_{\mathrm{ps}}=28,500 \mathrm{ksi} \\
& \begin{aligned}
\mathrm{A}_{\mathrm{ps}} & =\text { area of prestressing steel on the tension side of the member } \\
& =0.0 \mathrm{in}^{2}
\end{aligned}
\end{aligned}
$$

Substitute these variables in Eq. S5.8.3.4.2-1 to determine $\varepsilon_{\mathrm{x}}$ :

$$
\begin{aligned}
\varepsilon_{\mathrm{x}} & =[1,535(12) / 72.44+0.5(376.8-0) \cot 35-0] /[2(29,000)(14.65)+0] \\
& =0.00062
\end{aligned}
$$

At the section under consideration $v_{\mathrm{u}} / \mathrm{f}^{\prime}{ }_{\mathrm{c}}=0.1203$ (from Design Step 5.7.3.3)
Determine the values of $\theta$ and $\beta$ using Table S5.8.3.4.2-1 (reproduced above)
If no interpolation between the values in Table S5.8.3.4.2-1 is desired:
Use the row and column that have the closest headings, but still larger than the calculated values, i.e.:

Use the row that corresponds to $\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}} \leq 0.125$
Use the column corresponding to $\varepsilon_{\mathrm{x}} \leq 0.00075$

$$
\begin{aligned}
\theta & =34.4 \text { degrees } \\
\beta & =2.26
\end{aligned}
$$

If interpolation between the values in Table S5.8.3.4.2-1 is desired:
Interpolate between the values in the row with heading values closest to the calculated $\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}}^{\prime}=0.1203$, i.e., interpolate between the rows with headings of $\mathrm{v}_{\mathrm{u}} / \mathrm{f}_{\mathrm{c}}^{\prime} \leq 0.1$ and $\leq$ 0.125 . Then, interpolate between the values in the columns with heading values closest to the calculated $\varepsilon_{\mathrm{x}}=0.00062$, i.e., interpolate between the columns with headings of $\varepsilon_{\mathrm{x}} \leq$ 0.0005 and $\leq 0.00075$. The table below shows the relevant portion of Table S5.8.3.4.2-1 with the original and interpolated values. The shaded cells indicate interpolated values.

Excerpt from Table S5.8.3.4.2-1

| v/f ${ }_{\mathrm{c}}$ | $\varepsilon_{\mathrm{x}} \times 1,000$ |  |  |
| :--- | :---: | :---: | :---: |
|  | $=0.50$ | 0.62 | $=0.75$ |
| 0.100 | 30.8 |  | 34.0 |
|  | 2.50 |  | 2.32 |
| 0.1203 | 31.29 | 32.74 | 34.32 |
|  | 2.44 | 2.36 | 2.27 |
| $=0.125$ | 31.4 |  | 34.4 |
|  | 2.42 |  | 2.26 |

From the sub-table:

$$
\begin{aligned}
\theta & =32.74 \text { degrees } \\
\beta & =2.36
\end{aligned}
$$

Notice that the interpolated values are not significantly different from the ones calculated without interpolation. The analyses below are based on the interpolated values to provide the user with a reference for this process.

## Check the assumed value of $\theta$

For the purpose of calculating $\varepsilon_{\mathrm{x}}$, the value of $\theta$ was assumed to be 35 degrees. This value is close to the calculated value ( 32.74 degrees) and conducting another cycle of the analysis will not result in a significant difference. However, for the purpose of providing a complete reference, another cycle of calculations is provided below.

Assume that $\theta$ is the calculated value of 32.74 degrees
Substituting for the variables in Eq. S5.8.3.4.2-1for $\varepsilon_{\mathrm{x}}$ :

$$
\varepsilon_{\mathrm{x}}=0.00064
$$

Determine the values of $\theta$ and $\beta$ by interpolating the values in Table S5.8.3.4.2-1
$\theta=32.98$ degrees (almost equal to the assumed value, $\mathbf{O K}$ )
$\beta=2.34$
Notice that the values in Table 5.7-1 are slightly different (33.65 and 2.30). This is true since the spreadsheet used to determine the table values uses a step function instead of linear interpolation.

Calculate the shear resistance provided by concrete, $\mathrm{V}_{\mathrm{c}}$ :

$$
\begin{align*}
& \mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{{ }_{\mathrm{c}}^{\mathrm{b}}}{ }_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}}  \tag{S5.8.3.3-3}\\
& \mathrm{~V}_{\mathrm{c}}=0.0316(2.34)(2.449)(8)(72.44)=104.94 \mathrm{k}
\end{align*}
$$

Calculate the shear resistance provided by the transverse reinforcement (stirrups), $\mathrm{V}_{\mathrm{s}}$ :

$$
\begin{equation*}
\mathrm{V}_{\mathrm{s}}=\left[\mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{~d}_{\mathrm{v}}(\cot \theta+\cot \alpha) \sin \alpha\right] / \mathrm{s} \tag{S5.8.3.3-4}
\end{equation*}
$$

Assuming the stirrups are placed perpendicular to the beam longitudinal axis at 7 in . spacing and are comprised of \#4 bars, each having two legs:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{v}} & =2(\text { area of \#4 bar }) \\
& =2(0.2) \\
& =0.4 \mathrm{in}^{2} \\
\mathrm{~S} & =7 \mathrm{in} \\
\mathrm{a} & =90 \text { degrees } \\
\mathrm{V}_{\mathrm{s}} & =0.4(60)(72.44)(\cot 32.98) / 7=382.74 \mathrm{k}
\end{aligned}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is determined as the lesser of:

$$
\begin{align*}
& V_{n}=V_{c}+V_{s}+V_{p}  \tag{S5.8.3.3-1}\\
& V_{n}=0.25 f^{\prime}{ }_{c} b_{v} d_{v}+V_{p} \tag{S5.8.3.3-2}
\end{align*}
$$

Notice that the purpose of the limit imposed by Eq. S5.8.3.3-2 is intended to eliminate excessive shear cracking.

$$
V_{p}=0.0 \text { for straight strands }
$$

$\mathrm{V}_{\mathrm{n}}$ is taken as the lesser of:

$$
\begin{aligned}
& \quad V_{c}+V_{s}+V_{p}=104.94+382.74+0.0=487.68 \mathrm{k} \\
& \text { and } \\
& \qquad 0.25 f^{\prime} b_{v} d_{v}+V_{p}=0.25(6)(8)(72.44)+0.0=869.3 \mathrm{k}
\end{aligned}
$$

Therefore, $\mathrm{V}_{\mathrm{n}}=487.68 \mathrm{k}$
The resistance factor, $\varphi$, for shear in normal weight concrete $=0.90$ (S5.5.4.2.1)

Factored shear resistance:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(487.68) \\
& =438.91 \mathrm{k}>\text { max. applied factored shear, } \mathrm{V}_{\mathrm{u}}=376.8 \mathrm{k} \mathrm{OK}
\end{aligned}
$$

## Design Step <br> 5.7.4

Factored bursting resistance
(S5.10.10.1)
The bursting resistance of the pretensioned anchorage zones is calculated according to S5.10.10.1 at the service limit state.

$$
\begin{equation*}
P_{r}=f_{s} A_{s} \tag{S5.10.10.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
f_{s}= & \text { stress in the steel not exceeding } 20 \mathrm{ksi} \\
A_{s}= & \text { total area of vertical reinforcement located within the } \\
& \text { distance h/4 from the end of the beam }\left(\text { in }^{2}\right)
\end{aligned}
$$

The resistance shall not be less than $4 \%$ of the prestressing force at transfer.
From Design Step 5.4.4:

$$
\begin{aligned}
\text { Prestressing force at transfer at end of beam } & =32(0.153)(188.8) \\
& =924.4 \mathrm{kips}
\end{aligned}
$$

Determine the required area of steel to meet the minimum resistance using $\mathrm{f}_{\mathrm{s}}=20 \mathrm{ksi}$ (max).

Therefore,

$$
\begin{aligned}
0.04(924.4) & =20\left(\mathrm{~A}_{\mathrm{s}}\right) \\
\mathrm{A}_{\mathrm{s}} & =1.85 \mathrm{in}^{2}
\end{aligned}
$$

Since one stirrup is 0.4 in $^{2}$ (includes 2 legs), determine the number of stirrups required.

$$
1.85 / 0.4=4.63 \text { Say } 5 \text { stirrups required }
$$

These stirrups must fit within $\mathrm{h} / 4$ distance from the end of the beam.

$$
\begin{aligned}
\mathrm{h} / 4 & =72 / 4 \\
& =18 \mathrm{in} .
\end{aligned}
$$

Use 5 stirrups at 3 in. spacing as shown in Figure 5.7-1.

Design Step
5.7.5

Confinement reinforcement (S5.10.10.2)

For the distance of $1.5 d[1.5(72 / 12)=9$ ft.] from the end of the beam, reinforcement shall be placed to confine the prestressing steel in the bottom flange. The reinforcement is required to be not less than No. 3 deforming bars, with spacing not exceeding 6.0 in . and shaped to enclose the strands. The stirrups required to resist the applied shear and to satisfy the maximum stirrup requirements are listed in Table 5.7-1 for different sections. The maximum required spacings shown in Table 5.7-1 in the end zones of the beam is greater than 6 in . For a beam where all strands are located in the bottom flange, two different approaches may be utilized to provide the required confinement reinforcement:

1) Reduce the stirrup spacing in the end zone (1.5d) to not greater than 6 in.
2) Place the main vertical bars of the stirrups at the spacing required by vertical shear analysis. Detail the vertical bars in the bottom of the beam to enclose the prestressing and place these bars at a spacing not greater than 6 in. within the end zones. The stirrups and the confinement bars in this approach will not be at the same spacing and pouring of the concrete may be difficult.

For a beam where some strands are located in the web approach (1) should be used.
For this example, approach (1) was used. This is the basis for the stirrup distribution shown in Figure 5.7-1.



Figure 5.7-2 - Section A-A from Figure 5.7-1, Beam Cross Section Near the Girder Ends

Force in the longitudinal reinforcement including the effect of the applied shear (S5.8.3.5)

In addition to the applied moment, $M_{u}$, the following force effects contribute to the force in the longitudinal reinforcement:

- Applied shear forces, $V_{u}$
- Vertical component of the prestressing force
- Applied axial force, $N_{u}$
- The shear force resisted by the transverse reinforcement, $V_{s}$

To account for the effect of these force effects on the force in the longitudinal reinforcement, S5.8.3.5 requires that the longitudinal reinforcement be proportioned so that at each section, the tensile capacity of the reinforcement on the flexural tension side of the member, taking into account any lack of full development of that reinforcement, is greater than or equal to the force T calculated as:

$$
\begin{equation*}
T=\frac{M_{u}}{d_{\nu} \varphi}+0.5 \frac{N_{u}}{\varphi}+\left(\frac{V_{u}}{\varphi}-0.5 V_{s}-V_{p}\right) \cot \theta \tag{S5.8.3.5-1}
\end{equation*}
$$

where:
$V_{s}=$ shear resistance provided by the transverse reinforcement at the section under investigation as given by Eq. S5.8.3.3-4, except $V_{s}$ needs to be greater than $V_{u} / \varphi$ (kips)
$\theta=$ angle of inclination of diagonal compressive stresses used in determining the nominal shear resistance of the section under investigation as determined by S5.8.3.4 (deg)
$\varphi=$ resistance factors taken from S5.5.4.2 as appropriate for moment, shear and axial resistance

This check is required for sections located no less than a distance equal to $0.5 \mathrm{~d}_{\mathrm{v}} \cot \theta$ from the support. The values for the critical section for shear near the end support are substituted for $\mathrm{d}_{\mathrm{v}}$ and $\theta$.

$$
0.5(72.44) \cot 22.6=87.01 \mathrm{in} . \sim 7.0 \mathrm{ft} .
$$

The check for tension in the longitudinal reinforcement may be performed for sections no closer than 7.0 ft . from the support.
$\underline{\text { Sample calculation: Section at } 7.0 \mathrm{ft} \text {. from the centerline of bearing at the end support }}$
Using information from Table 5.7-1
Force in the longitudinal reinforcement at nominal flexural resistance, T

$$
\begin{aligned}
\mathrm{T} & =2,241(12) /[72.40(1.0)]+0+[(340.4 / 0.9)-0.5(260.9)-0] \cot 22.6 \\
& =966.7 \mathrm{kips}
\end{aligned}
$$

From Table 5.5-1, the maximum strand resistance at this section at the nominal moment resistance is $1,128.1 \mathrm{kips}>\mathrm{T}=966.7 \mathrm{kips} \mathbf{O K}$

## Design Step $\mid$ Horizontal shear between the beam and slab

5.7.7

Table 5.7-2 - Interface Shear Calculations

| Dist. | $\mathbf{d}_{\mathbf{e}}$ | $\mathbf{V}_{\mathbf{u}}$ | Max. <br> Stirrup <br> Spcg | Interface <br> reinf., $\mathbf{A}_{\mathbf{v f}}$ | Horiz. <br> Shear, $\mathbf{V}_{\mathbf{h}}$ | Nominal <br> resistance | Factored <br> resistance | resist./ <br> applied <br> load |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (ft.) | (in.) | (kips) | (in.) | (in²/in.) | (k/in.) | (k/in.) | (k/in.) | $>1.0$ OK |
| 7.00 | 74.13 | 340.40 | 16.0 | 0.050 | 4.59 | 7.20 | 6.48 | 1.41 |
| 11.00 | 74.22 | 315.10 | 18.0 | 0.044 | 4.25 | 6.84 | 6.16 | 1.45 |
| 16.50 | 74.34 | 280.66 | 21.0 | 0.038 | 3.78 | 6.48 | 5.83 | 1.54 |
| 22.00 | 74.34 | 246.74 | 20.0 | 0.040 | 3.32 | 6.60 | 5.94 | 1.79 |
| 27.50 | 74.50 | 213.36 | 24.0 | 0.033 | 2.86 | 6.18 | 5.56 | 1.94 |
| 33.00 | 74.50 | 180.55 | 24.0 | 0.033 | 2.42 | 6.18 | 5.56 | 2.30 |
| 38.50 | 74.50 | 148.33 | 24.0 | 0.033 | 1.99 | 6.18 | 5.56 | 2.79 |
| 44.00 | 74.50 | 116.71 | 24.0 | 0.033 | 1.57 | 6.18 | 5.56 | 3.55 |
| 49.50 | 74.50 | 85.74 | 24.0 | 0.033 | 1.15 | 6.18 | 5.56 | 4.83 |
| 54.50 | 74.50 | 118.40 | 24.0 | 0.033 | 1.59 | 6.18 | 5.56 | 3.50 |
| 55.00 | 74.50 | 121.32 | 24.0 | 0.033 | 1.63 | 6.18 | 5.56 | 3.42 |
| 60.50 | 74.50 | 153.49 | 24.0 | 0.033 | 2.06 | 6.18 | 5.56 | 2.70 |
| 66.00 | 74.50 | 185.68 | 24.0 | 0.033 | 2.49 | 6.18 | 5.56 | 2.23 |
| 71.50 | 74.50 | 217.85 | 24.0 | 0.033 | 2.92 | 6.18 | 5.56 | 1.90 |
| 77.00 | 74.50 | 249.96 | 24.0 | 0.033 | 3.36 | 6.18 | 5.56 | 1.66 |
| 82.50 | 74.50 | 281.95 | 21.0 | 0.033 | 3.78 | 6.18 | 5.56 | 1.47 |
| 88.00 | 74.34 | 313.79 | 19.0 | 0.042 | 4.22 | 6.72 | 6.05 | 1.43 |
| 93.50 | 75.52 | 345.42 | 11.0 | 0.073 | 4.57 | 8.58 | 7.72 | 1.69 |
| 99.00 | 75.52 | 376.79 | 8.0 | 0.100 | 4.99 | 10.20 | 9.18 | 1.84 |
| 102.50 | 75.52 | 396.58 | 7.0 | 0.114 | 5.25 | 11.04 | 9.94 | 1.89 |
|  |  |  |  |  |  |  |  |  |

Sample calculations at 11 ft . from the centerline of bearing on the abutment ( $11 \mathrm{ft} .-9 \mathrm{in}$. from girder end)

Horizontal shear forces develop along the interface between the concrete girders and the deck. As an alternative to the classical elastic strength of materials approach, the value of these forces per unit length of the girders at the strength limit state can be taken as:
$\mathrm{V}_{\mathrm{h}}=\mathrm{V}_{\mathrm{u}} / \mathrm{d}_{\mathrm{e}}$
(SC5.8.4.1-1)
where:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{h}} & =\text { horizontal shear per unit length of the girder (kips) } \\
\mathrm{V}_{\mathrm{u}} & =\text { the factored vertical shear (kips) } \\
& =315.1 \mathrm{k} \text { (From Table } 5.7-2)
\end{aligned}
$$

$d_{e}=$ distance between the centroid of the steel in the tension side of the beam to the center of the compression blocks in the deck (in.)
$=74.22$ in. (see Table 5.7-2)

$$
\begin{aligned}
\mathrm{V}_{\mathrm{h}} & =315.1 / 74.22 \\
& =4.25 \mathrm{k} / \mathrm{in} .
\end{aligned}
$$

Stirrup spacing at this location $=18$ in.
Assume that the stirrups extend into the deck. In addition, assume that there is another \#4 bar with two legs extending into the deck as shown in Figure 5.7-2.

Area of reinforcement passing through the interface between the deck and the girder, $\mathrm{A}_{\mathrm{vf}}$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{vf}} & =4 \# 4 \text { bars } \\
& =4(0.2) \\
& =0.8 \mathrm{in}^{2}
\end{aligned}
$$

$\mathrm{A}_{\mathrm{vf}}$ per unit length of beam $=0.8 / 18=0.044 \mathrm{in}^{2} / \mathrm{in}$. of beam length .
Check if the minimum interface shear reinforcement may be waived (S5.8.4.1)
Shear stress on the interface $=\mathrm{V}_{\mathrm{h}} /$ area of the interface

$$
=4.25 / 42
$$

$=0.101 \mathrm{ksi}>0.1 \mathrm{ksi}$, minimum reinforcement requirement may not be waived

Notice that the difference is only 1\%. For actual design, this difference would be within acceptable tolerances, therefore, the minimum reinforcement requirement could be waived. For this example, in order to provide a complete reference, the minimum reinforcement requirement will not be waived.

Check the minimum interface shear reinforcement

$$
\begin{align*}
\mathrm{A}_{\mathrm{vf}} & \geq 0.05 \mathrm{~b}_{\mathrm{v}} / \mathrm{f}_{\mathrm{y}}  \tag{S5.8.4.1-4}\\
& =0.05(42) / 60 \\
& =0.035 \mathrm{in}^{2} / \mathrm{in} . \text { of beam length }<\mathrm{A}_{\mathrm{s}} \text { provided } \mathbf{O K}
\end{align*}
$$

## Shear friction resistance

The interface shear resistance of the interface has two components. The first component is due to the adhesion between the two surfaces. The second component is due to the friction. In calculating friction, the force acting on the interface is taken equal to the compression force on the interface plus the yield strength of the reinforcement passing
through the interface. The nominal shear resistance of the interface plane, $\mathrm{V}_{\mathrm{n}}$, is calculated using S5.8.4.1.

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}}=\mathrm{c} \mathrm{~A}_{\mathrm{cv}}+\mu\left(\mathrm{A}_{\mathrm{vf}} \mathrm{f}_{\mathrm{y}}+\mathrm{P}_{\mathrm{c}}\right) \tag{S5.8.4.1-1}
\end{equation*}
$$

where:
$\mathrm{V}_{\mathrm{n}}=$ nominal shear friction resistance (kips)
$\mathrm{A}_{\mathrm{cv}}=$ area of concrete engaged in shear transfer $\left(\mathrm{in}^{2}\right)$
$\mathrm{A}_{\mathrm{vf}}=$ area of shear reinforcement crossing the shear plane (in ${ }^{2}$ )
$\mathrm{f}_{\mathrm{y}}=$ yield strength of reinforcement $(\mathrm{ksi})$
c $=$ cohesion factor specified in S5.8.4.2 (ksi)
$\mu=$ friction factor specified in S5.8.4.2
$\mathrm{P}_{\mathrm{c}}=$ permanent net compressive force normal to the shear plane (kips)
Calculate the nominal shear resistance per unit length of beam.
Assuming the top surface of the beam was clean and intentionally roughened,

$$
\begin{equation*}
\mathrm{c}=0.1 \mathrm{ksi} \text { and } \mu=1.0 \lambda \tag{S5.8.4.2}
\end{equation*}
$$

Ignore compression on the interface from loads on the deck: $\mathrm{P}_{\mathrm{c}}=0.0$

$$
\begin{aligned}
& \mathrm{A}_{\mathrm{cv}}=42 \mathrm{in}^{2} / \mathrm{in} . \text { of beam length } \\
& \mathrm{A}_{\mathrm{vf}}=0.044 \mathrm{in}^{2} / \mathrm{in} . \text { of beam length } \\
& \mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =0.1(42)+1.0[0.044(60)+0.0] \\
& =6.84 \mathrm{k} / \mathrm{in} . \text { of beam length }
\end{aligned}
$$

According to S5.8.4.1, the nominal shear resis tance, $\mathrm{V}_{\mathrm{n}}$, used in the design must also satisfy:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}} \leq 0.2 \mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{A}_{\mathrm{cv}} \tag{S5.8.4.1-2}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}} \leq 0.8 \mathrm{~A}_{\mathrm{cv}} \tag{S5.8.4.1-3}
\end{equation*}
$$

where:
$\mathrm{f}_{\mathrm{c}}^{\prime}=$ the strength of the weaker concrete (ksi)
$=4.0 \mathrm{ksi}$ for slab concrete
$\mathrm{V}_{\mathrm{n}} \leq 0.2 \mathrm{f}_{\mathrm{c}}{ }_{\mathrm{c}} \mathrm{A}_{\mathrm{cv}}=0.2(4.0)(42)=33.6 \mathrm{k} / \mathrm{in}$. of beam length
OR

$$
\mathrm{V}_{\mathrm{n}} \leq 0.8 \mathrm{~A}_{\mathrm{cv}}=0.8(42)=33.6 \mathrm{k} / \mathrm{in} \text {. of beam length }
$$

Therefore, $\mathrm{V}_{\mathrm{n}}$ used for design $=7.02 \mathrm{k} / \mathrm{in}$. of beam length.

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(6.84) \\
& =6.16 \mathrm{k} / \mathrm{in} . \text { of beam length }>\text { applied force, } \mathrm{V}_{\mathrm{h}}=4.25 \mathrm{k} / \mathrm{in} . \text { OK }
\end{aligned}
$$

# Design Step $\mid$ STEEL-REINFORCED ELASTOMERIC BEARING DESIGN 6.0 (S14) <br> <br> Design requirements (S14.5.3) 

 <br> <br> Design requirements (S14.5.3)}

Movements during construction
Where practicable, construction staging should be used to delay construction of abutments and piers located in or adjacent to embankments until the embankments have been placed and consolidated. Otherwise, deck joints should be sized to accommodate the probable abutment and pier movements resulting from embankment consolidation after their construction.

Closure pours may be used to minimize the effect of prestress-induced shortening on the width of seals and the size of bearings.

## Characteristics (S14.6.2)

The bearing chosen for a particular application has to have appropriate load and movement capabilities. Table S14.6.2-1 may be used as a guide when comparing different bearing systems.

## Force effects resulting from restraint of movement at the bearing (S14.6.3)

Restraint forces occur when any part of a movement is prevented. Forces due to direct loads include dead load of the bridge and loads due to traffic, earthquakes, water and wind. The applicable limit states must be considered.

Bearings are typically located in an area which collects large amounts of dirt and moisture and promotes problems of corrosion and deterioration. As a result, bearings should be designed and installed to have the maximum possible protection against the environment and to allow easy access for inspection.

## Elastomeric bearing overview

Shore A Durometer hardnesses of $60 \pm 5$ are common, and they lead to shear modulus values in the range of 80 to 180 psi. The shear stiffness of the bearing is its most important property since it affects the forces transmitted between the superstructure and substructure. Some states use a slightly different common range than stated above. See S14.7.5.2 and S14.7.6.2 for material requirements of neoprene bearing pads.

Elastomer may be used as a plain pad (PEP) or may be reinforced with steel. Steel reinforced elastomeric bearings are composed of layers of elastomer and steel plates bonded together with adhesive.

Elastomers are flexible under shear and uniaxial deformation, but they are very stiff against volume changes. This feature makes the design of a bearing that is stiff in compression but flexible in shear possible. Under uniaxial compression, the flexible elastomer would shorten significantly and, to maintain constant volume, sustain large increases in its plan dimension, but the stiff steel layers of the steel reinforced elastomeric bearings restrain the lateral expansion.

Elastomers stiffen at low temperatures. The low temperature stiffening effect is very sensitive to the elastomer compound, and the increase in shear resistance can be controlled by selection of an elasotmer compound which is appropriate for the climatic conditions.

The design of a steel reinforced elastomeric bearing requires an appropriate balance of compressive, shear and rotational stiffnesses. The shape factor, taken as the plan area divided by the area of the perimeter free to bulge, affects the compressive and rotational stiffnesses, but it has no impact on the translational stiffness or deformation capacity.

The bearing must be designed to control the stress in the steel reinforcement and the strain in the elastomer. This is done by controlling the elastomer layer thickness and the shape factor of the bearing. Fatigue, stability, delamination, yield and rupture of the steel reinforcement, stiffness of the elastomer, and geometric constraints must all be satisfied.

## Design methods

Two design methods are allowed by the AASHTO-LRFD Specifications. Method A, specified in S14.7.6, is applicable to plain, steel reinforced and fiber glass reinforced elastomeric pads as well as cotton duck pads. Method B, specified in S14.7.5, is applicable to steel reinforced elastomeric bearings. The following sections and the design example below are based on Method B. Flowcharts for the bearing design using both Method A and Method B are included in Section 3.

## General elastomer material properties and selection criteria (S14.7.5.2)

Commonly used elastomers have a shear modulus between 0.080 and 0.175 ksi and a nominal hardness between 50 and 60 on the Shore A scale. The shear modulus of the elastomer at $73^{\circ} \mathrm{F}$ is used as the basis for design. The elastomer may be specified by its shear modulus or hardness. If the elastomer is specified explicitly by its shear modulus, that value is used in design, and other properties are obtained from Table S14.7.5.2-1. If the material is specified by its hardness, the shear modulus is taken as the least favorable value from the range for that hardness given in Table S14.7.5.2-1. Intermediate values may be obtained by interpolation.

Elastomer grade is selected based on the temperature zone of the bridge location and by Table S14.7.5.2-2. The temperature zones are shown in Figure 6-1.

Table S14.7.5.2-2 - Low-Temperature Zones and Minimum Grades of Elastomer

| Low-Temperature Zone | A | B | C | D | E |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 50-year low temperature $\left(^{\circ} \mathrm{F}\right)$ | 0 | -20 | -30 | -45 | $<-45$ |
| Maximum number of consecutive days when the <br> temperature does not rise above $32^{\circ} \mathrm{F}$ | 3 | 7 | 14 | NA | NA |
| Minimum low-temperature elastomer grade | 0 | 2 | 3 | 4 | 5 |
| Minimum low-temperature elastomer grade <br> when special force provisions are incorporated | 0 | 0 | 2 | 3 | 5 |



## Figure 6-1 - Temperature Zones

According to S14.7.5.2, any of the three design options listed below may be used to specify the elastomer:

1) Specify the elastomer with the minimum low-temperature grade indicated in Table S14.7.5.2-2 and determine the shear force transmitted by the bearing as specified in S14.6.3.1;
2) Specify the elastomer with the minimum low-temperature grade for use when special force provisions are incorporated in the design but do not provide a low friction sliding surface, in which case the bridge shall be designed to withstand twice the design shear force specified in S14.6.3.1; or
3) Specify the elastomer with the minimum low-temperature grade for use when special force provisions are incorporated in the design but do not provide a low friction sliding surface, in which case the components of the bridge shall be designed to resist four times the design shear force as specified in S14.6.3.1.

Design Step Design a steel reinforced elastomeric bearing for the interior girders at the intermediate pier

A typical elastomer with hardness 60 Shore A Durometer and a shear modulus of 150 psi is assumed. The 1.75 ksi delamination stress limit of Eq. S14.7.5.3.2-3 requires a total plan area at least equal to the vertical reaction on the bearing divided by 1.75. The bearing reaction at different limit states is equal to the shear at the end of Span 1 as shown in Tables 5.3-3 and -4. These values are shown in Table 6-1 below.

Table 6-1 - Design Forces on Bearings of Interior Girders at the Intermediate Pier

|  | Max. factored reaction <br> $(\mathrm{k})$ | Max. reaction due to LL <br> $(\mathrm{k})$ |
| :--- | :---: | :---: |
| Strength I | 433.0 | $1.75(129.9)$ |
| Service I | 290.5 | 129.9 |

Notice that:

- The loads shown above include the dynamic load allowance. According to the commentary of S14.7.5.3.2, the effect of the dynamic load allowance on the elastomeric bearing reaction may be ignored. The reason for this is that the dynamic load allowance effects are likely to be only a small proportion of the total load and because the stress limits are based on fatigue damage, whose limits are not clearly defined. For this example, the dynamic load allowance (33\% of the girder maximum response due to the truck) adds 21.64 and 37.88 kips to the girder factored end shear at the Service I and Strength I limit states, respectively. This is a relatively small force, therefore, the inclusion of the dynamic load allowance effect leads to a slightly more conservative design.
- The live load reaction per bearing is taken equal to the maximum girder live load end shear. Recognizing that the girder, which is continuous for live load, has two bearings on the intermediate pier, another acceptable procedure is to divide the maximum live load reaction on the pier equally between the two bearings. This will result in lower bearing loads compared to using the girder end shear to design the bearings. This approach was not taken in this example, rather, the girder end shear was applied to the bearing.


## Design Step Determine the minimum bearing area

6.1.1

The bearing at the intermediate pier is fixed and is not subject to shear deformation due to the lack of movements. According to S14.7.5.3.2, the maximum compressive stress limit under service limit state for bearings fixed against shear deformations:

$$
\begin{align*}
& \sigma_{\mathrm{s}} \leq 2.00 \mathrm{GS} \leq 1.75 \mathrm{ksi}  \tag{S14.7.5.3.2-3}\\
& \sigma_{\mathrm{L}} \leq 1.00 \mathrm{GS} \tag{S14.7.5.3.2-4}
\end{align*}
$$

where:
$\sigma_{\mathrm{s}}=$ service average compressive stress due to the total load (ksi)
$\sigma_{\mathrm{L}}=$ service average compressive stress due to live load (ksi)
$\mathrm{G}=$ shear modulus of elastomer (ksi)
$S=$ shape factor of the thickest layer of the bearing
To satisfy the 1.75 ksi limit, the minimum bearing area, $\mathrm{A}_{\text {req }}$, should satisfy:

$$
\mathrm{A}_{\mathrm{req}}>290.5 / 1.75=166.0 \mathrm{in}^{2}
$$

The corners of the bottom flanges of the girder are usually chamfered. The bearing should be slightly narrower than the flat part of the flange unless a stiff sole plate is used to insure uniform distribution of the compressive stress and strain over the bearing area. The bearing should be as short along the ength of the girder as practical to permit rotation about the transverse axis. This requires the bearing to be as wide as possible which is desirable when stabilizing the girder during erection. For a first estimate, choose a 24 in . width [ 28 in . wide girder bottom flange $-2(1 \mathrm{in}$. chamfer +1 in . edge clearance)] and a 7.5 in. longitudinal dimension to ensure that the maximum compressive stress limit is satisfied (area $=24(7.5)=180 \mathrm{in}^{2}>166 \mathrm{in}^{2}$ required OK). The longitudinal translation is 0 in . for a fixed bearing. Notice that for a bearing subject to translation, i.e., movable bearing, the shear strains due to translation must be less than $0.5 \mathrm{in} . / \mathrm{in}$. to prevent rollover and excess fatigue damage. This means that the total elastomer thickness, $\mathrm{h}_{\mathrm{rt}}$, must be greater than two times the design translation, $\Delta_{\mathrm{s}}$, where applicable. A preliminary shape factor should be calculated according to S14.7.5.1.

## Design Step

Steel-reinforced elastomeric bearings - Method B (S14.7.5)
6.1.2

For bridges at locations where the roadway has positive or negative grade, the thickness of the bearing may need to be varied along the length of the girder. This is typically accomplished through the used of a tapered steel top plate. In this example, the bridge is assumed to be at zero grade and, therefore, each elastomer and reinforcement layer has a constant thickness. All internal layers of elastomer shall be of the same thickness. For bearings with more than two elastomer layers, the top and bottom cover layers should be no thicker than 70 percent of the internal layers.

The shape factor of a layer of an elastomeric bearing, $\mathrm{S}_{\mathrm{i}}$, is taken as the plan area of the layer divided by the area of perimeter free to bulge. For rectangular bearings without holes, the shape factor of the layer may be taken as:

$$
\begin{equation*}
\mathrm{S}_{\mathrm{i}}=\mathrm{LW} /\left[2 \mathrm{~h}_{\mathrm{ri}}(\mathrm{~L}+\mathrm{W})\right] \tag{S14.7.5.1-1}
\end{equation*}
$$

where:
$\mathrm{L}=$ length of a rectangular elastomeric bearing (parallel to the longitudinal bridge axis) (in.)
$\mathrm{W}=$ width of the bearing in the transverse direction (in.)
$\mathrm{h}_{\mathrm{ri}}=$ thickness of $\mathrm{i}^{\text {th }}$ elastomeric layer in elastomeric bearing (in.)
Determine the thickness of the $1^{\text {th }}$ elastomeric layer by rewriting Eq. S14.7.5.1-1 and solving for $\mathrm{h}_{\mathrm{r}}$ due to the total load.

$$
\mathrm{h}_{\mathrm{ri}}=\mathrm{LW} /\left[2 \mathrm{~S}_{\mathrm{i}}(\mathrm{~L}+\mathrm{W})\right]
$$

Design Step
Design Requirements (S14.7.5.3)
6.1.2.1

Compressive stress (S14.7.5.3.2):
In any elastomeric bearing layer, the average compressive stress at the service limit state will satisfy the following provisions.

These provisions limit the shear stress and strain in the elastomer. The relationship between the shear stress and the applied compressive bad depends directly on the shape factor, with higher shape factors leading to higher capacities.

First, solve for the shape factor under total load, $\mathrm{S}_{\mathrm{TL}}$, by rewriting Eq. S14.7.5.3.2-3 for bearings fixed against shear deformation.

$$
\begin{equation*}
\mathrm{S}_{\mathrm{TL}} \geq \sigma_{\mathrm{S}} / 2.00 \mathrm{G} \tag{S14.7.5.3.2-3}
\end{equation*}
$$

where:

$$
\begin{align*}
& \sigma_{\mathrm{s}}=\mathrm{P}_{\mathrm{TL}} / \mathrm{A}_{\mathrm{req}} \\
& \mathrm{P}_{\mathrm{TL}}=\text { maximum bearing reaction under total load }(\mathrm{k}) \\
&=290.5 \mathrm{k} \\
& \sigma_{\mathrm{s}}=290.5 /[7.5(24)] \\
&=1.614 \mathrm{ksi} \\
& \mathrm{G}=0.150 \mathrm{ksi} \\
& \\
& \mathrm{~S}_{\mathrm{TL}} \geq 1.614 /[2.00(0.150)]  \tag{1}\\
& \geq 5.38
\end{align*}
$$

Solve for the shape factor under live load, $S_{L L}$, by rewriting Eq. S14.7.5.3.2-4 for bearings fixed against shear deformation.

$$
\begin{equation*}
\mathrm{S}_{\mathrm{LL}} \geq \sigma_{\mathrm{L}} / 1.00 \mathrm{G} \tag{S14.7.5.3.2-4}
\end{equation*}
$$

where:

$$
\begin{align*}
& \sigma_{\mathrm{L}}=\mathrm{P}_{\mathrm{LL}} / \mathrm{A}_{\text {req }} \\
& \mathrm{P}_{\mathrm{LL}}=\text { maximum bearing live load reaction }(\mathrm{k}) \\
&=129.9 \mathrm{k} \\
& \sigma_{\mathrm{L}}=129.9 /[7.5(24)] \\
&=0.722 \mathrm{ksi} \\
& \mathrm{~S}_{\mathrm{LL}} \geq 0.722 /[1.00(0.150)] \\
& \geq 4.81 \tag{2}
\end{align*}
$$

From (1) and (2), the minimum shape factor of any layer is 5.38.
Notice that if holes are present in the elastomeric bearing their effect needs to be accounted for when calculating the shape factor because they reduce the loaded area and increase the area free to bulge. Use Eq. SC14.7.5.1-1 in this case instead of Eq. S14.7.5.1-1.

Using the shape factors of $\mathrm{S}_{\mathrm{TL}}$ and $\mathrm{S}_{\mathrm{LL}}$ calculated above, determine the elastomer thickness.

$$
\begin{aligned}
\mathrm{h}_{\mathrm{ri}(\mathrm{TL})} & <(\mathrm{LW}) /\left[2\left(\mathrm{~S}_{\mathrm{TL}}\right)(\mathrm{L}+\mathrm{W})\right] \\
& <7.5(24) /[2(5.38)(7.5+24)] \\
& <0.531 \mathrm{in} .
\end{aligned}
$$

and

$$
\begin{aligned}
\mathrm{h}_{\mathrm{ri}(\mathrm{LL})} & <(\mathrm{LW}) /\left[2\left(\mathrm{~S}_{\mathrm{LL}}\right)(\mathrm{L}+\mathrm{W})\right] \\
& <7.5(24) /[2(4.81)(7.5+24)] \\
& <0.594 \mathrm{in} .
\end{aligned}
$$

Use an interior elastomer layer thickness of $\mathrm{h}_{\mathrm{ri}}=0.5 \mathrm{in}$.
The shape factor is:

$$
\begin{aligned}
\mathrm{S} & =(\mathrm{LW}) /\left[2\left(\mathrm{~h}_{\mathrm{r}}\right)(\mathrm{L}+\mathrm{W})\right] \\
& =7.5(24) /[2(0.5)(7.5+24)] \\
& =5.71
\end{aligned}
$$

Design Step<br>6.1.2.2

Compressive deflection (S14.7.5.3.3)
This provision need only be checked if deck joints are present on the bridge. Since this design example is a jointless bridge, commentary for this provision is provided below, but no design is investigated.

Deflections of elastometric bearings due to total load and live load alone will be considered separately.

Instantaneous deflection is be taken as:

$$
\begin{equation*}
\delta=\Sigma \varepsilon_{i} h_{r i} \tag{S14.7.5.3.3-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \varepsilon_{i}=\text { instantaneous compressive strain in } i^{\text {th }} \text { elastomer layer of a } \\
& \quad \text { laminated bearing }
\end{aligned}
$$

Values for $\varepsilon_{i}$ are determined from test results or by analysis when considering long-term deflections. The effects of creep of the elastomer are added to the instantaneous deflection. Creep effects should be determined from information relevant to the elastomeric compound used. In the absence of material-specific data, the values given in S14.7.5.2 may be used.

## Design Step <br> Shear deformation (S14.7.5.3.4)

6.1.2.3

This provision need only be checked if the bearing is a movable bearing. Since the bearing under consideration is a fixed bearing, this provision does not apply. Commentary on this provision is provided below, but no design checks are performed.

The maximum horizontal movement of the bridge superstructure, $\Delta_{o}$, is taken as the extreme displacement caused by creep, shrinkage, and posttensioning combined with thermal movements.

The maximum shear deformation of the bearing at the service limit state, $\Delta_{s}$, is taken as $\Delta_{o}$, modified to account for the substructure stiffness and construction procedures. If a low friction sliding surface is installed, $\Delta_{s}$ need not be taken to be larger than the deformation corresponding to first slip.

The bearing is required to satisfy:

$$
\begin{equation*}
h_{r t} \geq 2 \Delta_{s} \tag{S14.7.5.3.4-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
& h_{r t}=\text { total elastomer thickness (sum of the thicknesses of all elastomer } \\
& \text { layers) (in.) }
\end{aligned}
$$

$\Delta_{s}=$ maximum shear deformation of the elastomer at the service limit
state (in.)

This limit on $h_{r t}$ ensures that rollover at the edges and delamination due to fatigue will not take place. See SC14.7.5.3.4 for more stringent requirements when shear deformations are due to high cycle loading such as braking forces and vibrations.

Design Step
Combined compression and rotation (S14.7.5.3.5)
6.1.2.4

Service limit state applies. Design rotations are taken as the maximum sum of the effects of initial lack of parallelism between the bottom of the girder and the top of the superstructure and subsequent girder end rotation due to imposed loads and movements.

The goal of the following requirements is to prevent uplift of any corner of the bearing under any combination of loading and corresponding rotation.

Rectangular bearings are assumed to satisfy uplift requirements if they satisfy:
$\sigma_{\mathrm{s}}>1.0 \mathrm{GS}\left(\theta_{\mathrm{s}} / \mathrm{n}\right)\left(\mathrm{B} / \mathrm{h}_{\mathrm{ri}}\right)^{2}$
where:
n = number of interior layers of elastomer, where interior layers are defined as those layers which are bonded on each face. Exterior layers are defined as those layers which are bonded only on one face. When the thickness of the exterior layer of elastomer is more than one-half the thickness of an interior layer, the parameter, n, may be increased by one-half for each such exterior layer.
$\mathrm{h}_{\mathrm{ri}}=0.5 \mathrm{in}$.
$\sigma_{\mathrm{s}}=$ maximum compressive stress in elastomer (ksi)
$=1.614 \mathrm{ksi}$
B = length of pad if rotation is about its transverse axis or width of pad if rotation is about its longitudinal axis (in.)
$=7.5 \mathrm{in}$.
$\theta_{\mathrm{s}}=$ maximum service rotation due to the total load (rads)
For this example, $\theta_{\mathrm{s}}$ will include the rotations due to live load and construction load (assume 0.005 rads) only. As a result of camber under the prestressing force and permanent dead loads, prestressed beams typically have end rotation under permanent dead loads in the opposite direction than that of the live load end rotations. Conservatively assume the end rotations to be zero under the effect of the prestressing and permanent loads.

$$
=0.005944 \text { rads (from a live load analysis program) }
$$

Rewrite Eq. S14.7.5.3.5-1 to determine the number of interior layers of elastomer, $n_{u}$, for uplift:

$$
\begin{aligned}
\mathrm{n}_{\mathrm{u}} & >1.0 \mathrm{GS}\left(\theta_{\mathrm{s}}\right)\left(\mathrm{B} / \mathrm{h}_{\mathrm{ri}}{ }^{2} / \sigma_{\mathrm{s}}\right. \\
& >1.0(0.150)(5.71)(0.005944)(7.5 / 0.5)^{2} / 1.614 \\
& >0.710
\end{aligned}
$$

To prevent excessive stress on the edges of the elastomer, rectangular bearings fixed against shear deformation must also satisfy:

$$
\begin{equation*}
\sigma_{\mathrm{s}}<2.25 \mathrm{GS}\left[1-0.167\left(\theta_{\mathrm{s}} / \mathrm{n}\right)\left(\mathrm{B} / \mathrm{h}_{\mathrm{ri}}\right)^{2}\right] \tag{S14.7.5.3.5-3}
\end{equation*}
$$

Rewrite Eq. S14.7.5.3.5-3 to determine the number of interior layers of elastomer, $n$, required to limit compression along the edges.

$$
\begin{aligned}
\mathrm{n}_{\mathrm{c}} & >-0.167\left(\theta_{\mathrm{s}}\right)\left(\mathrm{B} / \mathrm{h}_{\mathrm{ri}}\right)^{2} /\left[\sigma_{\mathrm{s}} / 2.25 \mathrm{GS}-1\right] \\
& >-0.167(0.005944)(7.5 / 0.5)^{2} /[1.614 /[2.25(0.150)(5.71)]-1] \\
& >1.37
\end{aligned}
$$

Use 2 interior layers 0.5 in. thick each. Use exterior layers 0.25 in. thick each ( $<70 \%$ of the thickness of the interior layer).

## Design Step 6.1.2.5

Stability of elastomeric bearings (S14.7.5.3.6)
Bearings are investigated for instability at the service limit state load combinations specified in Table S3.4.1-1.

Bearings satisfying Eq. S14.7.5.3.6-1 are considered stable, and no further investigation of stability is required.

$$
\begin{equation*}
2 \mathrm{~A} \leq \mathrm{B} \tag{S14.7.5.3.6-1}
\end{equation*}
$$

for which:

$$
\begin{align*}
& \mathrm{A}=\frac{1.92 \frac{\mathrm{~h}_{\mathrm{rt}}}{\mathrm{~L}}}{\sqrt{1+\frac{2.0 \mathrm{~L}}{\mathrm{~W}}}}  \tag{S14.7.5.3.6-2}\\
& B=\frac{2.67}{(\mathrm{~S}+2.0)\left(1+\frac{\mathrm{L}}{4.0 \mathrm{~W}}\right)} \tag{S14.7.5.3.6-3}
\end{align*}
$$

where:

$$
\begin{aligned}
\mathrm{L} & =7.5 \mathrm{in} . \\
\mathrm{W} & =24 \mathrm{in} . \\
& \\
\mathrm{h}_{\mathrm{rt}} & =\text { total thickness of the elastomer in the bearing (in.) } \\
& =2(0.25)+2(0.5) \\
& =1.5 \mathrm{in} .
\end{aligned}
$$

For a rectangular bearing where L is greater than W , stability will be investigated by interchanging L and W in Eqs. S14.7.5.3.6-2 and -3.

$$
\begin{aligned}
\mathrm{A} & =\frac{1.92\left(\frac{1.5}{7.5}\right)}{\sqrt{1+\frac{2.0(7.5)}{24}}} \\
& =0.301 \\
\mathrm{~B} & =\frac{2.67}{(5.71+2.0)\left(1+\frac{7.5}{4.0(24)}\right)} \\
& =0.321
\end{aligned}
$$

Check 2A $\leq \mathrm{B}$
$2(0.301)=0.602>0.321$, therefore, the bearing is not stable and
Eqs. S14.7.5.3.6-4 and -5 need to be checked.
For bridge decks fixed against translation, the following equation needs to be satisfied to ensure stability.

$$
\begin{equation*}
\sigma_{\mathrm{s}} \leq \mathrm{GS} /(\mathrm{A}-\mathrm{B}) \tag{S14.7.5.3.6-5}
\end{equation*}
$$

However, if $\mathrm{A}-\mathrm{B} \leq 0$, then the bearing is considered stable.

$$
\begin{aligned}
\mathrm{A}-\mathrm{B} & =0.301-0.321 \\
& =-0.02
\end{aligned}
$$

Therefore, the bearing is stable.

## Design Step Reinforcement (S14.7.5.3.7)

6.1.2.6

The reinforcement should sustain the tensile stresses induced by compression on the bearing. With the present load limitations, the minimum steel plate thickness practical for fabrication will usually provide adequate strength.

At the service limit state:

$$
\begin{equation*}
\mathrm{h}_{\mathrm{s}} \geq 3 \mathrm{~h}_{\max } \sigma_{\mathrm{s}} / \mathrm{F}_{\mathrm{y}} \tag{S14.7.5.3.7-1}
\end{equation*}
$$

where:
$\mathrm{h}_{\max }=$ thickness of thickest elastomeric layer in elastomeric bearing (in.)
$=0.5 \mathrm{in}$.
$\sigma_{\mathrm{s}} \quad=1.614 \mathrm{ksi}$
$\mathrm{F}_{\mathrm{y}} \quad=$ yield strength of steel reinforcement (ksi)
$=36 \mathrm{ksi}$
$\mathrm{h}_{\mathrm{s}(\mathrm{TL})} \geq 3(0.5)(1.614) / 36$
$\geq 0.067$ in.
At the fatigue limit state:

$$
\begin{equation*}
\mathrm{h}_{\mathrm{s}} \geq 2.0 \mathrm{~h}_{\max } \sigma_{\mathrm{L}} / \Delta \mathrm{F}_{\mathrm{TH}} \tag{S14.7.5.3.7-2}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{h}_{\max } & =0.5 \mathrm{in} . \\
& \\
\sigma_{\mathrm{L}} & =129.9 /[7.5(24)] \\
& =0.722 \mathrm{ksi}
\end{aligned}
$$

$\Delta \mathrm{F}_{\mathrm{TH}}=$ constant amplitude fatigue threshold for Category A as specified in Table S6.6.1.2.5-3 (ksi)
$=24 \mathrm{ksi}$

$$
h_{s(L L)} \geq 2(0.5)(0.722) / 24
$$

$$
\geq 0.030 \mathrm{in} .
$$

Use $h_{s}=0.120$ in. thick steel reinforcement plates; this is an 11 gage shim.

If holes exist in the reinforcement, the minimum thickness is increased by a factor equal to twice the gross width divided by the net width. Holes in the reinforcement cause stress concentrations. Their use should be discouraged. The required increase in steel
thickness accounts for both the material removed and the stress concentrations around the hole.

The total height of the bearing, $\mathrm{h}_{\mathrm{t}}$ :

$$
\mathrm{h}_{\mathrm{rt}} \quad=\text { cover layers }+ \text { elastomer layers }+ \text { shim thicknesses }
$$

$=2(0.25)+2(0.5)+3(0.120)$

$$
=1.86 \mathrm{in} .
$$



PLAN
2-1/4" Cover layers
3-0.120" Shims
2-1/2" Interior layers


## ELEVATION

## Figure 6-2 - Dimensions of Elastomeric Bearing

Notes:

1. 11 gage steel shim thickness is held constant for all bearings
2. All cover layers and edge covers are to be $1 / 4$-inch thick.
3. Total bearing thickness will include the summation of a masonry plate, a sole plate, and the laminated elastomeric pad thickness.
4. Elastomer in all bearings shall have grade 60 Shore A Durometer hardness.
5. Pad shall be vulcanized to masonry plate and sole plate in the shop
6. Pad thickness shown is uncompressed.

A shear key between the bent cap and the concrete diaphragm will provide the movement restraint in the longitudinal direction. See Figure 6-3.


Figure 6-3 - Longitudinal Fixity at Intermediate Bent

## Design Step $\quad$ INTEGRAL ABUTMENT DESIGN

7.1

## General considerations and common practices

Integral abutments are used to eliminate expansion joints at the end of a bridge. They often result in "Jointless Bridges" and serve to accomplish the following desirable objectives:

- Long-term serviceability of the structure
- Minimal maintenance requirements
- Economical construction
- Improved aesthetics and safety considerations

A jointless bridge concept is defined as any design procedure that attempts to achieve the goals listed above by eliminating as many expansion joints as possible. The ideal jointless bridge, for example, contains no expansion joints in the superstructure, substructure or deck.

Integral abutments are generally founded on one row of piles made of steel or concrete. The use of one row of piles reduces the stiffness of the abutment and allows the abutment to translate parallel to the longitudinal axis of the bridge. This permits the elimination of expansion joints and movable bearings. Because the earth pressure on the two end abutments is resisted by compression in the superstructure, the piles supporting the integral abutments, unlike the piles supporting conventional abutments, do not need to be designed to resist the earth loads on the abutments.

When expansion joints are completely eliminated from a bridge, thermal stresses must be relieved or accounted for in some manner. The integral abutment bridge concept is based on the assumption that due to the flexibility of the piles, thermal stresses are transferred to the substructure by way of a rigid connection, i.e. the uniform temperature change causes the abutment to translate without rotation. The concrete abutment contains sufficient bulk to be considered as a rigid mass. A positive connection to the girders is generally provided by encasing girder ends in the reinforced concrete backwall. This provides for full transfer of forces due to thermal movements and live load rotational displacement experienced by the abutment piles.

## Design criteria

Neither the AASHTO-LRFD Specifications nor the AASHTO-Standard Specifications contain detailed design criteria for integral abutments. In the absence of universallyaccepted design criteria, many states have developed their own design guidelines. These guidelines have evolved over time and rely heavily on past experience with integral abutments at a specific area. There are currently two distinctive approaches used to design integral abutments:

- One group of states design the piles of an integral abutment to resist only gravity loads applied to the abutment. No consideration is given to the effect of the horizontal displacement of the abutment on the pile loads and/or pile resistance. This approach is simple and has been used successfully. When the bridge is outside a certain range set by the state, e.g. long bridges, other considerations are taken into account in the design.
- The second approach accounts for effects of different loads, in additional to gravity loads, when calculating pile loads. It also takes into account the effect of the horizontal movements on the pile load resistance. One state that has detailed design procedures following this approach is Pennsylvania.

The following discussion does not follow the practices of a specific state; it provides a general overview of the current state-of-practice.

## Bridge length limits

Most states set a limit on the bridge length of jointless bridges beyond which the bridge is not considered a "typical bridge" and more detailed analysis is taken into account. Typically, the bridge length is based on assuming that the total increase of the bridge length under uniform temperature change from the extreme low to the extreme high temperature is 4 inches. This means that the movement at the top of the pile at each end is 2 inches or, when the bridge is constructed at the median temperature, a 1 inch displacement in either direction. This results in a maximum bridge length of 600 ft . for concrete bridges and 400 ft. for steel bridges at locations where the climate is defined as "Moderate" in accordance to S3.12.2.1. The maximum length is shorter for regions defined as having a "cold" climate.

## Soil conditions

The above length limits assume that the soil conditions at the bridge location and behind the abutment are such that the abutment may translate with relatively low soil resistance. Therefore, most jurisdictions specify select granular fill for use behind integral abutments. In addition, the fill within a few feet behind the integral abutment is typically lightly compacted using a vibratory plate compactor (jumping jack). When bedrock, stiff soil and/or boulders exist in the top layer of the soil (approximately the top 12 to 15 ft .), it is typically required that oversized holes be drilled to a depth of approximately 15 ft .; the piles are then installed in the oversized holes. Subsequently, the holes are filled with sand. This procedure is intended to allow the piles to translate with minimal resistance.

## Skew angle

Earth pressure acts in a direction perpendicular to the abutments. For skewed bridges, the earth pressure forces on the two abutments produce a torque that causes the bridge to twist in plan. Limiting the skew angle reduces this effect. For skewed, continuous bridges, the twisting torque also results in additional forces acting on intermediate bents.

In addition, sharp skews are suspected to have caused cracking in some abutment backwalls due to rotation and thermal movements. This cracking may be reduced or eliminated by limiting the skew. Limiting the skew will also reduce or eliminate design uncertainties, backfill compaction difficulty and the additional design and details that would need to be worked out for the abutment $U$-wingwalls and approach slab.

Currently, there are no universally accepted limits on the degree of skew for integral abutment bridges.

## Horizontal alignment and bridge plan geometry

With relatively few exceptions, integral abutments are typically used for straight bridges. For curved superstructures, the effect of the compression force resulting from the earth pressure on the abutment is a cause for concern. For bridges with variable width, the difference in the length of the abutments results in unbalanced earth pressure forces if the two abutments are to move the same distance. To maintain force equilibrium, it is expected that the shorter abutment will deflect more than the longer one. This difference should be considered when determining the actual expected movement of the two abutments as well as in the design of the piles and the expansion joints at the end of the approach slabs (if used).

## Grade

Some jurisdictions impose a limit on the maximum vertical grade between abutments. These limits are intended to reduce the effect of the abutment earth pressure forces on the abutment vertical reactions.

## Girder types, maximum depth and placement

Integral abutments have been used for bridges with steel Ibeams, concrete Hbeams, concrete bulb tees and concrete spread box beams.

Deeper abutments are subjected to larger earth pressure forces and, therefore, less flexible. Girder depth limits have been imposed by some jurisdictions based on past successful practices and are meant to ensure a reasonable level of abutment flexibility. Soil conditions and the length of the bridge should be considered when determining maximum depth limits. A maximum girder depth of 6 ft . has been used in the past. Deeper girders may be allowed when the soil conditions are favorable and the total length of the bridge is relatively short.

## Type and orientation of piles

Integral abutments have been constructed using steel Hpiles, concrete-filled steel pipe piles and reinforced and prestressed concrete piles. For H-piles, there is no commonly used orientation of the piles. In the past, H-piles have been placed both with their strong
axis parallel to the girder's longitudinal axis and in the perpendicular direction. Both orientations provide satisfactory results.

## Consideration of dynamic load allowance in pile design

Traditionally, dynamic load allowance is not considered in foundation design. However, for integral abutment piles, it may be argued that the dynamic load allowance should be considered in the design of the top portion of the pile. The rationale for this requirement is that the piles are almost attached to the superstructure, therefore, the top portions of the piles do no benefit from the damping effect of the soil.

## Construction sequence

Typically, the connection between the girders and the integral abutment is made after the deck is poured. The end portion of the deck and the backwall of the abutment are usually poured at the same time. This sequence is intended to allow the dead load rotation of the girder ends to take place without transferring these rotations to the piles.

Two integral abutment construction sequences have been used in the past:

- One-stage construction:

In this construction sequence, two piles are placed adjacent to each girder, one pile on each side of the girder. A steel angle is connected to the two piles and the girder is seated on the steel angle. The abutment pier cap (the portion below the bottom of the beam) and the end diaphragm or backwall (the portion encasing the ends of the beams) are poured at the same time. The abutment is typically poured at the time the deck in the end span is poured.

- Two-stage construction:

Stage 1:
A pile cap supported on one row of vertical piles is constructed. The piles do not have to line up with the girders. The top of the pile cap reaches the bottom of the bearing pads under the girders. The top of the pile cap is required to be smooth in the area directly under the girders and a strip approximately 4 in. wide around this area. Other areas are typically roughened (i.e. rake finished).

Stage 2:
After pouring the entire deck slab, except for the portions of the deck immediately adjacent to the integral abutment (approximately the end 4 ft. of the deck from the front face of the abutment) the end diaphragm (backwall) encasing the ends of the bridge girders is poured. The end portion of the deck is poured simultaneously with the end diaphragm.

## Negative moment connection between the integral abutment and the superstructure

The rigid connection between the superstructure and the integral abutment results in the development of negative moments at this location. Some early integral abutments showed signs of deck cracking parallel to the integral abutments in the end section of the deck due to the lack of proper reinforcement to resist this moment. This cracking was prevented by specifying additional reinforcement connecting the deck to the back (fill) face of the abutment. This reinforcement may be designed to resist the maximum moment that may be transferred from the integral abutment to the superstructure. This moment is taken equal to the sum of the plastic moments of the integral abutment piles. The section depth used to design these bars may be taken equal to the girder depth plus the deck thickness. The length of the bars extending into the deck is typically specified by the bridge owner. This length is based on the length required for the superstructure dead load positive moment to overcome the connection negative moment.

## Wingwalls

Typically, U-wingwalls (wingwalls parallel to the longitudinal axis of the bridge) are used in conjunction with integral abutments. A chamfer (typically 1 ft .) is used between the abutment and the wingwalls to minimize concrete shrinkage cracking caused by the abrupt change in thickness at the connection.

## Approach slab

Bridges with integral abutments were constructed in the past with and without approach slabs. Typically, bridges without approach slabs are located on secondary roads that have asphalt pavements. Traffic and seasonal movements of the integral abutments cause the fill behind the abutment to shift and to self compact. This often caused settlement of the pavement directly adjacent to the abutment.

Providing a reinforced concrete approach slab tied to the bridge deck moves the expansion joint away from the end of the bridge. In addition, the approach slab bridges cover the area where the fill behind the abutment settles due to traffic compaction and movements of the abutment. It also prevents undermining of the abutments due to drainage at the bridge ends. Typically, approach slabs are cast on polyethylene sheets to minimize the friction under the approach slab when the abutment moves.

The approach slab typically rests on the abutment at one end and on a sleeper slab at the other. The approach slab differs from typical roadway pavement since the soil under the approach slab is more likely to settle unevenly resulting in the approach slab bridging a longer length than expected for roadway pavement. Typically, the soil support under the approach slab is ignored in the design and the approach slab is designed as a one-way slab bridging the length between the integral abutment and the sleeper slab. The required length of the approach slab depends on the total depth of the integral abutment. The sleeper slab should be placed outside the area where the soil is expected to be
affected by the movement of the integral abutment. This distance is a function of the type of fill and the degree of compaction.

Due to the difference in stiffness between the superstructure and the approach slab, the interface between the integral abutment and the approach slab should preferably allow the approach slab to rotate freely at the end connected to the abutment. The reinforcement bars connecting the abutment to the approach slab should be placed such that the rotational restraint provided by these bars is minimized.

A contraction joint is placed at the interface between the approach slab and the integral abutment. The contraction joint at this bcation provides a controlled crack location rather than allowing a random crack pattern to develop.

## Expansion joints

Typically, no expansion joints are provided at the interface between the approach slab and the roadway pavement when the bridge total length is relatively small and the roadway uses flexible pavement. For other cases, an expansion joint is typically used.

## Bearing pads

Plain elastomeric bearing pads are placed under all girders when the integral abutment is constructed using the two-stage sequence described above. The bearing pads are intended to act as leveling pads and typically vary from $1 / 2$ to $3 / 4$ in. thick. The pad length parallel to the girder's longitudinal axis varies depending on the bridge owner's specifications and the pad length in the perpendicular direction varies depending on the width of the girder bottom flange and the owner's specifications. It is recommended to block the area under the girders that is not in contact with the bearing pads using backer rods. Blocking this area is intended to prevent honeycombing of the surrounding concrete. Honeycombing will take place when the cement paste enters the gap between the bottom of girder and the top of the pile cap in the area under the girders not in contact with the bearing pads.

## Design Step

Gravity loads

Noncomposite:

| Girder | $=61.6 \mathrm{k}$ |
| :--- | :--- |
| Slab and haunch | $=62.2 \mathrm{k}$ |
| Exterior diaphragm | $=2.5 \mathrm{k}$ |
| Total NC | $=126.4 \mathrm{k}$ |

Composite:
Parapets $\quad=8.9 \mathrm{k}$
Future wearing surface $\quad=12.0 \mathrm{k}$
Live load:
Maximum truck per lane (without impact or distribution factors) $=64.42 \mathrm{k}$
Minimum truck per lane (without impact or distribution factors) $=-6.68 \mathrm{k}$
Maximum lane per lane $\quad=30.81 \mathrm{k}$
Minimum lane per lane $\quad=-4.39 \mathrm{k}$

Exterior girder: unfactored loads
(See Table 5.3-7 for girder end shears)
Noncomposite:

| Girder | $=61.6 \mathrm{k}$ |
| :--- | :--- |
| Slab and haunch | $=55.1 \mathrm{k}$ |
| Exterior diaphragm | $=1.3 \mathrm{k}$ |
| Total NC | $=117.9 \mathrm{k}$ |

Composite:
Parapets $\quad=8.9 \mathrm{k}$
Future wearing surface $\quad=8.1 \mathrm{k}$
Live load:
Maximum truck per lane (without impact or distribution factors) $=64.42 \mathrm{k}$
Minimum truck per lane (without impact or distribution factors) $=-6.68 \mathrm{k}$
Maximum lane per lane $\quad=30.81 \mathrm{k}$
Minimum lane per lane $\quad=-4.39 \mathrm{k}$


Figure 7.1-1 - General View of an Integral Abutment Showing Dimensions Used for the Example


Figure 7.1-2 - Plan View of the Integral Abutment


Figure 7.1-3 - Elevation View of Integral Abutment and Tapered Wingwall

In the next section, "w" and "P" denote the load per unit length and the total load, respectively. The subscripts denote the substructure component. Dimensions for each component are given in Figures 7.1-1 through 7.1-3.

Pile cap: unfactored loading
Pile cap length along the skew $=55.354 / \cos 20$

$$
=58.93 \mathrm{ft} .
$$

$$
\begin{aligned}
\mathrm{w}_{\mathrm{cap}} & =3.25(3)(0.150) \\
& =1.46 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {cap }} & =1.46(58.93) \\
& =86.0 \mathrm{k}
\end{aligned}
$$

Concrete weight from the end diaphragm (approximate, girder volume not removed): unfactored loading

Assuming bearing pad thickness of $3 / 4$ in., girder height of 72 in., haunch thickness of 4 in., and deck thickness of 8 in.:

$$
\begin{aligned}
\mathrm{w}_{\text {end dia }} & =3[(0.75+72+4+8) / 12](0.150) \\
& =3.18 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {end dia }} & =3.18(58.93) \\
& =187.4 \mathrm{k}
\end{aligned}
$$

Wingwall: unfactored load

$$
\begin{aligned}
\mathrm{A}_{\text {wing }} & =(123.75 / 12)(15)-1 / 2(14)(99.75 / 12) \\
& =96.5 \mathrm{ft}^{2}
\end{aligned}
$$

Wingwall thickness = parapet thickness at the base

$$
=20.25 \text { in. (given in Section 4) }
$$

Wingwall weight $\quad=96.5(20.25 / 12)(0.150)$

$$
=24.43 \mathrm{k}
$$

Chamfer weight $\quad=(123.75 / 12)(1.0)(1.0)(0.150) / 2$

$$
=0.77 \mathrm{k}
$$

Notice that the chamfer weight is insignificant and is not equal for the two sides of the bridge due to the skew. For simplicity, it was calculated based on a right angle triangle and the same weight is used for both sides.

Weight of two wingwalls plus chamfer $=2(24.43+0.77)$

$$
=50.4 \mathrm{k}
$$

Parapet weight $=0.65 \mathrm{k} / \mathrm{ft}$ (given in Section 5.2)
Parapet length on wingwall and abutment $=15+3 / \sin 70$

$$
=18.19 \mathrm{ft} .
$$

$$
\begin{aligned}
\mathrm{P}_{\text {parapet }} & =2(0.650)(18.19) \\
& =23.65 \mathrm{k} \text { total weight }
\end{aligned}
$$

Approach slab load acting on the integral abutment: unfactored loading
Approach slab length $=25 \mathrm{ft}$.
Approach slab width between parapets $=58.93-2[(20.25 / 12) / \sin 70]$

$$
=55.34 \mathrm{ft} .
$$

Self weight of the approach slab:

$$
\begin{aligned}
\mathrm{w}_{\text {approach slab }} & =1 / 2(25)(1.5)(0.150) \\
& =2.81 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {approach slab }} & =2.81(55.34) \\
& =155.5 \mathrm{k}
\end{aligned}
$$

Future wearing surface acting on the approach slab (assuming 25 psf ):

$$
\begin{aligned}
\mathrm{w}_{\mathrm{FWS}} & =1 / 2(0.025)(25) \\
& =0.31 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {FWS }} & =0.31(55.34) \\
& =17.2 \mathrm{k}
\end{aligned}
$$

Live load on the approach slab, reaction on integral abutment:

$$
\begin{align*}
\mathrm{P}_{\text {lane load }} & =1 / 2(0.64)(25)  \tag{S3.6.1.2.4}\\
& =8.0 \mathrm{k} \text { (one lane) }
\end{align*}
$$

Design Step
7.1.2

The girder reactions, interior and exterior, are required for the design of the abutment pile cap. Notice that neither the piles nor the abutment beam are infinitely rigid. Therefore, loads on the piles due to live loads are affected by the location of the live load across the width of the integral abutment. Moving the live load reaction across the integral abutment and trying to maximize the load on a specific pile by changing the number of loaded traffic lanes is not typically done when designing integral abutments. As a simplification, the live load is assumed to exist on all traffic lanes and is distributed equally to all girders in the bridge cross section. The sum of all dead and live loads on the abutment is then distributed equally to all piles supporting the abutment.

The maximum number of traffic lanes allowed on the bridge based on the available width ( 52 ft . between gutter lines) is:

$$
\begin{aligned}
\mathrm{N}_{\text {lanes }} & =52 \mathrm{ft} . / 12 \mathrm{ft} . \text { per lane } \\
& =4.33 \text { say } 4 \text { lanes }
\end{aligned}
$$

Factored dead load plus live load reactions for one interior girder, Strength I limit state controls (assume the abutment is poured in two stages as discussed earlier):

Maximum reaction Stage I:

$$
\begin{aligned}
\mathrm{P}_{\mathrm{SI}(\mathrm{I})} & =1.25(\text { girder }+ \text { slab }+ \text { haunch }) \\
& =1.25(126.4) \\
& =158 \mathrm{k}
\end{aligned}
$$

Notice that construction loads should be added to the above reaction if construction equipment is allowed on the bridge before pouring the backwall (Stage II).

Maximum reaction for Final Stage:
Including the dynamic load allowance (for design of the pile cap top portion of the piles):

$$
\begin{aligned}
\mathrm{P}_{\mathrm{FNL}(\mathrm{I})} & =1.25(\mathrm{DC})+1.50(\mathrm{DW})+1.75(\mathrm{LL}+\mathrm{IM})\left(\mathrm{N}_{\text {lanes }}\right) / \mathrm{N}_{\text {girders }} \\
& =1.25(126.4+8.9)+1.5(12.0)+1.75[1.33(64.42)+30.81](4) / 6 \\
& =323 \mathrm{k}
\end{aligned}
$$

Without the dynamic load allowance (for design of the lower portion of the piles):

$$
\mathrm{P}_{\mathrm{FNL}(\mathrm{I})}=298.3 \mathrm{k}
$$

Factored dead load plus live load reactions for one exterior girder, Strength I limit state controls:

Maximum reaction Stage I:

$$
\begin{aligned}
\mathrm{P}_{\mathrm{SI}(\mathrm{E})} & =1.25(117.9) \\
& =147.4 \mathrm{k}
\end{aligned}
$$

Typically, integral abutments may be supported on end bearing piles or friction piles. Reinforced and prestressed concrete piles, concrete-filled steel pipe piles or steel H-piles may be used. Steel H-piles will be used in this example.

Typically, the minimum distance between the piles and the end of the abutment, measured along the skew, is taken as 1 '-6" and the maximum distance is usually 2 '-6". These distances may vary from one jurisdiction to another. The piles are assumed to be embedded 1'-6"into the abutment. Maximum pile spacing is assumed to be 10 ft . The minimum pile spacing requirements of S10.7.1.5 shall apply.

- From S10.7.1.5, the center-to-center pile spacing shall not be less than the greater of 30.0 in. or 2.5 pile diameters (or widths). The edge distance from the side of any pile to the nearest edge of the footing shall be greater than 9.0 in .
- According to S10.7.1.5, where a reinforced concrete beam is cast-in-place and used as a bent cap supported by piles, the concrete cover at the sides of the piles shall be greater than 6.0 in., plus an allowance for permissible pile misalignment, and the piles shall project at least 6.0 in. into the cap. This provision is specifically for bent caps, therefore, keep 1'-6" pile projection for integral abutment to allow the development of moments in the piles due to movements of the abutment without distressing the surrounding concrete.

From Figure 7.1-2, steel H-piles are shown to be driven with their weak axis perpendicular to the centerline of the beams. As discussed earlier, piles were also successfully driven with their strong axis perpendicular to the centerline of the beams in the past.

According to S10.7.4.1, the structural design of driven concrete, steel, and timber piles must be in accordance with the provisions of Sections S5, S6, and S8 respectively. Articles S5.7.4, S5.13.4, S6.15, S8.4.13, and S8.5.2.2 contain specific provisions for concrete, steel, and wood piles. Design of piles supporting axial load only requires an allowance for unintended eccentricity. For the steel Hpiles used in this example, this has been accounted for by the resistance factors in S6.5.4.2 for steel piles.

## General pile design

As indicated earlier, piles in this example are designed for gravity loads only.
Generally, the design of the piles is controlled by the minimum capacity as determined for the following cases:

- Case A-Capacity of the pile as a structural member according to the procedures outlined in S6.15. The design for combined moment and axial force will be based on an analysis that takes the effect of the soil into account.
- Case B-Capacity of the pile to transfer load to the ground.
- Case C-Capacity of the ground to support the load.

For piles on competent rock, only Case A needs to be investigated.

## Design Step

7.1.3.1

Pile compressive resistance (S6.15 and S6.9.2)
The factored resistance of components in compression, $\mathrm{P}_{\mathrm{r}}$, is taken as:

$$
\begin{equation*}
P_{r}=\varphi P_{n} \tag{S6.9.2.1-1}
\end{equation*}
$$

where:
$\mathrm{P}_{\mathrm{n}}=$ nominal compressive resistance specified in S6.9.4 and S6.9.5 (kip)
$\varphi_{c}=$ resistance factor for axial compression, steel only as specified in S6.5.4.2
$=0.5$ for H -piles assuming severe driving conditions
Check the width/thickness requirements per S6.9.4.2. Assume HP12x53 piles.
Slenderness of plates must satisfy:

$$
\begin{equation*}
\frac{\mathrm{b}}{\mathrm{t}} \leq \mathrm{k} \sqrt{\frac{\mathrm{E}}{\mathrm{~F}_{\mathrm{y}}}} \tag{S6.9.4.2-1}
\end{equation*}
$$

where:
$\mathrm{k}=$ plate buckling coefficient as specified in Table S6.9.4.2-1
$=0.56$ for flanges and projecting legs or plates
b = width of plate equals one-half of flange width as specified in Table S6.9.4.2-1 (in.)

$$
=12.045 / 2
$$

$$
=6.02 \mathrm{in} .
$$

$\mathrm{t}=$ flange thickness (in.)
$=0.435 \mathrm{in}$.

$$
\begin{aligned}
\frac{\mathrm{b}}{\mathrm{t}} & =6.02 / 0.435 \\
& =13.8
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{k} \sqrt{\frac{\mathrm{E}}{\mathrm{~F}_{\mathrm{y}}}} & =0.56 \sqrt{\frac{29,000}{36}} \\
& =15.9>13.8
\end{aligned}
$$

Therefore, use S6.9.4.1 to calculate the compressive resistance.
(Notice that the b/t ratio for the webs of HP sections is always within the limits of Table S6.9.4.2-1 for webs and, therefore, need not be checked.)

For piles fully embedded in soil, the section is considered continuously braced and Eq. S6.9.4.1-1 is reduced to $P_{n}=F_{y} A_{s}$.

$$
\begin{aligned}
\mathrm{P}_{\mathrm{n}} & =36(15.5) \\
& =558 \mathrm{k}
\end{aligned}
$$

Therefore, the factored resistance of components in compression, $\mathrm{P}_{\mathrm{r}}$, is taken as:

$$
\begin{aligned}
\mathrm{P}_{\mathrm{r}} & =\varphi \mathrm{P}_{\mathrm{n}} \\
& =0.5(558) \\
& =279 \mathrm{k}
\end{aligned}
$$

The above capacity applies to the pile at its lower end where damage from driving may have taken place. At the top of the pile, higher resistance factors that do not account for damage may be used. For piles designed for gravity loads only, as in this example, the resistance at the lower end will always control due to the lower resistance factor regardless if the dynamic load allowance is considered in determining the load at the top of the pile or not (notice that the dynamic load allowance is not considered in determining the load at the bottom of the pile).

## Design Step

Determine the number of piles required
Maximum total girder reactions for Stage I (detailed calculations of girder reactions shown earlier):

$$
\begin{aligned}
\mathrm{P}_{\mathrm{SI}(\text { Total })} & =2(147.4)+4(158) \\
& =926.8 \mathrm{k}
\end{aligned}
$$

Maximum total girder reaction for final stage not including the dynamic load allowance (detailed calculations of girder reactions shown earlier):

$$
\begin{aligned}
\mathrm{P}_{\mathrm{FNL}(\text { Total })} & =2(281.8)+4(298.3) \\
& =1,756.8 \mathrm{k}
\end{aligned}
$$

Maximum factored DL + LL on the abutment, Strength I limit state controls:

$$
\begin{aligned}
\mathrm{P}_{\text {Str.I }}= & \mathrm{P}_{\mathrm{FNL}(\text { Total) }}+1.25(\mathrm{DC})+1.50(\mathrm{DW})+1.75\left(\mathrm{LL}_{\text {max }}\right)\left(\mathrm{N}_{\text {lanes }}\right) \\
= & 1,756.8+1.25(86.0+187.4+50.4+23.65+155.5)+1.5(17.2) \\
& +1.75(8.0)(4) \\
= & 1,756.8+710.5 \\
= & 2,467 \mathrm{k}
\end{aligned}
$$

where:
" $\mathrm{P}_{\mathrm{FNL} \text { (Total)" }}$ is the total factored $\mathrm{DL}+\mathrm{LL}$ reaction of the bridge girders on the abutment.
"DC" includes the weight of the pile cap, diaphragm, wingwalls, approach slab and parapet on the wingwalls.
"DW" includes the weight of the future wearing surface on the approach slab.
"LL $L_{\text {max }}$ " is the live load reaction from the approach slab transferred to the abutment (per lane)
' $\mathrm{N}_{\text {lanes }}$ " is the maximum number of traffic lanes that fit on the approach slab, 4 lanes.

Therefore, the number of piles required to resist the applied dead and live loads is:

$$
\begin{aligned}
\mathrm{N}_{\text {piles }} & =\mathrm{P}_{\text {Str.I }} / \mathrm{P}_{\mathrm{r}} \\
& =2,467 / 279 \\
& =8.84 \text { piles, say } 9 \text { piles }
\end{aligned}
$$

## Design Step

Pile spacing
Total length of the pile cap $=58.93 \mathrm{ft}$.
Assume pile spacing is 6 ' $-11^{\prime \prime}$ ( 6.917 ft .) which provides more than the recommended edge distance of 1 '- 6 " for the piles.

$$
\begin{aligned}
\text { Pile end distance } & =[58.93-8(6.917)] / 2 \\
& =1.80 \mathrm{ft} .\left(1^{\prime}-91 / 2{ }^{\prime \prime}\right)
\end{aligned}
$$

## Design Step

## Backwall design

7.1.4

The thickness of the abutment backwall is taken to be 3 ft .
Design of the pier cap for gravity loads
For an integral abutment constructed in two stages, the abutment is designed to resist gravity loads as follows:

- Case A - The first stage of the abutment, i.e., the part of the abutment below the bearing pads, is designed to resist the self weight of the abutment, including the diaphragm, plus the reaction of the girders due to the self weight of the girder plus the deck slab and haunch.
- Case B - The entire abutment beam, including the diaphragm, is designed under the effect of the full loads on the abutment.

Instead of analyzing the abutment beam as a continuous beam supported on rigid supports at pile locations, the following simplification is common in conducting these calculations and is used in this example:

- Calculate moments assuming the abutment beam acting as a simple span between piles and then taking $80 \%$ of the simple span moment to account for the continuity. The location of the girder reaction is often assumed at the midspan for moment calculations and near the end for shear calculations. This assumed position of the girders is meant to produce maximum possible load effects. Due to the relatively large dimensions of the pile cap, the required reinforcement is typically light even with this conservative simplification.


## Required information:

Concrete compressive strength, $\mathrm{f}_{\mathrm{c}}=3 \mathrm{ksi}$
Reinforcing steel yield strength, $\mathrm{F}_{\mathrm{y}}=60 \mathrm{ksi}$
Pile spacing $=6.917 \mathrm{ft}$.

## CASE A

The maximum factored load due to the girders and slab (from the interior girder):

$$
\begin{aligned}
\mathrm{P}_{\mathrm{u}} & =1.5(126.4) \\
& =189.6 \mathrm{k}
\end{aligned}
$$

Factored load due to the self weight of the pile cap and diaphragm:

$$
\begin{aligned}
\mathrm{w}_{\mathrm{u}} & =1.5(1.46+3.18) \\
& =6.96 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Notice that only dead loads exist at this stage. The 1.5 load factor in the above equations is for Strength III limit state, which does not include live loads.

## Flexural design for Case A

The maximum positive moment, $\mathrm{M}_{\mathrm{t}}$, assuming a simple span girder, is at midspan between piles. The simple span moments are reduced by $20 \%$ to account for continuity:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{u}} & =\mathrm{P}_{\mathrm{u}}\left|/ 4+\mathrm{w}_{\mathrm{u}}\right|^{2} / 8 \\
& =0.8\left[189.6(6.917) / 4+6.96(6.917)^{2} / 8\right] \\
& =295.6 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Determine the required reinforcing at the bottom of the pile cap.

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

The nominal flexural resistance, $\mathrm{M}_{\mathrm{n}}$, is calculated using Eq. (S5.7.3.2.2-1).

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}}= & \text { area of nonpresstressed tension reinforcement }\left(\text { in }^{2}\right) \text {, notice that } \\
& \text { available room will only allow four bars, two on either side of the } \\
& \text { piles. Use } 4 \# 8 \text { bars. } \\
= & 4(0.79) \\
= & 3.16 \mathrm{in}^{2} \\
\mathrm{f}_{\mathrm{y}}= & \text { specified yield strength of reinforcing bars (ksi) } \\
= & 60 \mathrm{ksi}
\end{aligned}
$$

$d_{s}=$ distance from the extreme compression fiber to the centroid of the nonprestressed tensile reinforcement (in.)
$=$ depth of pile cap - bottom cover $-1 / 2$ diameter bar
$=3.25(12)-3-1 / 2(1.0)$

$$
=35.5 \mathrm{in} .
$$

$\mathrm{a}=c \beta_{1}$, depth of the equivalent stress block (in.)
$=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{b}$
(S5.7.3.1.1-4)
$=3.16(60) /[0.85(3)(3.0)(12)]$
$=2.07 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{M}_{\mathrm{n}} & =3.16(60)(35.5-2.07 / 2) / 12 \\
& =544.5 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(544.5) \\
& =490 \mathrm{k}-\mathrm{ft}>\mathrm{M}_{\mathrm{u}}=295.6 \mathrm{k}-\mathrm{ft} \mathbf{O K}
\end{aligned}
$$

Negative moment over the piles is taken equal to the positive moment. Use the same reinforcement at the top of the pile cap as determined for the bottom (4 \#8 bars).

By inspection:

- $M_{r}>4 / 3\left(M_{u}\right)$. This means the minimum reinforcement requirements of S5.7.3.3.2 are satisfied.
- The depth of the compression block is small relative to the section effective depth. This means that the maximum reinforcement requirements of S5.7.3.3.1 are satisfied.


## Shear design for Case A

The maximum factored shear due to the construction loads assuming the simple span condition and girder reaction at the end of the span:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{u}} & =\mathrm{P}_{\mathrm{u}}+\mathrm{w}_{\mathrm{u}} / 2 \\
& =189.6+6.96(6.917) / 2 \\
& =213.7 \mathrm{k}
\end{aligned}
$$

The factored shear resistance, $\mathrm{V}_{\mathrm{r}}$, is calculated as:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{r}}=\varphi \mathrm{V}_{\mathrm{n}} \tag{S5.8.2.1-2}
\end{equation*}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is calculated according to S 5.8 .3 .3 and is the lesser of:

$$
\begin{equation*}
V_{n}=V_{c}+V_{s} \tag{S5.8.3.3-1}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}}=0.25 \mathrm{f}_{\mathrm{c}} \mathrm{~b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \tag{S5.8.3.3-2}
\end{equation*}
$$

where:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{{ }_{\mathrm{c}}^{\mathrm{b}}} \mathrm{~b}_{\mathrm{v}} \tag{S5.8.3.3-3}
\end{equation*}
$$

$\beta=$ factor indicating ability of diagonally cracked concrete to transmit tension as specified in S5.8.3.4

$$
=2.0
$$

$\mathrm{f}_{\mathrm{c}}^{\prime}=$ specified compressive strength of the concrete (ksi)

$$
=3.0 \mathrm{ksi}
$$

$\mathrm{b}_{\mathrm{v}}=$ effective shear width taken as the minimum web width within the depth $\mathrm{d}_{\mathrm{v}}$ as determined in S5.8.2.9 (in.)
$=36$ in.
$\mathrm{d}_{\mathrm{v}}=$ effective shear depth as determined in S5.8.2.9 (in.)
S5.8.2.9 states that $\mathrm{d}_{\mathrm{v}}$ is not to be taken less than the greater of $0.9 \mathrm{~d}_{\mathrm{e}}$ or 0.72h

$$
\begin{aligned}
\mathrm{d}_{\mathrm{v}} & =\mathrm{d}_{\mathrm{e}}-\mathrm{a} / 2 \\
& =35.5-(2.07 / 2) \\
& =34.47 \mathrm{in} . \\
0.9 \mathrm{~d}_{\mathrm{e}} & =0.9(35.5) \\
& =31.95 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
0.72 \mathrm{~h} & =0.72[3.25(12)] \\
& =28.08 \mathrm{in.}
\end{aligned}
$$

Therefore, $\mathrm{d}_{\mathrm{v}}$ should be taken as 34.47 in .

$$
\begin{aligned}
\mathrm{V}_{\mathrm{c}} & =0.0316(2.0) \sqrt{3}(36)(34.47) \\
& =135.8 \mathrm{k}
\end{aligned}
$$

Assuming shear reinforcement is \#5 @ 10 in . spacing perpendicular to the pier cap longitudinal axis.

$$
\begin{equation*}
\mathrm{V}_{\mathrm{s}}=\mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{~d}_{\mathrm{v}} / \mathrm{s} \tag{S5.8.3.3-4}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \mathrm{A}_{\mathrm{v}}=\text { area of shear reinforcement within a distance " } \mathrm{s} \text { " }\left(\mathrm{in}^{2}\right) \\
&=2 \operatorname{legs}(0.31) \\
&=0.62 \mathrm{in}^{2} \\
& \mathrm{~s}=\text { spacing of stirrups (in. }) \\
&=10 \mathrm{in} . \\
& \begin{aligned}
\mathrm{V}_{\mathrm{s}} & =0.62(60)(34.47) / 10 \\
& =128.2 \mathrm{k}
\end{aligned}
\end{aligned}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is taken as the smaller of:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =135.8+128.2 \\
& =264 \mathrm{k}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =0.25(3)(36)(34.47) \\
& =930.7 \mathrm{k}
\end{aligned}
$$

Therefore, use the shear resistance due to the concrete and transverse steel reinforcement.

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(264) \\
& =237.6 \mathrm{k}>\mathrm{V}_{\mathrm{u}}=213.7 \mathrm{k} \text { OK }
\end{aligned}
$$

## CASE B

The maximum factored load due to all applied dead and live loads which include the approach slab, live load on approach slab, etc. The load due to the wingwalls is not included since its load minimally affects the responses at the locations where girder reactions are applied.

Point load:

$$
\begin{aligned}
\mathrm{P}_{\text {Str- }} & =\text { maximum factored girder reaction calculated earlier } \\
& =323 \mathrm{k}
\end{aligned}
$$

Notice that the 323 k assumes that the live load is distributed equally to all girders. This approximation is acceptable since this load is assumed to be applied at the critical location for moment and shear. Alternately, the maximum reaction from the tables in Section 5.3 may be used.

Distributed load:

$$
\begin{aligned}
\mathrm{w}_{\text {Str }-\mathrm{I}}= & 1.25(\text { cap self wt. }+ \text { end diaph. }+ \text { approach slab })+1.5(\text { approach FWS })+ \\
& 1.75(\text { approach slab lane load })\left(\mathrm{N}_{\text {lanes }} / \mathrm{L}_{\text {abutment }}\right. \\
= & 1.25(1.46+3.18+2.81)+1.5(0.31)+1.75(8.0)(4) / 58.93 \\
= & 10.73 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

## Flexural design for Case B

The maximum positive moment is calculated assuming the girder reaction is applied at the midspan between piles and taking $80 \%$ of the simple span moment.

$$
\begin{aligned}
\mathrm{M}_{\mathrm{u}} & =0.8\left[323(6.917) / 4+10.73(6.917)^{2} / 8\right] \\
& =498.2 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Determine the required reinforcing at the bottom of the pile cap.

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

where:

$$
\begin{align*}
& \mathrm{A}_{\mathrm{s}}=\text { use } 4 \# 8 \text { bars } \\
&=4(0.79) \\
&=3.16 \text { in }^{2} \\
& \mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi} \\
& \\
& \mathrm{~d}_{\mathrm{s}}=\text { total depth of int. abut. (no haunch) - bottom cover }-1 / 2 \text { bar diameter } \\
&=119.75-3-1 / 2(1.0) \\
&=116.25 \mathrm{in} .  \tag{S5.7.3.1.1-4}\\
& \\
& \mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{b} \\
&=3.16(60) /[0.85(3)(3.0)(12)] \quad(\mathrm{S} 5.7 .3 .1 .1-4)
\end{align*}
$$

$$
\begin{aligned}
& =2.07 \mathrm{in} . \\
& \mathrm{M}_{\mathrm{n}}=3.16(60)(116.25-2.07 / 2) / 12 \\
& =1,820 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(1,820) \\
& =1,638 \mathrm{k}-\mathrm{ft}>\mathrm{M}_{\mathrm{u}}=498.2 \mathrm{k}-\mathrm{ft} \text { OK }
\end{aligned}
$$

Negative moment over the piles is taken equal to the positive moment. Use the same reinforcement at the top of the abutment beam as determined for the bottom (4 \#8 bars).

By inspection:

- $M_{r}>4 / 3\left(M_{u}\right)$.
- The depth of the compression block is small relative to the section effective depth.


## Shear design for Case B

Assume the girder reaction is adjacent to the pile.
The maximum factored shear due to all applied loading:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{u}} & =\mathrm{P}_{\mathrm{u}}+\mathrm{w}_{\mathrm{u}} \mathrm{l} / 2 \\
& =323+10.73(6.917) / 2 \\
& =360.1 \mathrm{k}
\end{aligned}
$$

The factored shear resistance, $\mathrm{V}_{\mathrm{r}}$, is calculated as:

$$
\begin{equation*}
V_{r}=\varphi V_{n} \tag{S5.8.2.1-2}
\end{equation*}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is calculated according to S5.8.3.3 and is the lesser of:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}}=\mathrm{V}_{\mathrm{c}}+\mathrm{V}_{\mathrm{s}} \tag{S5.8.3.3-1}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}}=0.25 f_{\mathrm{c}}^{\prime} \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \tag{S5.8.3.3-2}
\end{equation*}
$$

where:

$$
\begin{align*}
& \mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{\mathrm{~F}_{\mathrm{c}}^{\mathrm{b}}} \mathrm{~d}_{\mathrm{v}}  \tag{S5.8.3.3-3}\\
& \beta=2.0
\end{align*}
$$

$$
\begin{aligned}
f_{c}^{\prime} & =3.0 \mathrm{ksi} \\
\mathrm{~b}_{\mathrm{v}} & =36 \mathrm{in} . \\
\mathrm{d}_{\mathrm{v}} & =\mathrm{d}_{\mathrm{e}}-\mathrm{a} / 2 \\
\mathrm{~d}_{\mathrm{e}} & =116.25 \text { in. (calculated earlier) } \\
\mathrm{d}_{\mathrm{v}} & =116.25-(2.07 / 2) \\
& =115.2 \mathrm{in} . \\
0.9 \mathrm{~d}_{\mathrm{e}} & =0.9(116.25) \\
& =104.6 \mathrm{in} . \\
0.72 \mathrm{~h} & =0.72(119.75) \\
& =86.22 \mathrm{in} .
\end{aligned}
$$

Therefore, $\mathrm{d}_{\mathrm{v}}$ should be taken as 115.2 in.
The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is taken as the lesser of:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{c}} & =0.0316(2.0) \sqrt{3}(36)(115.2) \\
& =454.0 \mathrm{k}
\end{aligned}
$$

Notice that $\mathrm{V}_{\mathrm{c}}$ is large enough, relative to the applied load, that the contribution of the transverse shear reinforcement, $\mathrm{V}_{\mathrm{s}}$, is not needed.

OR

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =0.25(3)(36)(115.2) \\
& =3,110.4 \mathrm{k}
\end{aligned}
$$

Therefore, use the shear resistance due to the concrete, $\mathrm{V}_{\mathrm{c}}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(454.0) \\
& =408.6 \mathrm{k}>\mathrm{V}_{\mathrm{u}}=360.1 \mathrm{k} \mathrm{OK}
\end{aligned}
$$

Typical reinforcement details of the abutment beam are shown in Figures 7.1-4 through 7.1-7. Notice that bar shapes vary depending on the presence of girders and/or piles at the section.


Figure 7.1-4 - Integral Abutment Reinforcement, Girder and Pile Exist at the Same Section


Figure 7.1-5 - Integral Abutment Reinforcement, No Girder and No Pile at the Section


Figure 7.1-6 - Integral Abutment Reinforcement, Girder, No Pile at the Section


Figure 7.1-7 - Integral Abutment Reinforcement, Pile Without Girder

Design Step 7.1.4.1

Design the backwall as a horizontal beam resisting passive earth pressure

$10^{\prime}-77 / 16^{\prime \prime}=10.287 '$

Figure 7.1-8 - Passive Earth Pressure Applied to Backwall

Calculate the adequacy of the backwall to resist passive pressure due to the abutment backfill material.

Passive earth pressure coefficient, $\mathrm{k}_{\mathrm{p}}=(1+\sin \phi) /(1-\sin \phi)$
(Notice that $\mathrm{k}_{\mathrm{p}}$ may also be obtained from Figure S3.11.5.4-1)

$$
\begin{equation*}
w_{p}=1 / 2 \gamma z^{2} k_{p} \tag{S3.11.5.1-1}
\end{equation*}
$$

where:
$w_{p}=$ passive earth pressure per unit length of backwall (k/ft)
$\gamma=$ unit weight of soil bearing on the backwall (kcf)
$=0.130 \mathrm{kcf}$
z = height of the backwall from the bottom of the approach slab to the bottom of the pile cap (ft.)
$=$ slab + haunch + girder depth + bearing pad thickness + pile cap depth - approach slab thickness
$=(8 / 12)+(4 / 12)+6+(0.75 / 12)+3.25-1.5$

$$
=8.81 \mathrm{ft} .
$$

$\phi=$ internal friction of backfill soil assumed to be $30^{\circ}$
$\mathrm{w}_{\mathrm{p}}=1 / 2(0.130)(8.81)^{2}[(1+\sin 30) /(1-\sin 30)]$
$=15.1 \mathrm{k} / \mathrm{ft}$ of wall
Notice that developing full passive earth pressure requires relatively large displacement of the structure ( 0.01 to 0.04 of the height of the structure for cohesionless fill). The expected displacement of the abutment is typically less than that required to develop full passive pressure. However, these calculations are typically not critical since using full passive pressure is not expected to place high demand on the structure or cause congestion of reinforcement.

No load factor for passive earth pressure is specified in the LRFD specifications. Assume the load factor is equal to that of the active earth pressure $(\varphi=1.5)$.

$$
\begin{aligned}
\mathrm{w}_{\mathrm{u}} & =\varphi_{\mathrm{EH}} \mathrm{w}_{\mathrm{p}} \\
& =1.5(15.1) \\
& =22.65 \mathrm{k} / \mathrm{ft} \text { of wall }
\end{aligned}
$$

The backwall acts as a continuous horizontal beam supported on the girders, i.e., with spans equal to the girder spacing along the skew.

$$
\begin{aligned}
\mathrm{M}_{\mathrm{u}} & \cong \mathrm{w}_{\mathrm{u}} \mathrm{l}^{2} / 8 \\
& =22.65(9.667 / \cos 20)^{2} / 8 \\
& =300 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Calculate the nominal flexural resistance, $\mathrm{M}_{\mathrm{r}}$, of the backwall.

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

where:
$\mathrm{A}_{\mathrm{s}}=$ area of the longitudinal reinforcement bars at front face (tension side) of the abutment (9 \#6 bars)
$=9(0.44)$
$=3.96 \mathrm{in}^{2}$
$\mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi}$
$d_{s}=$ width of backwall - concrete cover - vertical bar dia. $-1 / 2$ bar dia.
$=3.0(12)-3-0.625-1 / 2(0.75)$
$=32.0 \mathrm{in}$.
$\mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{b}$
where " $b$ " is the height of the component
$=3.96(60) /[0.85(3)(119.75)]$
$=0.78 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{M}_{\mathrm{n}} & =3.96(60)(32.0-0.78 / 2) / 12 \\
& =626 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Therefore, the factored flexural resistance, where $\varphi=0.9$ for flexure (S5.5.4.2.1), is taken as:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(626) \\
& =563 \mathrm{k}-\mathrm{ft} / \mathrm{ft}>\mathrm{M}_{\mathrm{u}}=300 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \mathbf{O K}
\end{aligned}
$$

By inspection:

- $M_{r}>4 / 3\left(M_{u}\right)$.
- The depth of the compression block is small relative to the depth.

Check shear for the section of backwall between girders:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{u}} & =\mathrm{P}_{\mathrm{u}} \mathrm{I} / 2 \\
& =22.65(9.667 / \sin 20) / 2 \\
& =116.5 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

The factored shear resistance, $\mathrm{V}_{\mathrm{r}}$, is calculated as:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{r}}=\varphi \mathrm{V}_{\mathrm{n}} \tag{S5.8.2.1-2}
\end{equation*}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, is calculated according to S5.8.3.3 and is the lesser of:

$$
\begin{equation*}
V_{\mathrm{n}}=\mathrm{V}_{\mathrm{c}}+\mathrm{V}_{\mathrm{s}} \tag{S5.8.3.3-1}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}}=0.25 \mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \tag{S5.8.3.3-2}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{c}} & =0.0316 \beta \sqrt{\mathrm{~F}_{\mathrm{c}} \mathrm{~b}} \mathrm{~d}_{\mathrm{v}} \\
\beta & =2.0 \\
\mathrm{f}_{\mathrm{c}}^{\prime} & =3.0 \mathrm{ksi} \\
\mathrm{~b}_{\mathrm{v}} & =\text { effective horizontal beam width taken as the abutment depth (in.) } \\
& =119.75 \mathrm{in} . \\
\mathrm{d}_{\mathrm{v}} & =\mathrm{d}_{\mathrm{e}}-\mathrm{a} / 2 \\
& =32.0-(0.78 / 2) \\
& =31.61 \mathrm{in} . \\
0.9 \mathrm{~d}_{\mathrm{e}} & =0.9(32.0) \\
& =28.8 \mathrm{in} . \\
0.72 \mathrm{~h} & =0.72(36) \\
& =25.92 \mathrm{in} .
\end{aligned}
$$

Therefore, $\mathrm{d}_{\mathrm{v}}$ should be taken as 31.61 in .
Ignore the contribution of the transverse reinforcement to the shear resistance (i.e., $\mathrm{V}_{\mathrm{s}}=$ $0), \mathrm{V}_{\mathrm{n}}$ is taken as the smaller of:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{c}} & =0.0316(2.0) \sqrt{3}(119.75)(31.61) \\
& =414.4 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =0.25(3)(119.75)(31.61) \\
& =2,839 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Therefore, use the shear resistance due to the concrete, $\mathrm{V}_{\mathrm{c}}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(414.4) \\
& =373.0 \mathrm{k} / \mathrm{ft}>\mathrm{V}_{\mathrm{u}}=116.5 \mathrm{k} / \mathrm{ft} \quad \mathbf{O K}
\end{aligned}
$$

## Design Step

Wingwall design
There is no widely accepted method of determining design loads for the wingwalls of integral abutments. The following design procedure will result in a conservative design as it takes into account maximum possible loads.

Two load cases are considered:
Load Case 1:
The wingwall is subjected to passive earth pressure. This case accounts for the possibility of the bridge moving laterally and pushing the wingwall against the fill. It is not likely that the displacement will be sufficient to develop full passive pressure. However, there is no available method to determine the expected pressure with certainty. This load case is considered under strength limit state.

Load Case 2:
The wingwall is subjected to active pressure and collision load on the parapet. Active pressure was considered instead of passive to account for the low probability that a collision load and passive pressure will exist simultaneously. This load case is considered at the extreme event limit state, i.e. $\varphi=1.0$ (Table S3.4.1-1)

Required information:
Angle of internal friction of fill, $\phi \quad=30$ degrees
Coefficient of active earth pressure, $\mathrm{k}_{\mathrm{a}}=(1-\sin \phi) /(1+\sin \phi)$

$$
=0.333
$$

Coefficient of passive earth pressure, $\mathrm{k}_{\mathrm{p}}=(1+\sin \phi) /(1-\sin \phi)$

$$
=3
$$

$\mathrm{k}_{\mathrm{a}} / \mathrm{k}_{\mathrm{p}}$
$=0.333 / 3$
$=0.111$

## $\underline{\text { Load Case } 1}$

From Figure 7.1-9 and utilizing properties of a right angle pyramid [volume $=1 / 3$ (base area)(height) and the center of gravity (applied at a distance measured from the vertical leg of the right angle pyramid) $=1 / 4$ base length].

Moment at the critical section for moment under passive pressure:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{p}} & =0.2(14)(0.5)(14 / 2)+0.2[14(8.31 / 2)](14 / 3)+(1 / 3)[3.24(8.31)(14 / 2)](14 / 4) \\
& =284 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Minimum required factored flexural resistance, $\mathrm{M}_{\mathrm{r}}=284 \mathrm{k}-\mathrm{ft}$.

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{n}} & =\text { nominal resistance (k-ft) } \\
& =\mathrm{M}_{\mathrm{p}} \\
\varphi & =0.9 \text { for flexure at the strength limit state (S5.5.4.2) }
\end{aligned}
$$

Min. required $\mathrm{M}_{\mathrm{n}}=284 / 0.9$

$$
=316 \mathrm{k}-\mathrm{ft}
$$

## $\underline{\text { Load Case } 2}$

Moment on the critical section for moment under active pressure:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{a}} & =0.111(284) \\
& =31.5 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Moment from collision load on the parapet:
From SA13.2 for Test Level 5, the crash load on the parapet is equal to 124 kips and is applied over a length of 8 ft .

Maximum collision moment on the critical section:

$$
\begin{aligned}
\mathrm{M} & =124(14-8 / 2) \\
& =1,240 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Total moment for Load Case 2, $\mathrm{M}_{\text {total }}=1,240+31.5$

$$
=1,271.5 \mathrm{k}-\mathrm{ft}
$$

The minimum required factored flexural resistance, $\mathrm{M}_{\mathrm{r}}=1,271.5 \mathrm{k}-\mathrm{ft}$

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

where:
$\varphi=1.0$ for flexure at the extreme event limit state
Min. required $\mathrm{M}_{\mathrm{n}}=1,271.5 / 1.0$

$$
=1,271.5 \mathrm{k}-\mathrm{ft}
$$

From the two cases of loading:

$$
\mathrm{M}_{\mathrm{n}} \text { required }=1,271.5 \mathrm{k}-\mathrm{ft}
$$

Develop a section that provides the minimum nominal flexural resistance
Required information:
Assuming reinforcement of \#8 @ 6 in.
Number of bars within the 10.3125 ft . height of the wing wall $=22$ bars
Section thickness = parapet thickness at base

$$
=20.25 \mathrm{in} .
$$

Concrete cover $=3 \mathrm{in}$.

The nominal flexural resistance, $\mathrm{M}_{\mathrm{n}}$, is taken as:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{d}_{\mathrm{s}} & =\text { section thickness }- \text { cover }-1 / 2 \text { bar diameter } \\
& =20.25-3-1 / 2(1.0) \\
& =16.75 \mathrm{in} .
\end{aligned}
$$

$$
\mathrm{A}_{\mathrm{s}}=22(0.79)
$$

$$
=17.38 \mathrm{in}^{2}
$$

$$
\begin{equation*}
\mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{~b} \tag{S5.7.3.1.1-4}
\end{equation*}
$$

$$
=17.38(60) /[0.85(3)(123.75)]
$$

$$
=3.30 \mathrm{in}
$$

$$
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right)
$$

$$
=17.38(60)(16.75-3.30 / 2) / 12
$$

$$
=1,312 \mathrm{k}-\mathrm{ft}>1,271.5 \mathrm{k} \text { - } \mathrm{ft} \text { required } \mathbf{O K}
$$

Secondary reinforcement of the wingwall is not by design, it is only meant for shrinkage. Use \#6 @ 12 in. spacing as shown in Figure 7.1-10.


Figure 7.1-9 - Wingwall Dimensions


Figure 7.1-10 - Wingwall Reinforcement

## Design Step Design of approach slab

7.1.6

Approach slab loading for a 1 ft . wide strip:

$$
\begin{aligned}
\mathrm{w}_{\text {self }} & =0.15(1.5) \\
& =0.225 \mathrm{k} / \mathrm{ft} \\
& \\
\mathrm{w}_{\mathrm{FWS}} & =0.025 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Factored distributed dead loading:

$$
\begin{aligned}
\mathrm{w}_{\mathrm{Str}} \mathrm{I} & =1.25(0.225)+1.50(0.025) \\
& =0.32 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Live load distribution width (S4.6.2.3)
The equivalent strip width of longitudinal strips per lane for both shear and moment is calculated according to the provisions of S4.6.2.3.

- For single lane loaded

$$
\begin{equation*}
\mathrm{E}=10+5 \sqrt{\mathrm{~L}_{1} \mathrm{~W}_{1}} \tag{S4.6.2.3-1}
\end{equation*}
$$

- For multiple lanes loaded

$$
\begin{equation*}
\mathrm{E}=84.0+1.44 \sqrt{\mathrm{~L}_{1} \mathrm{~W}_{2}} \leq \frac{12.0 \mathrm{~W}}{\mathrm{~N}_{\mathrm{L}}} \tag{S4.6.2.3-2}
\end{equation*}
$$

where:
$\mathrm{E}=$ equivalent width (in.)
$\mathrm{L}_{1}=$ modified span length taken equal to the lesser of the actual span or 60.0 ft . (ft.)
$\mathrm{W}_{1}=$ modified edge-to-edge width of bridge taken to be equal to the lesser of the actual width or 60.0 ft . for multilane lading, or 30.0 ft . for single-lane loading (ft.)
$\mathrm{W}=$ physical edge-to-edge width of bridge (ft.)
$\mathrm{N}_{\mathrm{L}}=$ number of design lanes as specified in S3.6.1.1.1

$$
\begin{aligned}
\mathrm{E}_{\text {single }} & =10+5 \sqrt{25(30)} \\
& =146.9 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
\begin{aligned}
\mathrm{E}_{\text {mult. }} & =84.0+1.44 \sqrt{25(55.34)} \\
& =137.6 \mathrm{in} .
\end{aligned} \\
\begin{aligned}
\frac{12.0(55.34)}{4} & =166.02 \mathrm{in} .
\end{aligned}
\end{aligned}
$$

Therefore, the equivalent strip width is:

$$
\mathrm{E}=137.6 \mathrm{in} .
$$

Live load maximum moment:
Lane load: max moment $=0.64(25)^{2} / 8$

$$
=50 \mathrm{k}-\mathrm{ft}
$$

Truck load: max moment $=207.4 \mathrm{k}-\mathrm{ft}$ (from live load analysis output for a 25 ft . simple span)

Total LL $+\mathrm{IM}=50+1.33(207.4)$

$$
=325.8 \mathrm{k}-\mathrm{ft}
$$

Total LL + IM moment per unit width of slab $=325.8 /(137.6 / 12)$

$$
=28.4 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
$$

Maximum factored positive moment per unit width of slab due to dead load plus live load:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{u}} & =\mathrm{wl}^{2} / 8+1.75(\mathrm{LL}+\mathrm{IM} \text { moment }) \\
& =0.32(25)^{2} / 8+1.75(28.4) \\
& =74.7 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

The factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, is taken as:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}(\mathrm{~d}-\mathrm{a} / 2) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}} & =\text { use } \# 9 \text { bars at } 9 \mathrm{in} . \text { spacing } \\
& =1.0(12 / 9) \\
& =1.33 \mathrm{in}^{2} \text { per one foot of slab } \\
\mathrm{f}_{\mathrm{y}} & =60 \mathrm{ksi}
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{d}=\text { slab depth }- \text { cover (cast against soil) }-1 / 2 \text { bar diameter } \\
&=1.5(12)-3-1 / 2(1.128) \\
&=14.4 \mathrm{in} . \\
& \mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{~b} \\
&=1.33(60) /[0.85(3)(12)] \quad(\text { S5.7.3.1.1-4) } \\
&=2.61 \mathrm{in} . \\
& \begin{aligned}
\mathrm{M}_{\mathrm{n}} & =1.33(60)(14.4-2.61 / 2) / 12 \\
& =87.1 \mathrm{k}-\mathrm{ft}
\end{aligned}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(87.1) \\
& =78.4 \mathrm{k}-\mathrm{ft}>\mathrm{M}_{\mathrm{u}}=74.7 \mathrm{k}-\mathrm{ft} \mathbf{O K}
\end{aligned}
$$

Bottom distribution reinforcement (S9.7.3.2)
For main reinforcement parallel to traffic, the minimum distribution reinforcement is taken as a percentage of the main reinforcement:

$$
100 / \sqrt{\mathrm{S}} \leq 50 \%
$$

where:
$\mathrm{S}=$ the effective span length taken as equal to the effective length specified in S9.7.2.3 (ft.)

Assuming " $S$ " is equal to the approach slab length,

$$
100 / \sqrt{25}=20 \%
$$

Main reinforcement: \#9 @ 9 in. = 1.0(12/9)

$$
=1.33 \mathrm{in}^{2} / \mathrm{ft}
$$

Required distribution reinforcement $=0.2(1.33)$

$$
=0.27 \mathrm{in}^{2} / \mathrm{ft}
$$

Use \#6 @ $12 \mathrm{in} .=0.44 \mathrm{in}^{2} / \mathrm{ft}>$ required reinforcement $\mathbf{O K}$


Figure 7.1-11 - Typical Approach Slab Reinforcement Details

## Design Step

7.1.7

Sleeper slab
No design provisions are available for sleeper slabs. The reinforcement is typically shown as a standard detail. If desired, moment in the sleeper slab may be determined assuming the wheel load is applied at the midpoint of a length assumed to bridge over settled fill, say a 5 ft. span length.


* Trowel smooth and place 2 layers of 4 mil. polyethylene sheeting as bond breaker

Figure 7.1-12 - Sleeper Slab Details Used by the Pennsylvania Department of Transportation

Design Step INTERMEDIATE PIER DESIGN<br>7.2<br>Design Step<br>7.2.1<br>Substructure loads and load application<br>In the following sections, the word "pier" is used to refer to the intermediate pier or intermediate bent.<br>Dead load

Notice that the LRFD specifications include a maximum and minimum load factor for dead load. The intent is to apply the maximum or the minimum load factors to all dead loads on the structure. It is not required to apply maximum load factors to some dead loads and minimum load factors smultaneously to other dead loads to obtain the absolute maximum load effects.

## Live load transmitted from the superstructure to the substructure

Accurately determining live load effects on intermediate piers always represented an interesting problem. The live load case of loading producing the maximum girder reactions on the substructure varies from one girder to another and, therefore, the case of loading that maximizes live load effects at any section of the substructure also varies from one section to another. The equations used to determine the girder live load distribution produce the maximum possible live load distributed to a girder without consideration to the live load distributed concurrently to the surrounding girders. This is adequate for girder design but is not sufficient for substructure design. Determining the concurrent girder reactions requires a three-dimensional modeling of the structure. For typical structures, this will be cumbersome and the return, in terms of more accurate results, is not justifiable. In the past, different jurisdictions opted to incorporate some simplifications in the application of live loads to the substructure and these procedures, which are independent of the design specifications, are still applicable under the AASHTO-LRFD design specifications. The goal of these simplifications is to allow the substructure to be analyzed as a two-dimensional frame. One common procedure is as follows:

- Live load reaction on the intermediate pier from one traffic lane is determined. This reaction from the live load uniform load is distributed over a 10 ft . width and the reaction from the truck is applied as two concentrated loads 6 ft. apart. This means that the live load reaction at the pier location from each traffic lane is a line load 10 ft. wide and two concentrated loads 6 ft. apart. The loads are assumed to fit within a 12 ft . wide traffic lane. The reactions from the uniform load and the truck may be moved within the width of the traffic lane, however, neither of the two truck axle loads may be placed closer than 2 ft . from the edge of the traffic lane.
- The live load reaction is applied to the deck at the pier location. The load is distributed to the girders assuming the deck acts as a series of simple spans
supported on the girders. The girder reactions are then applied to the pier. In all cases, the appropriate multiple presence factor is applied.
- First, one lane is loaded. The reaction from that lane is moved across the width of the bridge. To maximize the loads, the location of the 12 ft . wide traffic lane is assumed to move across the full width of the bridge between gutter lines. Moving the traffic lane location in this manner provides for the possibility of widening the bridge in the future and/or eliminating or narrowing the shoulders to add additional traffic lanes. For each load location, the girder reactions transmitted to the pier are calculated and the pier itself is analyzed.
- Second, two traffic lanes are loaded. Each of the two lanes is moved across the width of the bridge to maximize the load effects on the pier. All possible combinations of the traffic lane locations should be included.
- The calculations are repeated for three lanes loaded, four lanes loaded and so forth depending on the width of the bridge.
- The maximum and minimum load effects, i.e. moment, shear, torsion and axial force, at each section from all load cases are determined as well as the other concurrent load effects, e.g. maximum moment and concurrent shear and axial loads. When a design provision involves the combined effect of more than one load effect, e.g. moment and axial load, the maximum and minimum values of each load effect and the concurrent values of the other load effects are considered as separate load cases. This results in a large number of load cases to be checked. Alternatively, a more conservative procedure that results in a smaller number of load cases may be used. In this procedure, the envelopes of the load effects are determined. For all members except for the columns and footings, the maximum values of all load effects are applied simultaneously. For columns and footings, two cases are checked, the case of maximum axial load and minimum moment and the case of maximum moment and minimum axial load.

This procedure is best suited for computer programs. For hand calculations, this procedure would be cumbersome. In lieu of this lengthy process, a simplified procedure used satisfactorily in the past may be utilized.

Load combinations

The live load effects are combined with other loads to determine the maximum factored loads for all applicable limit states. For loads other than live, when maximum and minimum load factors are specified, each of these two factored loads should be considered as separate cases of loading. Each section is subsequently designed for the controlling limit state.

## Temperature and shrinkage forces

The effects of the change in superstructure length due to temperature changes and, in some cases, due to concrete shrinkage, are typically considered in the design of the substructure.

In addition to the change in superstructure length, the substructure member lengths also change due to temperature change and concrete shrinkage. The policy of including the effects of the substructure length change on the substructure forces varies from one jurisdiction to another. These effects on the pier cap are typically small and may be ignored without measurable effect on the design of the cap. However, the effect of the change in the pier cap length may produce a significant force in the columns of multiple column bents. This force is dependant on:

- The length and stiffness of the columns: higher forces are developed in short, stiff columns
- The distance from the column to the point of equilibrium of the pier (the point that does not move laterally when the pier is subjected to a uniform temperature change): Higher column forces develop as the point of interest moves farther away from the point of equilibrium. The point of equilibrium for a particular pier varies depending on the relative stiffness of the columns. For a symmetric pier, the point of equilibrium lies on the axis of symmetry. The column forces due to the pier cap length changes are higher for the outer columns of multi-column bents. These forces increase with the increase in the width of the bridge.


## Torsion

Another force effect that some computer design programs use in pier design is the torsion in the pier cap. This torsion is applied to the pier cap as a concentrated torque at the girder locations. The magnitude of the torque at each girder location is calculated differently depending on the source of the torque.

- Torque due to horizontal loads acting on the superstructure parallel to the bridge longitudinal axis: The magnitude is often taken equal to the horizontal load on the bearing under the limit state being considered multiplied by the distance from the point of load application to mid-height of the pier cap, e.g. braking forces are assumed to be applied 6 ft. above the deck surface.
- Torque due to noncomposite dead load on simple spans made continuous for live load: Torque at each girder location is taken equal to the difference between the product of the noncomposite dead load reaction and the distance to the mid-width of the cap for the two bearings under the girder line being considered.

According to SC5.8.2.1, if the factored torsional moment is less than one-quarter of the factored pure torsional cracking moment, it will cause only a very small reduction in
shear capacity or flexural capacity and, hence, can be neglected. For pier caps, the magnitude of the torsional moments is typically small relative to the torsional cracking moments and, therefore, is typically ignored in hand calculations.

For the purpose of this example, a computer program that calculates the maximum and minimum of each load effect and the other concurrent load effects was used. Load effects due to substructure temperature expansion/contraction and concrete shrinkage were not included in the design. The results are listed in Appendix C. Selected values representing the controlling case of loading are used in the sample calculations.

## Superstructure dead load

These loads can be obtained from Section 5.2 of the superstructure portion of this design example.

Summary of the unfactored loading applied vertically at each bearing (12 bearings total, 2 per girder line):

Girders (E/I) $\quad=61.6 \mathrm{k}$
Deck slab and haunch (E) $=55.1 \mathrm{k}$
Deck slab and haunch (I) $=62.2 \mathrm{k}$
Intermediate diaphragm $(\mathrm{E})=1.3 \mathrm{k}$
Intermediate diaphragm (I) $=2.5 \mathrm{k}$
Parapets (E/I)
$=14.8 \mathrm{k}$
Future wearing surface (E) $=13.4 \mathrm{k}$
Future wearing surface (I) $=19.9 \mathrm{k}$
(E) - exterior girder
(I) - interior girder

## Substructure dead load



Figure 7.2-1 - General Pier Dimensions

Pier cap unfactored dead load

$$
\mathrm{w}_{\text {cap }}=(\text { cap cross-sectional area)(unit weight of concrete })
$$

Varying cross-section at the pier cap ends:

$$
\begin{aligned}
\mathrm{w}_{\text {cap } 1}=\text { varies linearly from } 2(2)(0.150) & =0.6 \mathrm{k} / \mathrm{ft} \\
\text { to } 4(4)(0.150) & =2.4 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Constant cross-section:

$$
\begin{aligned}
\mathrm{w}_{\mathrm{cap} 2} & =4(4)(0.150) \\
& =2.4 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {cap }} & =2.4(45.75)+[(2+4) / 2](0.150)(13.167) \\
& =115.7 \mathrm{k}
\end{aligned}
$$

Single column unfactored dead load

$$
\begin{aligned}
\mathrm{w}_{\text {column }} & =(\text { column cross sectional area)(unit weight of concrete }) \\
& =\pi(1.75)^{2}(0.150) \\
& =1.44 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {column }} & =1.44(18) \\
& =25.9 \mathrm{k}
\end{aligned}
$$

## Single footing unfactored dead load

$$
\begin{aligned}
\mathrm{w}_{\text {footing }} & =(\text { footing cross sectional area })(\text { unit weight of concrete }) \\
& =12(12)(0.150) \\
& =21.6 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{P}_{\text {footing }} & =21.6(3) \\
& =64.8 \mathrm{k}
\end{aligned}
$$

## Live load from the superstructure

Use the output from the girder live load analysis to obtain the maximum unfactored live load reactions for the interior and exterior girder lines.

Summary of HL-93 live load reactions, without distribution factors or impact, applied vertically to each bearing (truck pair + lane load case governs for the reaction at the pier, therefore, the $90 \%$ reduction factor from S3.6.1.3.1 is applied):

Maximum truck $=59.5 \mathrm{k}$
Minimum truck $=0.0 \mathrm{k}$
Maximum lane $=43.98 \mathrm{k}$
Minimum lane $\quad=0.0 \mathrm{k}$

## Braking force (BR) (S3.6.4)

According to the specifications, the braking force shall be taken as the greater of:
25 percent of the axle weight of the design truck or design tandem
OR
5 percent of the design truck plus lane load or 5 percent of the design tandem plus lane load

The braking force is placed in all design lanes which are considered to be loaded in accordance with S3.6.1.1.1 and which are carrying traffic headed in the same direction. These forces are assumed to act horizontally at a distance of 6 ft . above the roadway surface in either longitudinal direction to cause extreme force effects. Assume the example bridge can be a one-way traffic bridge in the future. The multiple presence factors in S3.6.1.1.2 apply.

$$
\begin{aligned}
\mathrm{BR}_{1} & =0.25(32+32+8)(4 \text { lanes })(0.65) / 1 \text { fixed support } \\
& =46.8 \mathrm{k}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{BR}_{2 \mathrm{~A}} & =0.05[72+(110+110)(0.64)] \\
& =10.6 \mathrm{k} \\
\mathrm{BR}_{2 \mathrm{~B}} & =0.05[(25+25)+220(0.64)] \\
& =9.54 \mathrm{k}
\end{aligned}
$$

where the subscripts are defined as:
1 - use the design truck to maximize the braking force
2 A - check the design truck + lane
2 B - check the design tandem + lane
Therefore, the braking force will be taken as 46.8 k ( 3.9 k per bearing or 7.8 k per girder) applied 6 ft . above the top of the roadway surface.

$$
\begin{aligned}
\text { Moment arm } & =6 \mathrm{ft} .+ \text { deck thickness }+ \text { haunch }+ \text { girder depth } \\
& =6+0.667+0.333+6 \\
& =13.0 \mathrm{ft} . \text { above the top of the bent cap }
\end{aligned}
$$

Apply the moment 2(3.9)(13.0) $=101.4 \mathrm{k}$ - ft at each girder location.

## Wind load on superstructure (S3.8.1.2)

The pressures specified in the specifications are assumed to be caused by a base wind velocity, $V_{B}$, of 100 mph .

Wind load is assumed to be uniformly distributed on the area exposed to the wind. The exposed area is the sum of all component surface areas, as seen in elevation, taken perpendicular to the assumed wind direction. This direction is varied to determine the extreme force effects in the structure or in its components. Areas that do not contribute to the extreme force effect under consideration may be neglected in the analysis.

Base design wind velocity varies significantly due to local conditions. For small or low structures, such as this example, wind usually does not govern.

Pressures on windward and leeward sides are to be taken simultaneously in the assumed direction of wind.

The direction of the wind is assumed to be horizontal, unless otherwise specified in S3.8.3. The design wind pressure, in KSF, may be determined as:

$$
\begin{align*}
\mathrm{P}_{\mathrm{D}} & =\mathrm{P}_{\mathrm{B}}\left(\mathrm{~V}_{\mathrm{DZ}} / \mathrm{V}_{\mathrm{B}}\right)^{2}  \tag{S3.8.1.2.1-1}\\
& =\mathrm{P}_{\mathrm{B}}\left(\mathrm{~V}_{\mathrm{DZ}}^{2} / 10,000\right)
\end{align*}
$$

where:

$$
\mathrm{P}_{\mathrm{B}}=\text { base wind pressure specified in Table S3.8.1.2.1-1 (ksf) }
$$

Since the bridge component heights are less than 30 ft . above the ground line, $\mathrm{V}_{\mathrm{B}}$ is taken to be 100 mph .

Wind load transverse to the superstructure

$$
\mathrm{F}_{\mathrm{T} \text { Super }}=\mathrm{p}_{\mathrm{wT}}\left(\mathrm{H}_{\text {wind }}\right)\left[\left(\mathrm{L}_{\text {back }}+\mathrm{L}_{\mathrm{ahead}}\right) / 2\right]
$$

where:

$$
\begin{aligned}
\mathrm{H}_{\text {wind }} & =\text { the exposed superstructure height }(\mathrm{ft} .) \\
& =\text { girder }+ \text { haunch }+ \text { deck }+ \text { parapet } \\
& =6+0.333+0.667+3.5 \\
& =10.5 \mathrm{ft} . \\
\mathrm{p}_{\mathrm{wT}} & =\text { transverse wind pressure values }(\mathrm{ksf}) \\
& \left.=\mathrm{P}_{\mathrm{B}} \text { (use Table } \mathrm{S} 3.8 .1 .2 .2-1\right)
\end{aligned}
$$

$\mathrm{L}_{\text {back }}=$ span length to the deck joint, or end of bridge, back station from pier (ft.)
$=110 \mathrm{ft}$.
$\mathrm{L}_{\text {ahead }}=$ span length to the deck joint, or end of bridge, ahead station from pier (ft.)
$=110 \mathrm{ft}$.

$$
\begin{array}{rlrl}
\mathrm{F}_{\mathrm{T} \text { Super }} & =0.05(10.5)[(110+110) / 2] & & =57.8 \mathrm{k} \\
& =0.044(1,155) & & (0 \text { degrees }) \\
& =0.041(1,155) & & =47.4 \mathrm{k} \\
& =0.033(1,155) & & (15 \text { degrees }) \\
& =0.017(1,155) & & =38.1 \mathrm{k} \\
& & (45 \text { degrees }) \\
& & 19.6 \mathrm{k} & \\
(60 \text { degrees })
\end{array}
$$

Wind load along axes of superstructure (longitudinal direction)
The longitudinal wind pressure loading induces forces acting parallel to the longitudinal axis of the bridge.
$\mathrm{F}_{\mathrm{L} \text { Super }}=\mathrm{p}_{\mathrm{wL}}\left(\mathrm{H}_{\text {wind }}\right)\left(\mathrm{L}_{\text {back }}+\mathrm{L}_{\text {ahead }}\right) / n_{\text {fixed piers }}$
where:

$$
\begin{aligned}
\mathrm{H}_{\text {wind }} & =10.5 \mathrm{ft} . \\
& =\text { Longitudinal wind pressure values (ksf) } \\
\mathrm{p}_{\mathrm{wL}} & =\mathrm{P}_{\mathrm{B}} \text { (use Table S3.8.1.2.2-1) } \\
& \\
\mathrm{L}_{\text {back }} & =110 \mathrm{ft} . \\
\mathrm{L}_{\text {ahead }} & =110 \mathrm{ft} .
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{F}_{\mathrm{L} \text { Super }} & =0.0(10.5)[(110+110)] / 1 & & =0 \mathrm{k} \\
& =0.006(2,310) / 1 & & =13.9 \mathrm{k}
\end{aligned} \begin{array}{ll}
(0 \text { degrees }) \\
& =0.012(2,310) / 1 \\
& =0.016(2,310) / 1 \\
& =0.019(2,310) / 1
\end{array}
$$

The transverse and longitudinal pressures should be applied simultaneously.

Resultant wind load along axes of pier
The transverse and longitudinal superstructure wind forces, which are aligned relative to the superstructure axis, are resolved into components that are aligned relative to the pier axes.

Load perpendicular to the plane of the pier:

$$
\mathrm{F}_{\mathrm{L} \text { Pier }}=\mathrm{F}_{\mathrm{L} \text { Super }} \cos \left(\theta_{\text {skew }}\right)+\mathrm{F}_{\mathrm{T} \text { Super }} \sin \left(\theta_{\text {skew }}\right)
$$

At 0 degrees:

$$
\begin{aligned}
\mathrm{F}_{\text {LPier }} & =0 \cos 20+57.8 \sin 20 \\
& =19.8 \mathrm{k}
\end{aligned}
$$

At 60 degrees:

$$
\begin{aligned}
\mathrm{F}_{\text {LPier }} & =43.9 \cos 20+19.6 \sin 20 \\
& =48.0 \mathrm{k}
\end{aligned}
$$

Load in the plane of the pier (parallel to the line connecting the columns):

$$
\mathrm{F}_{\mathrm{T} \text { Pier }}=\mathrm{F}_{\mathrm{L} \text { Super }} \sin \left(\theta_{\text {skew }}\right)+\mathrm{F}_{\mathrm{T} \text { Super }} \cos \left(\theta_{\text {skew }}\right)
$$

At 0 degrees:

$$
\begin{aligned}
\mathrm{F}_{\text {T Pier }} & =0 \sin 20+57.8 \cos 20 \\
& =54.3 \mathrm{k}
\end{aligned}
$$

At 60 degrees:

$$
\begin{aligned}
\mathrm{F}_{\text {T Pier }} & =43.9 \sin 20+19.6 \cos 20 \\
& =33.4 \mathrm{k}
\end{aligned}
$$

The superstructure wind load acts at $10.5 / 2=5.25 \mathrm{ft}$. from the top of the pier cap.
The longitudinal and transverse forces applied to each bearing are found by dividing the forces above by the number of girders. If the support bearing line has expansion bearings, the $F_{L \text { Super }}$ component in the above equations is zero.

## Wind load on substructure (S3.8.1.2.3)

The transverse and longitudinal forces to be applied directly to the substructure are calculated from an assumed base wind pressure of 0.040 ksf (S3.8.1.2.3). For wind directions taken skewed to the substructure, this force is resolved into omponents perpendicular to the end and front elevations of the substructures. The component perpendicular to the end elevation acts on the exposed substructure area as seen in end elevation, and the component perpendicular to the front elevation acts on the exposed areas and is applied simultaneously with the wind loads from the superstructure.

$$
\mathrm{W}_{\text {wind on sub }}=\mathrm{W}_{\text {cap }}+\mathrm{W}_{\text {column }}
$$

Transverse wind on the pier cap (wind applied perpendicular to the longitudinal axis of the superstructure):

$$
\begin{aligned}
\mathrm{W}_{\text {cap }} & =0.04(\mathrm{cap} \text { width }) \\
& =0.04(4) \\
& =0.16 \mathrm{k} / \mathrm{ft} \text { of cap height }
\end{aligned}
$$

Longitudinal wind on the pier cap (wind applied parallel to the longitudinal axis of the superstructure):

$$
\begin{aligned}
\mathrm{W}_{\text {cap }} & =0.04(\text { cap length along the skew) } \\
& =0.04(58.93) \\
& =2.36 \mathrm{k} / \mathrm{ft} \text { of cap height }
\end{aligned}
$$

Transverse wind on the end column, this force is resisted equally by all columns:

$$
\begin{aligned}
\mathrm{W}_{\mathrm{T}, \text { column }} & =0.04(\text { column diameter }) / \mathrm{n}_{\text {columns }} \\
& =0.04(3.5) / 4 \\
& =0.035 \mathrm{k} / \mathrm{ft} \text { of column height above ground }
\end{aligned}
$$

Longitudinal wind on the columns, this force is resisted by each of the columns individually:

$$
\begin{aligned}
\mathrm{W}_{\mathrm{L}, \text { column }} & =0.04(\text { column diameter }) \\
& =0.04(3.5) \\
& =0.14 \mathrm{k} / \mathrm{ft} \text { of column height above ground }
\end{aligned}
$$

Total wind load on substructure:

$$
\begin{aligned}
& \mathrm{W}_{\mathrm{T} \text { wind on sub }}=0.16+0.035=0.20 \mathrm{k} / \mathrm{ft} \\
& \mathrm{~W}_{\mathrm{L} \text { wind on sub }}=2.36+0.14=2.50 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

## Wind on live load (S3.8.1.3)

When vehicles are present, the design wind pressure is applied to both the structure and vehicles. Wind pressure on vehicles is represented by an interruptible, moving force of 0.10 klf acting normal to, and 6.0 ft . above, the roadway and is transmitted to the structure.

When wind on vehicles is not taken as normal to the structure, the components of normal and parallel force applied to the live load may be taken as follows with the skew angle taken as referenced normal to the surface.

Use Table S3.8.1.3-1 to obtain $\mathrm{F}_{\mathrm{W}}$ values,

$$
\left.\begin{array}{rlrl}
\mathrm{F}_{\mathrm{T} \text { Super }} & =\mathrm{F}_{\mathrm{WT}}\left(\mathrm{~L}_{\text {back }}+\mathrm{L}_{\text {ahead }}\right) / 2 & & \\
\mathrm{~F}_{\mathrm{T} \text { Super }} & =0.100(110+110) / 2 & =11 \mathrm{k} & \\
& =0.088(110) & & =9.68 \mathrm{k}
\end{array}\right)\left(\begin{array}{ll}
(15 \text { degrees }) \\
& =0.082(110) \\
& =0.066(110) \\
& =9.02 \mathrm{k}
\end{array}\right)
$$

$\mathrm{F}_{\mathrm{WLL}}=11 \mathrm{k}$ (transverse direction, i.e., perpendicular to longitudinal axis of the superstructure)

## Temperature force (S3.12.2)

Due to the symmetry of the bridge superstructure, no force is developed at the intermediate bent due to temperature expansion/shrinkage of the superstructure.

## Shrinkage (S3.12.4)

Due to the symmetry of the bridge superstructure, no force is developed at the intermediate bent due to shrinkage of the superstructure.

## Load combinations

Figures $7.2-2$ and $7.2-3$ show the unfactored loads applied to the bent from the superstructure and wind.


Substructure Dead Loads


Figure 7.2-2 - Super- and Substructure Applied Dead Loads

## Transverse Wind on Structure



Longitudinal Wind on Structure


Figure 7.2-3 - Wind and Braking Loads on Super- and Substructure

## Design Step

7.2.2

Required information:
General (these values are valid for the entire pier cap):
$\mathrm{f}_{\mathrm{c}}{ }^{\prime}=3.0 \mathrm{ksi}$
$\beta_{1}=0.85$
$\mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi}$
Cap width $=4 \mathrm{ft}$.
Cap depth $=4 \mathrm{ft}$. (varies at ends)
No. stirrup legs $=6$
Stirrup diameter $=0.625$ in. (\#5 bars)
Stirrup area $=0.31 \mathrm{in}^{2}($ per leg $)$
Stirrup spacing $=$ varies along cap length
Side cover $=2$ in. (Table S5.12.3-1)
Cap bottom flexural bars:
No. bars in bottom row, positive region = 9 (\#8 bars)
Positive region bar diameter $=1.0$ in.
Positive region bar area, $\mathrm{A}_{\mathrm{s}}=0.79 \mathrm{in}^{2}$
Bottom cover $=2$ in. (Table S5.12.3-1)
Cap top flexural bars:
No. bars in top row, negative region $=14$ ( 7 sets of $2 \# 9$ bars bundled horizontally)
Negative region bar diameter $=1.128 \mathrm{in}$.
Negative region bar area, $\mathrm{A}_{\mathrm{s}}=1.0 \mathrm{in}^{2}$
Top cover $=2$ in. $($ Table S5.12.3-1)

From the analysis of the different applicable limit states, the maximum load effects on the cap were obtained. These load effects are listed in Table 7.2-1. The maximum factored positive moment occurs at 44.65 ft . from the cap end under Strength I limit state.

Table 7.2-1 - Strength I Limit State for Critical Locations in the Pier Cap (Maximum Positive Moment, Negative Moment and Shear)

|  |  | Unfactored Responses |  |  |  | Str-I |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Location* | DC | DW | LL + IM | BR |  |
|  | Max Pos M (k-ft) | 44.65 ft. | 147.5 | 37.1 | 437.9 | 5.2 |
| $1,015.5$ |  |  |  |  |  |  |
| Max Neg M (k-ft) | 6.79 ft. | -878.5 | -84.9 | -589.0 | -1.9 | $-2,259.4$ |
| Max Shear $(\mathrm{k})$ | 34.96 ft. | 292.9 | 39.5 | 210.4 | 2.8 | 798.3 |

* measured from the end of the cap

Notes:
DC: superstructure dead load (girders, slab and haunch, diaphragms, and parapets)
plus the substructure dead load (all components)
DW: dead load due to the future wearing surface
LL + IM: live load + impact transferred from the superstructure
BR: braking load transferred from the superstructure
Str-I: load responses factored using Strength I limit state load factors

## Design Step

 7.2.2.1Pier cap flexural resistance (S5.7.3.2)
The factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, is taken as:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{r}}=\varphi \mathrm{M}_{\mathrm{n}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\varphi & =\text { flexural resistance factor as specified in S5.5.4.2 } \\
& =0.9
\end{aligned}
$$

$$
\mathrm{M}_{\mathrm{n}}=\text { nominal resistance }(\mathrm{k}-\mathrm{in})
$$

For calculation of $M_{n}$, use the provisions of S5.7.3.2.3 which state, for rectangular sections subjected to flexure about one axis, where approximate stress distribution specified in S5.7.2.2 is used and where the compression flange depth is not less than "c" as determined in accordance with Eq. S5.7.3.1.1-3, the flexural resistance $M_{n}$ may be determined by using Eq. S5.7.3.1.1-1 through S5.7.3.2.2-1, in which case " $b_{w}$ " is taken as " $b$ ".

Rectangular section behavior is used to design the pier cap. The compression reinforcement is neglected in the calculation of the flexural resistance.

## Design Step Maximum positive moment

7.2.2.2

Applied Strength I moment, $\mathrm{M}_{\mathrm{u}}=1,015.5 \mathrm{k}-\mathrm{ft}$
Applied Service I moment, $\mathrm{M}_{\mathrm{s}}=653.3 \mathrm{k}-\mathrm{ft}$ (from computer software)
Axial load on the pier cap is small, therefore, the effects of axial load is neglected in this example.

Check positive moment resistance (bottom steel)
Calculate the nominal flexural resistance according to S5.7.3.2.3.

$$
\begin{equation*}
\mathrm{M}_{\mathrm{n}}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right) \tag{S5.7.3.2.2-1}
\end{equation*}
$$

Determine $\mathrm{d}_{\mathrm{s}}$, the corresponding effective depth from the extreme fiber to the centroid of the tensile force in the tensile reinforcement.

$$
\mathrm{d}_{\mathrm{s}}=\text { cap depth }-\mathrm{CSG}_{\mathrm{b}}
$$

where:
$\mathrm{CGS}_{\mathrm{b}}=$ distance from the centroid of the bottom bars to the bottom of the cap (in.)
$=$ cover + stirrup diameter $+1 / 2$ bar diameter
$=2+0.625+1 / 2(1.0)$

$$
=3.125 \mathrm{in}
$$

$$
\begin{aligned}
\mathrm{d}_{\mathrm{s}} & =4(12)-3.125 \\
& =44.875 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}} & =\left(\mathrm{n}_{\text {bars Tension }}\right)\left(\mathrm{A}_{\mathrm{s} \text { bar }}\right) \\
& =9(0.79) \\
& =7.1 \mathrm{in}^{2}
\end{aligned}
$$

Determine "a" using Eq. S5.7.3.1.1-4

$$
\begin{align*}
\mathrm{a} & =\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{~b}  \tag{S5.7.3.1.1-4}\\
& =7.1(60) /[0.85(3)(48)] \\
& =3.48 \mathrm{in} .
\end{align*}
$$

Calculate the nominal flexural resistance, $\mathrm{M}_{\mathrm{n}}$

$$
\begin{align*}
\mathrm{M}_{\mathrm{n}} & =\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{a} / 2\right)  \tag{S5.7.3.2.2-1}\\
& =7.1(60)[44.875-(3.48 / 2)] / 12 \\
& =1,531 \mathrm{k}-\mathrm{ft}
\end{align*}
$$

Therefore, the factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, can be calculated as follows:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(1,531) \\
& =1,378 \mathrm{k}-\mathrm{ft}>\mathrm{M}_{\mathrm{u}}=1015.5 \mathrm{k}-\mathrm{ft} \text { OK }
\end{aligned}
$$

Limits for reinforcement (S5.7.3.3)
Check if the section is over-reinforced.
The maximum amount of nonprestressed reinforcement shall be such that:

$$
\begin{equation*}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \leq 0.42 \tag{S5.7.3.3.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{c} & =\mathrm{a} / \beta_{1} \\
& =3.48 / 0.85 \\
& =4.1 \mathrm{in} . \\
& \\
\mathrm{d}_{\mathrm{e}} & =\mathrm{d}_{\mathrm{s}} \\
& =44.875 \mathrm{in} . \\
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \quad & =4.1 / 44.875 \\
& =0.091<0.42 \text { OK }
\end{aligned}
$$

Check the minimum reinforcement requirements (S5.7.3.3.2)
Unless otherwise specified, at any section of a flexural component, the amount of nonprestressed tensile reinforcement must be adequate to develop a factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, at least equal to the lesser of:

$$
1.2 \mathrm{M}_{\mathrm{cr}}=1.2 \mathrm{f}_{\mathrm{r}} \mathrm{~S}
$$

where:

$$
\begin{aligned}
\mathrm{f}_{\mathrm{r}} & =0.24 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \\
& =0.24 \sqrt{3} \\
& =0.42 \mathrm{ksi} \\
\mathrm{~S} & =\mathrm{bh}^{2} / 6 \\
& =4(12)[4(12)]^{2} / 6 \\
& =18,432 \mathrm{in}^{3}
\end{aligned}
$$

$$
\begin{aligned}
1.2 \mathrm{M}_{\mathrm{cr}} & =1.2(0.42)(18,432) / 12 \\
& =774.1 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
1.33 \mathrm{M}_{\mathrm{u}} & =1.33(1,015.5) \\
& =1,351 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Minimum required section resistance $=774.1 \mathrm{k}-\mathrm{ft}$
Provided section resistance $\quad=1,378 \mathrm{k}-\mathrm{ft}>774.1 \mathrm{k}$-ft OK

Check the flexural reinforcement distribution (S5.7.3.4)
Check allowable stress, $\mathrm{f}_{\mathrm{s}}$

$$
\begin{equation*}
\mathrm{f}_{\mathrm{s} \text {, allow }}=\mathrm{Z} /\left[\left(\mathrm{d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3}\right] \leq 0.6 \mathrm{f}_{\mathrm{y}} \tag{S5.7.3.4-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{Z} & =\text { crack width parameter (k/in) } \\
& =170 \mathrm{k} / \mathrm{in} \text { (moderate exposure conditions are assumed) }
\end{aligned}
$$

$\mathrm{d}_{\mathrm{c}}=$ distance from the extreme tension fiber to the center of the closest bar (in.)
$=$ clear cover + stirrup diameter $+1 / 2$ bar diameter
The cover on the bar under investigation cannot exceed 2.0 in ., therefore, the stirrup diameter is not taken into account for $\mathrm{d}_{\mathrm{c}}$ is:

$$
\begin{aligned}
& =2+1 / 2(1.0) \\
& =2.5 \mathrm{in} .
\end{aligned}
$$

A = area having the same centroid as the principal tensile reinforcement and bounded by the surfaces of the cross-section and a straight line parallel to the neutral axis, divided by the number of bars ( $\mathrm{in}^{2}$ )

$$
=2 \mathrm{~d}_{\mathrm{c}}(\mathrm{cap} \text { width }) / \mathrm{n}_{\text {bars }}
$$

$$
=2(2.5)(48) / 9
$$

$$
=26.7 \mathrm{in}^{2}
$$

$$
\begin{aligned}
\mathrm{f}_{\mathrm{s}, \text { allow }} & =\mathrm{Z} /\left[\left(\mathrm{d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3}\right] \\
& =170 /[(2.5)(26.7)]^{1 / 3} \\
& =41.9 \mathrm{ksi}>0.6(60)=36 \mathrm{ksi} \text { therefore, } \mathrm{f}_{\mathrm{s}, \text { allow }}=36 \mathrm{ksi}
\end{aligned}
$$

## Check service load applied steel stress, $\mathrm{f}_{\mathrm{s} \text {, actual }}$

For 3.0 ksi concrete, the modular ratio, $\mathrm{n}=9$ (see S 6.10 .3 .1 .1 b or calculate by dividing the steel modulus of elasticity by the concrete and rounding up as required by S5.7.1)

Assume the stresses and strains vary linearly.
From the load analysis of the bent:
Dead load + live load positive service load moment $=653.3 \mathrm{k}$ - ft
The transformed moment of inertia is calculated assuming elastic behavior, i.e., linear stress and strain distribution. In this case, the first moment of area of the transformed steel on the tension side about the neutral axis is assumed equal to that of the concrete in compression.

Assume the neutral axis at a distance " $y$ " from the compression face of the section.
The section width equals 48 in .
Transformed steel area $=($ total steel bar area $)($ modular ratio $)=7.1(9)=63.9 \mathrm{in}^{2}$
By equating the first moment of area of the transformed steel about that of the concrete, both about the neutral axis:

$$
63.9(44.875-y)=48 y(y / 2)
$$

Solving the equation results in $\mathrm{y}=9.68 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{I}_{\text {transformed }} & =\mathrm{A}_{\mathrm{ts}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{y}\right)^{2}+\mathrm{by}^{3} / 3 \\
& =63.9(44.875-9.68)^{2}+48(9.68)^{3} / 3 \\
& =93,665 \mathrm{in}^{4}
\end{aligned}
$$

Stress in the steel, $\mathrm{f}_{\mathrm{s} \text {, actual }}=\left(\mathrm{M}_{\mathrm{s}} \mathrm{c} / \mathrm{I}\right) \mathrm{n}$, where M is the moment action on the section.

$$
\begin{aligned}
\mathrm{f}_{\mathrm{s}, \text { actual }} & =[653.3(12)(35.195) / 93,665] 9 \\
& =26.5 \mathrm{ksi}<\mathrm{f}_{\mathrm{s}, \text { allow }}=36 \mathrm{ksi} \mathbf{O K}
\end{aligned}
$$



Figure 7.2-4 - Crack Control for Positive Reinforcement Under Service Load

## Design Step

7.2.2.3

## Maximum negative moment

From the bent analysis, the maximum factored negative moment occurs at 6.79 ft . from the cap edge under Strength I limit state:

Applied Strength I moment, $\mathrm{M}_{\mathrm{u}}=-2,259.4 \mathrm{k}$ - ft
Applied Service I moment, $\mathrm{M}_{\mathrm{s}}=-1,572.4 \mathrm{k}$-ft (from computer analysis)

Check negative moment resistance (top steel)
Calculate $\mathrm{M}_{\mathrm{n}}$ using Eq. S5.7.3.2.2-1.
Determine $d_{s}$, the corresponding effective depth from the extreme fiber to the centroid of the tensile force in the tensile reinforcement. The compressive reinforcement is neglected in the calculation of the nominal flexural resistance.

$$
\mathrm{d}_{\mathrm{s}}=\text { cap depth }-\mathrm{CGS}_{\mathrm{t}}
$$

where:
$\mathrm{CGS}_{\mathrm{t}}=$ distance from the centroid of the top bars to the top of the cap
(in.)
$=$ cover + stirrup diameter $+1 / 2$ bar diameter
$=2+0.625+1 / 2(1.128)$
$=3.189 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{d}_{\mathrm{s}} & =4(12)-3.189 \\
& =44.81 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}} & =\left(\mathrm{n}_{\text {bars Tension }}\right)\left(\mathrm{A}_{\mathrm{s} \text { bar }}\right) \\
& =14(1.0) \\
& =14.0 \mathrm{in}^{2}
\end{aligned}
$$

Determine " a " using Eq. S5.7.3.1.1-4

$$
\begin{align*}
\mathrm{a} & =\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{~b}  \tag{S5.7.3.1.1-4}\\
& =14.0(60) /[(0.85(3)(4)(12)] \\
& =6.86 \mathrm{in} .
\end{align*}
$$

Calculate the nominal flexural resistance, $\mathrm{M}_{\mathrm{n}}$

$$
\begin{aligned}
\mathrm{M}_{\mathrm{n}} & =14.0(60)[44.81-(6.86 / 2)] / 12 \\
& =2,897 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Therefore, the factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$ :

$$
\begin{aligned}
\mathrm{M}_{\mathrm{r}} & =0.9(2,897) \\
& =2,607 \mathrm{k}-\mathrm{ft}>\mathrm{M}_{\mathrm{u}}=|-2,259.4| \mathrm{k}-\mathrm{ft} \mathbf{O K}
\end{aligned}
$$

$\underline{\text { Limits for reinforcement (S5.7.3.3) }}$
Check if the section is over-reinforced.
The maximum amount of nonprestressed reinforcement shall be such that:

$$
\begin{equation*}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \leq 0.42 \tag{S5.7.3.3.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{c} \quad & =\mathrm{a} / \beta_{1} \\
& =6.86 / 0.85 \\
& =8.07 \mathrm{in} . \\
& \\
\mathrm{d}_{\mathrm{e}} & =\mathrm{d}_{\mathrm{s}} \\
& =44.81 \mathrm{in.} \\
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \quad & =8.07 / 44.81 \\
& =0.18<0.42 \mathrm{OK}
\end{aligned}
$$

## Check minimum reinforcement (S5.7.3.3.2)

Unless otherwise specified, at any section of a flexural component, the amount of nonprestressed tensile reinforcement shall be adequate to develop a factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, at least equal to the lesser of:

$$
1.2 \mathrm{M}_{\mathrm{cr}}=1.2 \mathrm{f}_{\mathrm{r}} \mathrm{~S}
$$

where:

$$
\begin{align*}
\mathrm{f}_{\mathrm{r}} & =0.24 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}}  \tag{S5.4.2.6}\\
& =0.24 \sqrt{3} \\
& =0.42 \mathrm{ksi} \\
\mathrm{~S} & =\mathrm{bh}^{2} / 6 \\
& =4(12)[4(12)]^{2} / 6 \\
& =18,432 \mathrm{in}^{3}
\end{align*}
$$

OR

$$
\begin{aligned}
1.33 \mathrm{M}_{\mathrm{u}} & =1.33(-2,259.4) \\
& =|-3,005| \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

$$
1.2 \mathrm{M}_{\mathrm{cr}}=1.2(0.42)(18,432) / 12
$$

$$
=774.1 \mathrm{k}-\mathrm{ft}
$$

Minimum required section resistance $=774.1 \mathrm{k}-\mathrm{ft}$
Provided section resistance $\quad=2,607 \mathrm{k}-\mathrm{ft}>774.1 \mathrm{k}$-ft OK

Check the flexural reinforcement distribution (S5.7.3.4)
Check the allowable stress, $\mathrm{f}_{\mathrm{s}}$

$$
\begin{equation*}
\mathrm{f}_{\mathrm{s} \text {, allow }}=\mathrm{Z} /\left[\left(\mathrm{d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3}\right] \leq 0.6 \mathrm{f}_{\mathrm{y}} \tag{S5.7.3.4-1}
\end{equation*}
$$

where:
$\mathrm{Z}=170 \mathrm{k} / \mathrm{in}$. (moderate exposure conditions are assumed)
$\mathrm{d}_{\mathrm{c}}=2+1 / 2(1.128)$

$$
=2.56 \mathrm{in} .
$$

A = area having the same centroid as the principal tensile reinforcement and bounded by the surfaces of the cross-section and a straight line parallel to the neutral axis, divided by the number of bars (in ${ }^{2}$ )

$$
=2 \mathrm{~d}_{\mathrm{c}}(\mathrm{cap} \text { width }) / \mathrm{n}_{\text {bars }}
$$

$$
=2(2.56)(48) / 14
$$

$$
=17.6 \mathrm{in}^{2}
$$

$$
\begin{aligned}
\mathrm{f}_{\mathrm{s}, \text { allow }} & =\mathrm{Z} /\left[\left(\mathrm{d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3}\right] \\
& =170 /[2.56(17.6)]^{1 / 3} \\
& =47.8 \mathrm{ksi}>0.6(60)=36 \mathrm{ksi} \text { OK, therefore, use } \mathrm{f}_{\mathrm{s}, \text { allow }}=36 \mathrm{ksi}
\end{aligned}
$$

Check the service load applied steel stress, $\mathrm{f}_{\mathrm{s}, \text { actual }}$
For 3.0 ksi concrete, the modular ratio, $n=9$
Assume the stresses and strains vary linearly.
From the load analysis of the bent:
Dead load + live load negative service load moment $=-1,572.4 \mathrm{k}-\mathrm{ft}$
The transformed moment of inertia is calculated assuming elastic behavior, i.e., linear stress and strain distribution. In this case, the first moment of area of the transformed steel on the tension side about the neutral axis is assumed equal to that of the concrete in compression.

Assume the neutral axis at a distance " $y$ " from the compression face of the section.
Section width $=48 \mathrm{in}$.
Transformed steel area $=($ total steel bar area $)($ modular ratio $)=14.0(9)=126 \mathrm{in}^{2}$
By equating the first moment of area of the transformed steel about that of the concrete, both about the neutral axis:

$$
126(44.81-y)=48 y(y / 2)
$$

Solving the equation results in $\mathrm{y}=12.9 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{I}_{\text {transformed }} & =\mathrm{A}_{\mathrm{ts}}\left(\mathrm{~d}_{\mathrm{s}}-\mathrm{y}\right)^{2}+\mathrm{by}^{3} / 3 \\
& =126(44.81-12.9)^{2}+48(12.9)^{3} / 3 \\
& =162,646 \mathrm{in}^{4}
\end{aligned}
$$

Stress in the steel, $\mathrm{f}_{\mathrm{s} \text {, actual }}=\left(\mathrm{M}_{\mathrm{s}} \mathrm{c} / \mathrm{I}\right) \mathrm{n}$, where M is the moment action on the section.

$$
\begin{aligned}
\mathrm{f}_{\mathrm{s}, \text { actual }} & =[|-1,572.4|(12)(31.91) / 162,646] 9 \\
& =33.3 \mathrm{ksi}<\mathrm{f}_{\mathrm{s},} \text { allow }=36 \mathrm{ksi} \text { OK }
\end{aligned}
$$



Figure 7.2-5 - Crack Control for Negative Reinforcement Under Service Load

Design Step
7.2.2.4

Check minimum temperature and shrinkage steel (S5.10.8)
Reinforcement for shrinkage and temperature stresses is provided near the surfaces of the concrete exposed to daily temperature changes and in structural mass concrete. Temperature and shrinkage reinforcement is added to ensure that the total reinforcement on exposed surfaces is not less than that specified below.

Using the provisions of S5.10.8.2,

$$
\begin{equation*}
\mathrm{A}_{\mathrm{s}, \min 1}=0.11 \mathrm{~A}_{\mathrm{g}} / \mathrm{f}_{\mathrm{y}} \tag{S5.10.8.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{g}} & =\text { gross area of section }\left(\mathrm{in}^{2}\right) \\
& =[4(12)]^{2} \\
& =2,304 \mathrm{in}^{2}
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}, \min 1} & =0.11(2,304) / 60 \\
& =4.2 \mathrm{in}^{2}
\end{aligned}
$$

This area is to be divided between the two faces, i.e., 2.1 in $^{2}$ per face. Shrinkage and temperature reinforcement must not be spaced farther apart than 3.0 times the component thickness or 18.0 in .

Use 4 \# 7 bars per face.

$$
\begin{aligned}
\mathrm{A}_{\text {s provided }} & =4(0.6) \\
& =2.4 \mathrm{in}^{2}>2.1 \mathrm{in}^{2} \mathbf{O K}
\end{aligned}
$$

## Design Step $\mid \underline{\text { Skin reinforcement (S5.7.3.4) }}$

7.2.2.5

If the effective depth, $\mathrm{d}_{\mathrm{c}}$, of the reinforced concrete member exceeds 3 ft ., longitudinal skin reinforcement is uniformly distributed along both side faces of the component for a distance of $\mathrm{d} / 2$ nearest the flexural tension reinforcement. The area of skin reinforcement $\left(\mathrm{in}^{2} / \mathrm{ft}\right.$ of height) on each side of the face is required to satisfy:

$$
\begin{equation*}
\mathrm{A}_{\mathrm{sk}} \geq 0.012\left(\mathrm{~d}_{\mathrm{e}}-30\right) \leq\left(\mathrm{A}_{\mathrm{s}}+\mathrm{A}_{\mathrm{ps}}\right) / 4 \tag{S5.7.3.4-4}
\end{equation*}
$$

where:
$\mathrm{A}_{\mathrm{ps}}=$ area of prestressing $\left(\mathrm{in}^{2}\right)$
$d_{e}=$ flexural depth taken as the distance from the compression face of the centroid of the steel, positive moment region(in.)

$$
\begin{aligned}
\mathrm{A}_{\mathrm{sk}} & =0.012(44.875-30) \\
& =0.179 \mathrm{in}^{2} / \mathrm{ft} \leq 14.0 / 4=3.5 \mathrm{in}^{2} / \mathrm{ft}
\end{aligned}
$$

Required $\mathrm{A}_{\text {sk }}$ per face $=0.179(4)=0.72 \mathrm{in}^{2}<2.4 \mathrm{in}^{2}$ provided $\mathbf{O K}$


## Design Step

7.2.2.6

Maximum shear
From analysis of the bent, the maximum factored shear occurs at 34.96 ft . from the cap end under Strength I limit state:

Shear, $\mathrm{V}_{\mathrm{u}}=798.3 \mathrm{k}$

Calculate the nominal shear resistance using S5.8.3.3.
The factored shear resistance, $\mathrm{V}_{\mathrm{r}}$

$$
\begin{equation*}
V_{r}=\varphi V_{n} \tag{S5.8.2.1-2}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \varphi=0.9, \text { shear resistance factor as specified in S5.5.4.2 } \\
& \mathrm{V}_{\mathrm{n}}=\text { nominal shear resistance }(\mathrm{k})
\end{aligned}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$, shall be determined as the lesser of:

$$
\begin{equation*}
V_{n}=V_{c}+V_{s}+V_{p} \tag{S5.8.3.3-1}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{n}}=0.25 \mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}}+\mathrm{V}_{\mathrm{p}} \tag{S5.8.3.3-2}
\end{equation*}
$$

where:
$\mathrm{V}_{\mathrm{c}}=$ shear resistance due to concrete $(\mathrm{k})$

$$
\begin{equation*}
=0.0316 \beta \sqrt{\mathrm{~F}_{\mathrm{c}}}{ }_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \tag{S5.8.3.3-3}
\end{equation*}
$$

where:
$\mathrm{b}_{\mathrm{v}}=$ effective web width taken as the minimum web width within the depth $\mathrm{d}_{\mathrm{v}}$ as determined in S5.8.2.9 (in.)
$=48 \mathrm{in}$.
$\mathrm{d}_{\mathrm{v}}=$ effective shear depth as determined in S5.8.2.9 (in.). It is the distance, measured perpendicular to the neutral axis between the resultants of the tensile and compressive force due to flexure. It need not be taken less than the greater of $0.9 \mathrm{~d}_{\mathrm{e}}$ or 0.72 h .
$=\mathrm{d}_{\mathrm{e}}-\mathrm{a} / 2$
$=44.81-(6.86 / 2)$
$=41.4 \mathrm{in}$.
$0.9 \mathrm{~d}_{\mathrm{e}}=0.9(44.81)$
$=40.3$ in.

$$
0.72 \mathrm{~h}=0.72(48)
$$

$$
=34.56 \mathrm{in} .
$$

$\beta=$ factor indicating ability of diagonally cracked concrete to
transmit tension as specified in S5.8.3.4
$=$ for nonprestressed sections, $\beta$ may be taken as 2.0
$\mathrm{~V}_{\mathrm{c}}=0.0316(2.0) \sqrt{3}(48)(41.4)$
$=217.5 \mathrm{k}$
$\mathrm{V}_{\mathrm{s}}=$ shear resistance due to steel (k)
$=\left[\mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{d}_{\mathrm{v}}(\cot \theta+\cot \alpha) \sin \alpha\right] / \mathrm{s}$
where:
$\mathrm{s}=$ spacing of stirrups (in.)
$=$ assume 7 in .
$\theta=$ angle of inclination of diagonal compressive stresses as
determined in S5.8.3.4 (deg)
$=45 \mathrm{deg}$ for nonprestressed members
$\alpha$ = angle of inclination of transverse reinforcement to
longitudinal axis (deg)
$=90$ deg for vertical stirrups
$A_{v}=(6$ legs of \#5 bars)(0.31)
$=1.86 \mathrm{in}^{2}$
$\mathrm{~V}_{\mathrm{s}}=[1.86(60)(41.4)(1 / \tan 45)] / 7$
$=660.0 \mathrm{k}$
$\mathrm{V}_{\mathrm{p}}=$ component in the direction of the applied shear of the effective
prestressing force; positive if resisting the applied shear (k), not
applicable in the pier cap
$=0.0$ for nonprestressed members

Therefore, $\mathrm{V}_{\mathrm{n}}$ is the lesser of:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =217.5+660.0+0 \\
& =877.5 \mathrm{k}
\end{aligned}
$$

OR

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =0.25(3)(48)(41.4)+0 \\
& =1,490.4 \mathrm{k}
\end{aligned}
$$

Use $\mathrm{V}_{\mathrm{n}}=877.5 \mathrm{k}$

Therefore,

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =\varphi \mathrm{V}_{\mathrm{n}} \\
& =0.9(877.5) \\
& =789.8 \mathrm{k}>\mathrm{V}_{\mathrm{u}}=798.3 \mathrm{k} \mathrm{OK}
\end{aligned}
$$

Check the minimum transverse reinforcement (S5.8.2.5)
A minimum amount of transverse reinforcement is required to restrain the growth of diagonal cracking and to increase the ductility of the section. A larger amount of transverse reinforcement is required to control cracking as the concrete strength is increased.

Where transverse reinforcement is required, as specified in S5.8.2.4, the area of steel must satisfy:

$$
\begin{equation*}
\mathrm{A}_{\mathrm{v}}=0.0316 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \mathrm{b}_{\mathrm{v}} \mathrm{~s} / \mathrm{f}_{\mathrm{y}} \tag{S5.8.2.5-1}
\end{equation*}
$$

where:
$\mathrm{b}_{\mathrm{v}}=$ width of web adjusted for the presence of ducts as specified
in S5.8.2.9 (in.)

$$
\begin{aligned}
\mathrm{A}_{\mathrm{v}} & =0.0316 \sqrt{3}(48)(7) / 60 \\
& =0.307 \mathrm{in}^{2}<1.86 \mathrm{in}^{2} \text { provided } \mathbf{O K}
\end{aligned}
$$

Check the maximum spacing of the transverse reinforcement (S5.8.2.7)
The spacing of the transverse reinforcement must not exceed the maximum permitted spacing, $\mathrm{s}_{\text {max }}$, determined as:

$$
\text { If } \begin{align*}
& \mathrm{v}_{\mathrm{u}}<0.125 \mathrm{f}_{\mathrm{c}}^{\prime}, \text { then } \\
&  \tag{S5.8.2.7-1}\\
& \mathrm{s}_{\max }=0.8 \mathrm{~d}_{\mathrm{v}} \leq 24.0 \mathrm{in} .
\end{align*}
$$

$$
\text { If } \begin{array}{ll}
v_{u} \geq 0.125 f_{c}^{\prime}, \text { then: } \\
& s_{\max }=0.4 d_{v} \leq 12.0 \mathrm{in} . \tag{S5.8.2.7-2}
\end{array}
$$

The shear stress on the concrete, $\mathrm{v}_{\mathrm{u}}$, is taken to be:

$$
\begin{align*}
\mathrm{v}_{\mathrm{u}} & =\mathrm{V}_{\mathrm{u}} /\left(\varphi \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}}\right)  \tag{S5.8.2.9-1}\\
& =798.3 /[0.9(48)(41.4)] \\
& =0.446 \mathrm{ksi}>0.125(3)=0.375 \mathrm{ksi}
\end{align*}
$$

Therefore, use Eq. S5.8.2.7-2

$$
\begin{aligned}
\mathrm{s}_{\max } & =0.4(41.4) \\
& =16.6 \mathrm{in} . \mathrm{s}_{\max } \text { cannot exceed } 12 \mathrm{in} ., \text { therefore, use } 12 \mathrm{in} . \text { as maximum } \\
\mathrm{s}_{\text {actual }} & =7 \mathrm{in} .<12 \mathrm{in.} \text { OK }
\end{aligned}
$$



Figure 7.2-7 - Stirrup Distribution in the Bent Cap

## Design Step <br> 7.2.3

Column design
Required information:
General:

$$
\begin{aligned}
& \mathrm{f}_{\mathrm{c}}^{\prime}=3.0 \mathrm{ksi} \\
& \mathrm{E}_{\mathrm{c}}=3,321 \mathrm{ksi}(\mathrm{~S} 5.4 .2 .4) \\
& \mathrm{n}=9 \\
& \mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi}
\end{aligned}
$$

Circular Columns:
Column diameter $=3.5 \mathrm{ft}$.
Column area, $\mathrm{A}_{\mathrm{g}}=9.62 \mathrm{ft}^{2}$
Side cover $=2$ in. (Table S5.12.3-1)
Vertical reinforcing bar diameter $(\# 8)=1.0 \mathrm{in}$.
Steel area $=0.79$ in $^{2}$
Number of bars $=16$
Total area of longitudinal reinforcement $=12.64 \mathrm{in}^{2}$
Type of transverse reinforcement $=$ ties
Tie spacing $=12 \mathrm{in}$.
Transverse reinforcement bar diameter (\#3) $=0.375$ in. (S5.10.6.3)
Transverse reinforcement area $=0.11 \mathrm{in}^{2} / \mathrm{bar}$

The example bridge is in Seismic Zone 1, therefore, a seismic investigation is not necessary for the column design. Article S 5.10 .11 provides provisions for seismic design where applicable.

## Applied moments and shears

The maximum biaxial responses occur on column 1 at 0.0 ft . from the bottom (top face of footing).

From the load analysis of the bent, the maximum load effects at the critical location were obtained and are listed in Table 7.2-2.

Table 7.2-2 - Maximum Factored Load Effects and the Concurrent Load Effects for Strength Limit States

| Load effect <br> maximized | Limit State | $\mathrm{M}_{\mathrm{t}}$ <br> $(\mathrm{k}-\mathrm{ft})$ | $\mathrm{M}_{\mathrm{l}}$ <br> $(\mathrm{k}-\mathrm{ft})$ | $\mathrm{P}_{\mathrm{u}}$ <br> $(\mathrm{k})$ | $\mathrm{M}_{\mathrm{u}}$ <br> $(\mathrm{k}-\mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Positive $\mathrm{M}_{\mathrm{t}}$ | Strength V | 342 | 352 | 1,062 | 491 |
| Negative $\mathrm{M}_{\mathrm{t}}$ | Strength V | -129 | -216 | 682 | 252 |
| Positive $\mathrm{M}_{\mathrm{l}}$ | Strength V | 174 | 822 | 1,070 | 840 |
| Negative $\mathrm{M}_{\mathrm{l}}$ | Strength V | 116 | -824 | 1,076 | 832 |
| Axial Load P | Strength I | 90 | -316 | 1,293 | 329 |

where:
$M_{t}$ : Factored moment about the transverse axis
$\mathrm{M}_{1}$ : Factored moment about the longitudinal axis
$\mathrm{P}_{\mathrm{u}}$ : Factored axial load
Sample hand calculations are presented for the case of maximum positive $M_{1}$ from Table 7.2-2.

Maximum shear occurs on column 1 at 0.0 ft . from the bottom (top face of footing)
Factored shears - strength limit state:

$$
\begin{array}{ll}
\mathrm{V}_{\mathrm{t}}=44.8 \mathrm{k} & (\text { Str- } \mathrm{V}) \\
\mathrm{V}_{\mathrm{l}}=26.0 \mathrm{k} & (\text { Str- })
\end{array}
$$

## Check limits for reinforcement in compression members (S5.7.4.2)

The maximum area of nonprestressed longitudinal reinforcement for non-composite compression components shall be such that:

$$
\begin{equation*}
\mathrm{A}_{s} / \mathrm{A}_{\mathrm{g}} \leq 0.08 \tag{S5.7.4.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
& A_{s}=\text { area of nonprestressed tension steel }\left(\mathrm{in}^{2}\right) \\
& A_{g}=\text { gross area of section }\left(\mathrm{in}^{2}\right)
\end{aligned}
$$

$$
12.64 /[9.62(144)]=0.009<0.08 \mathbf{O K}
$$

The minimum area of nonprestressed longitudinal reinforcement for noncomposite compression components shall be such that:

$$
\begin{align*}
\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / \mathrm{A}_{\mathrm{g}} \mathrm{f}_{\mathrm{c}}^{\prime} & \geq 0.135  \tag{S5.7.4.2-3}\\
& =12.64(60) /[9.62(144)(3)] \\
& =0.182>0.135 \mathrm{OK}
\end{align*}
$$

 effective section. For oversized columns, the required minimum longitudinal reinforcement may be reduced by assuming the column area is in accordance with S5.7.4.2.

Strength reduction factor, $\varphi$, to be applied to the nominal axial resistance (S5.5.4.2)
For compression members with flexure, the value of $\varphi$ may be increased linearly from axial ( 0.75 ) to the value for flexure (0.9) as the factored axial load resistance, $\varphi \mathrm{P}_{\mathrm{n}}$, decreases from $0.10 f_{c} A_{g}$ to zero. The resistance factor is incorporated in the interaction diagram of the column shown graphically in Figure 7.2-8 and in tabulated form in Table 7.2-3.


Figure 7.2-8 - Column Interaction Diagram

Table 7.2-3 - Column Interaction Diagram in Tabulated Form

| $\mathbf{P ~ ( k ) ~}$ | $\mathbf{M}(\mathbf{k}-\mathbf{f t})$ | $\mathbf{P}(\mathbf{k})$ (cont.) | $\mathbf{M}(\mathbf{k}-\mathbf{f t})$ (cont.) |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\max }=2,555$ | 764 | 799 | 1,354 |
| 2,396 | 907 | 639 | 1,289 |
| 2,236 | 1,031 | 479 | 1,192 |
| 2,076 | 1,135 | 319 | 1,124 |
| 1,917 | 1,222 | 160 | 1,037 |
| 1,757 | 1,291 | 0 | 928 |
| 1,597 | 1,348 | -137 | 766 |
| 1,437 | 1,389 | -273 | 594 |
| 1,278 | 1,419 | -410 | 410 |
| 1,118 | 1,424 | -546 | 212 |
| 958 | 1,404 | -683 | 0 |

## Design Step <br> Slenderness effects

7.2.3.1

The effective length factor, $K$, is taken from S4.6.2.5. The slenderness moment magnification factors are typically determined in accordance with S4.5.3.2.2. Provisions specific to the slenderness of concrete columns are listed in S5.7.4.3.

Typically, the columns are assumed unbraced in the plane of the bent with the effective length factor, $K$, taken as 1.2 to account for the high rigidity of the footing and the pier cap. In the direction perpendicular to the bent $K$ may be determined as follows:

- If the movement of the cap is not restrained in the direction perpendicular to the bent, the column is considered not braced and the column is assumed to behave as a free cantilever. $K$ is taken equal to 2.1 (see Table SC4.6.2.5-1)
- If the movement of the cap is restrained in the direction perpendicular to the bent, the column is considered braced in this direction and $K$ is taken equal to 0.8 (see Table SC4.6.2.5-1)

For the example, the integral abutments provide restraint to the movements of the bent in the longitudinal direction of the bridge (approximately perpendicular to the bent). However, this restraint is usually ignored and the columns are considered unbraced in this direction, i.e. $\mathrm{K}=2.1$.

The slenderness ratio is calculated as $K \mathrm{I}_{\mathrm{u}} / \mathrm{r}$
where:
$\mathrm{K}=$ effective length factor taken as 1.2 in the plane of the bent and 2.1 in the direction perpendicular to the bent
$I_{u}=$ unbraced length calculated in accordance with S5.7.4.3 (ft.)
= distance from the top of the footing to the bottom of the cap
$=18 \mathrm{ft}$.
r = radius of gyration (ft.)
$=1 / 4$ the diameter of circular columns
$=0.875 \mathrm{ft}$.
For a column to be considered slender, $\left.K\right|_{u /} / r$ should exceed 22 for unbraced columns and, for braced columns, should exceed $34-12\left(M_{1} / M_{2}\right)$ where $M_{1}$ and $M_{2}$ are the smaller and larger end moments, respectively. The term $\left(M_{1} / M_{2}\right)$ is positive for single curvature flexure (S5.7.4.3)
$\underline{\text { Slenderness ratio in the plane of the bent }}$

$$
\begin{aligned}
\left.\mathrm{K}\right|_{\mathrm{u}} / \mathrm{r} & =1.2(18) /(0.875) \\
& =24.7>22 \text { therefore, the column is slightly slender }
\end{aligned}
$$

Slenderness ratio out of the plane of the bent

$$
\begin{aligned}
\left.\mathrm{K}\right|_{\mathrm{u}} / \mathrm{r} & =2.1(18) /(0.875) \\
& =43.2>22 \text { therefore, the column is slender }
\end{aligned}
$$

With the column slender in both directions, effect of slenderness needs to be considered.

Moment magnification in the bent
Longitudinal direction:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{cl}}=\delta_{\mathrm{b}} \mathrm{M}_{2 \mathrm{~b}}+\delta_{\mathrm{s}} \mathrm{M}_{2 \mathrm{~s}} \tag{S4.5.3.2.2b-1}
\end{equation*}
$$

where:

$$
\begin{align*}
& \delta_{\mathrm{b}}=\mathrm{C}_{\mathrm{m}} /\left[1-\left(\mathrm{P}_{\mathrm{u}} / \varphi \mathrm{P}_{\mathrm{e}}\right)\right] \geq 1.0  \tag{S4.5.3.2.2b-3}\\
& \delta_{\mathrm{s}}=1 /\left[1-\Sigma \mathrm{P}_{\mathrm{u}} / \varphi \Sigma \mathrm{P}_{\mathrm{e}}\right] \tag{S4.5.3.2.2b-4}
\end{align*}
$$

where:
$\mathrm{C}_{\mathrm{m}}=$ parameter of the effect of moment-curvature
$=1.0$ for members not braced for sidesway (S4.5.3.2.2b)
$\mathrm{P}_{\mathrm{u}} \quad=$ factored axial load for critical case, see Table 7.2-2 (k)
$=1,070 \mathrm{k}$
$\mathrm{P}_{\mathrm{e}} \quad=$ Euler buckling load (k)
$\varphi \quad=0.75$, resistance factor for axial compression (S5.5.4.2)
$\mathrm{M}_{2 \mathrm{~b}}=$ moment on compression member due to factored gravity loads that result in no appreciable sidesway calculated by conventional first-order elastic frame analysis, always positive ( k - ft )
$\mathrm{M}_{2 \mathrm{~s}}=$ moment on compression member due to factored lateral or gravity loads that result in sidesway, $\Delta$, greater than $\left.\right|_{\mathrm{u}} / 1500$, calculated by conventional first-order elastic frame analysis, always positive ( $\mathrm{k}-\mathrm{ft}$ )

Calculate $\mathrm{P}_{\mathrm{e}}$,

$$
\begin{equation*}
\mathrm{P}_{\mathrm{e}}=\pi^{2} \mathrm{EI} /\left(\left.\mathrm{K}\right|_{\mathrm{u}}\right)^{2} \tag{S4.5.3.2.2b-5}
\end{equation*}
$$

where:
EI $=$ column flexural stiffness calculated using the provisions of S5.7.4.3 and is taken as the greater of:

$$
\begin{equation*}
\mathrm{EI}=\left[\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{g}} / 5+\mathrm{E}_{\mathrm{s}} \mathrm{I}_{\mathrm{s}}\right] /\left(1+\beta_{\mathrm{d}}\right) \tag{S5.7.4.3-1}
\end{equation*}
$$

AND

$$
\begin{equation*}
\mathrm{EI}=\left[\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{g}} / 2.5\right] /\left(1+\beta_{\mathrm{d}}\right) \tag{S5.7.4.3-2}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{E}_{\mathrm{c}}= & \text { modulus of elasticity of concrete per S5.4.2.4 (ksi) } \\
= & 33,000 \mathrm{w}_{\mathrm{c}}^{1.5} \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}}=33,000(0.150)^{1.5} \sqrt{3} \\
= & 3,321 \mathrm{ksi} \\
\mathrm{I}_{\mathrm{g}}= & \text { moment of inertia of gross concrete section about the } \\
& \text { centroidal axis }\left(\mathrm{in}^{4}\right) \\
= & \pi \mathrm{r}^{4} / 4=\pi[1.75(12)]^{4} / 4 \\
= & 152,745 \mathrm{in}^{4}
\end{aligned}
$$

$\beta_{\mathrm{d}}=$ ratio of the maximum factored permanent load moment to the maximum factored total load moment, always positive. This can be determined for each separate load case, or for simplicity as shown here, it can be taken as the ratio of the maximum factored permanent load from all cases to the maximum factored total load moment from all cases at the point of interest.
$=\mathrm{M}_{1 \text { permanent }} / \mathrm{M}_{\mathrm{l} \text { total }}$
$=118.3 / 822$

$$
=0.144
$$

As a simplification, steel reinforcement in the column is ignored in calculating EI, therefore, neglect Eq. S5.7.4.3-1.

$$
\begin{aligned}
\mathrm{EI} & =[3,321(152,745) / 2.5] /(1+0.144) \\
& =1.77 \times 10^{8} \mathrm{k}-\mathrm{in}^{2} \\
\mathrm{~K} & =\text { effective length factor per Table SC4.6.2.5-1 } \\
& =2.1
\end{aligned}
$$

$$
\begin{aligned}
& \left.\quad\right|_{u}=\text { unsupported length of the compression member (in.) } \\
& =18(12) \\
& =216 \mathrm{in} . \\
& \mathrm{P}_{\mathrm{e}}=\pi^{2}\left(1.77 \times 10^{8}\right) /[2.1(216)]^{2} \\
& =8,490 \mathrm{k}
\end{aligned}
$$

Therefore, the moment magnification factors $\delta_{\mathrm{b}}$ and $\delta_{\mathrm{s}}$ can be calculated.

$$
\begin{aligned}
\delta_{\mathrm{b}} & =1.0 /[1-(1,070 /[0.75(8,490)])] \\
& =1.20 \\
\delta_{\mathrm{s}} & =1 /\left[1-\Sigma \mathrm{P}_{\mathrm{u}} / \varphi \Sigma \mathrm{P}_{\mathrm{e}}\right]
\end{aligned}
$$

$\Sigma \mathrm{P}_{\mathrm{u}}$ and $\Sigma \mathrm{P}_{\mathrm{e}}$ are the sum of the applied factored loads and the sum of the buckling loads of all columns in the bent, respectively. For hand calculations, it is not feasible to do calculations involving several columns simultaneously. Therefore, in this example, $\mathrm{P}_{\mathrm{u}}$ and $\mathrm{P}_{\mathrm{e}}$ of the column being designed are used instead of $\Sigma \mathrm{P}_{\mathrm{u}}$ and $\Sigma \mathrm{P}_{\mathrm{e}}$.
$\delta_{\mathrm{s}}=1.20$
Therefore, the magnified moment in the longitudinal direction is taken as:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{cl}} & =\delta_{\mathrm{b}} \mathrm{M}_{2 \mathrm{~b}}+\delta_{\mathrm{s}} \mathrm{M}_{2 \mathrm{~s}} \\
& =1.20\left(\mathrm{M}_{2 \mathrm{~b}}+\mathrm{M}_{2 \mathrm{~s}}\right) \\
& =1.20\left(\text { total factored moment, } \mathrm{M}_{\mathrm{l}}\right) \\
& =1.20(822) \\
& =986.4 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Transverse direction:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{ct}}=\delta_{\mathrm{b}} \mathrm{M}_{2 \mathrm{~b}}+\delta_{\mathrm{s}} \mathrm{M}_{2 \mathrm{~s}} \tag{S4.5.3.2.2b-1}
\end{equation*}
$$

Calculate $\mathrm{P}_{\mathrm{e}}$,
$P_{e}=\pi^{2} E I /\left(K I_{u}\right)^{2}$
where:
EI $=$ column flexural stiffness calculated using the provisions of S5.7.4.3 and is taken as the greater of:
$\mathrm{EI}=\left[\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{g}} / 5+\mathrm{E}_{\mathrm{s}} \mathrm{I}_{\mathrm{s}}\right] /\left(1+\beta_{\mathrm{d}}\right)$
AND

$$
\begin{equation*}
\mathrm{EI}=\left[\mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{g}} / 2.5\right] /\left(1+\beta_{\mathrm{d}}\right) \tag{S5.7.4.3-1}
\end{equation*}
$$

where:

$$
\mathrm{E}_{\mathrm{c}}=3,321 \mathrm{ksi}
$$

$$
\begin{aligned}
\mathrm{I}_{\mathrm{g}} & =152,745 \mathrm{in}^{4} \\
\beta_{\mathrm{d}} & =\mathrm{M}_{\mathrm{t} \text { permanent }} / \mathrm{M}_{\mathrm{t} \text { total }} \\
& =101.7 / 342 \\
& =0.30
\end{aligned}
$$

For simplification, steel reinforcement in the column is ignored in calculating EI, therefore, neglect Eq. S5.7.4.3-1.

$$
\begin{aligned}
& \mathrm{EI}=[3,321(152,745) / 2.5] /(1+0.30) \\
&=1.56 \times 10^{8} \mathrm{k}-\mathrm{in}^{2} \\
& \mathrm{~K}=1.2 \\
& \mathrm{I}_{\mathrm{u}}=216 \mathrm{in} . \\
& \mathrm{P}_{\mathrm{e}}=\pi^{2}\left(1.56 \times 10^{8}\right) /[1.2(216)]^{2} \\
&= 22,917 \mathrm{k}
\end{aligned}
$$

Therefore, the moment magnification factors $\delta_{\mathrm{b}}$ and $\delta_{\mathrm{s}}$ can be calculated.

$$
\begin{aligned}
\delta_{\mathrm{b}} & =1.0 /[1-(1,070 /[0.75(23,064)])] \\
& =1.07 \\
\delta_{\mathrm{s}} & =1 /\left[1-\Sigma \mathrm{P}_{\mathrm{u}} / \varphi \Sigma \mathrm{P}_{\mathrm{e}}\right]
\end{aligned}
$$

Similar to longitudinal, use $\mathrm{P}_{\mathrm{u}}$ and $\mathrm{P}_{\mathrm{e}}$ instead of $\Sigma \mathrm{P}_{\mathrm{u}}$ and $\Sigma \mathrm{P}_{\mathrm{e}}$.

$$
=1.07
$$

Therefore, the magnified moment in the transverse direction is taken as:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{ct}} & =1.07\left(\mathrm{total} \text { factored moment, } \mathrm{M}_{\mathrm{t}}\right) \\
& =1.07(174) \\
& =186 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

The combined moment $\mathrm{M}_{\mathrm{u}}$ is taken as:

$$
\begin{aligned}
\mathrm{M}_{\mathrm{u}} & =\sqrt{\mathrm{M}_{\mathrm{cl}}+\mathrm{M}_{\mathrm{ct}}} \\
& =\sqrt{986.4^{2}+186^{2}} \\
& =1004 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Factored axial load on the column for the load case being checked $=1,070 \mathrm{k}$
By inspection, from the column interaction diagram Figure 7.2-8 or Table 7.2-3, the applied factored loads ( $\mathrm{M}=1,004 \mathrm{k}-\mathrm{ft}$ and $\mathrm{P}=1,070 \mathrm{k}$ ) are within the column resistance.


Figure 7.2-9 - Column Cross-Section

## Design Step <br> 7.2.4

Footing design
Based on the intermediate bent load analysis, the critical footing is Footing 1 supporting Column 1

## Required information:

General:
$\mathrm{f}_{\mathrm{c}}^{\prime}=3.0 \mathrm{ksi}$
$\mathrm{f}_{\mathrm{y}}=60 \mathrm{ksi}$
Side concrete cover $=3$ in. $($ Table S5.12.3-1)
Top concrete cover $=3$ in.
Bottom concrete cover $=3$ in.
Top bars (T)ransverse or (L)ongitudinal in bottom mat $=\mathrm{L}$
Direction of bottom bars in bottom mat $=\mathrm{T}$

A preliminary analysis of the footing yielded the following information:
Footing depth $=3.0 \mathrm{ft}$.
Footing width, $\mathrm{W}=12.0 \mathrm{ft}$.
Footing length, $\mathrm{L}=12.0 \mathrm{ft}$.
Top mat reinforcing bar diameter, \#5 bars $=0.625 \mathrm{in}$.
Top mat reinforcing bar area, \#5 bars $=0.31 \mathrm{in}^{2}$
Bottom mat reinforcing bar diameter, \#9 bars $=1.128$ in.
Bottom mat reinforcing bar area, \#9 bars $=1.0 \mathrm{in}^{2}$
Number of bars $=13$ bars in each direction in both the top and bottom mats

## $\underline{\text { Location of critical sections }}$

According to S5.13.3.6.1, the critical section for one-way shear is at a distance $d_{v}$, the shear depth calculated in accordance with S5.8.2.9, from the face of the column. For two-way shear, the critical section is at a distance of $d_{v} / 2$ from the face of the column.

For moment, the critical section is taken at the face of the column in accordance with S5.13.3.4.

For the circular column in this example, the face of the column is assumed to be located at the face of an equivalent square area concentric with the circular column in accordance with S5.13.3.4.

## Determine the critical faces along the y -axis for moment

Since the column has a circular cross-section, the column may be transformed into an effective square cross-section for the footing analysis.

Critical face in $y$-direction $=1 / 2$ footing width, $\mathrm{W}-1 / 2$ equivalent column width
Equivalent column width $=\sqrt{\text { shaft area }}$

$$
\begin{aligned}
& =\sqrt{9.62} \\
& =3.10 \mathrm{ft} .
\end{aligned}
$$

Critical face in $y$-direction $=1 / 2$ footing width, $\mathrm{W}-1 / 2$ equivalent column width $=1 / 2(12)-1 / 2(3.10)$

$$
=4.45 \mathrm{ft}
$$

Critical faces in the y -direction $=4.45 \mathrm{ft}$. and 7.55 ft .

Determine the critical faces along the x -axis for moment
For a square footing with an equivalent square column:
Critical face in the $x$-direction $=$ Critical face in the $y$-direction $=4.45 \mathrm{ft}$.

Critical faces in the x -direction $=4.45 \mathrm{ft}$. and 7.55 ft .

See Figure 7.2-10 for a schematic showing the critical sections for moments.


Figure 7.2-10 - Critical Sections for Moment

## $\underline{\text { Design factored loads at the critical section }}$

From the analysis of the intermediate bent computer program, the cases of loading that produced maximum load effects and the other concurrent load effects on the footing are shown in Table 7.2-4.

Table 7.2-4 - Loads on Critical Footing (Footing Supporting Column 1)

| Load effect <br> maximized | Limit State | $\mathrm{M}_{\mathrm{t}}$ <br> $(\mathrm{k}-\mathrm{ft})$ | $\mathrm{M}_{\mathrm{l}}$ <br> $(\mathrm{k}-\mathrm{ft})$ | $\mathrm{P}_{\mathrm{u}}$ <br> $(\mathrm{k})$ |
| :---: | :---: | :---: | :---: | :---: |
| Positive $\mathrm{M}_{\mathrm{t}}$ | Strength V | 423 | 377 | 1,143 |
| Negative $\mathrm{M}_{\mathrm{t}}$ | Strength III | -154 | -197 | 628 |
| Positive $\mathrm{M}_{\mathrm{l}}$ | Strength V | 232 | 895 | 1,151 |
| Negative $\mathrm{M}_{\mathrm{l}}$ | Strength V | 158 | -897 | 1,157 |
| Axial Load P | Strength I | 121 | -363 | 1,374 |

Each row in Table 7.2-4 represents the maximum value of one load effect (max. $+\mathrm{M}_{\mathrm{t}},-\mathrm{M}_{1}$, etc.). The corresponding concurrent load effects are also given. Many engineers design the footing for the above listed cases. However, computer design programs are able to check many more cases of loading to determine the most critical case. For example, a load case that does not produce maximum axial load or maximum moment may still produce the maximum combined effects on the footing. From the output of a footing design program, the critical case for the footing design was found to produce the following factored footing loads under Strength I limit state:

$$
\begin{aligned}
& \mathrm{P}_{\mathrm{u}}=1,374 \mathrm{k} \\
& \mathrm{M}_{\mathrm{t}}=-121 \mathrm{k}-\mathrm{ft} \\
& \mathrm{M}_{\mathrm{l}}=626 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

The critical Service I loads:

$$
\begin{aligned}
& \mathrm{P}_{\mathrm{u}}=891 \mathrm{k} \\
& \mathrm{M}_{\mathrm{t}, \mathrm{~s}}=176 \mathrm{k}-\mathrm{ft} \\
& \mathrm{M}_{\mathrm{l}, \mathrm{~s}}=620 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

For the sample calculations below, the factored loads listed above for the critical case of loading were used.

Sample calculations for the critical footing under the critical case of loading
If $\mathrm{M} / \mathrm{P}<\mathrm{L} / 6$ then the soil under the entire area of the footing is completely in compression and the soil stress may be determined using the conventional stress formula (i.e. $\sigma=\mathrm{P} / \mathrm{A} \pm \mathrm{Mc} / \mathrm{I}$ ).

$$
\begin{aligned}
\mathrm{M}_{\mathrm{t}} / \mathrm{P}_{\mathrm{u}} & =121 / 1,374 \\
& =0.088<12 / 6=2 \text { OK } \\
\mathrm{M}_{\mathrm{l}} / \mathrm{P}_{\mathrm{u}} & =626 / 1,374 \\
& =0.456<2 \text { OK }
\end{aligned}
$$

Therefore, the soil area under the footing is under compression.

## Moment

For $\mathrm{M}_{\mathrm{ux}}(\mathrm{k}-\mathrm{ft} / \mathrm{ft})$, where $\mathrm{M}_{\mathrm{ux}}$ is the maximum factored moment per unit width of the footing due to the combined forces at a longitudinal face, see Figure 7.2-10:

$$
\sigma_{1}, \sigma_{2}=\mathrm{P} / \mathrm{LW} \pm \mathrm{M}_{1}(\mathrm{~L} / 2) /\left(\mathrm{L}^{3} \mathrm{~W} / 12\right)
$$

where:
$\sigma_{1}=$ stress at beginning of footing in direction considered (see Figure 7.2-10) (ksf)
$\sigma_{2}=$ stress at end of footing in direction considered (ksf)
$\mathrm{P}=$ axial load from above (k)
$\mathrm{M}_{1}=$ moment on longitudinal face from above ( $\mathrm{k}-\mathrm{ft}$ )
$\mathrm{L}=$ total length of footing (ft.)
$\mathrm{W}=$ total width of footing (ft.)
$\sigma_{1}=1,374 /[12(12)]+626(12 / 2) /\left[12^{3}(12) / 12\right]$
$=9.54+2.17$
$=11.71 \mathrm{ksf}$

$$
\sigma_{2}=9.54-2.17
$$

$$
=7.37 \mathrm{ksf}
$$

Interpolate to calculate $\sigma_{3}$, the stress at critical location for moment (at face of column, 4.45 ft . from the end of the footing along the width.

$$
\sigma_{3}=10.10 \mathrm{ksf}
$$

Therefore,

$$
\mathrm{M}_{\mathrm{ux}}=\sigma_{3} \mathrm{~L}_{1}\left(\mathrm{~L}_{1} / 2\right)+0.5\left(\sigma_{1}-\sigma_{3}\right)\left(\mathrm{L}_{1}\right)\left(2 \mathrm{~L}_{1} / 3\right)
$$

where:
$\mathrm{L}_{1}=$ distance from the edge of footing to the critical location (ft.)

$$
\begin{aligned}
\mathrm{M}_{\mathrm{ux}} & =10.10(4.45)(4.45 / 2)+0.5(11.71-10.10)(4.45)[2(4.45) / 3] \\
& =100.0+10.63 \\
& =110.6 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

For $\mathrm{M}_{\mathrm{uy}}(\mathrm{k}-\mathrm{ft} / \mathrm{ft})$, where $\mathrm{M}_{\mathrm{uy}}$ is the maximum factored moment per unit length from the combined forces at a transverse face acting at 4.45 ft . from the face of the column (see Figure 7.2-10):

$$
\sigma_{5}, \sigma_{6}=\mathrm{P} / \mathrm{LW} \pm \mathrm{M}_{\mathrm{t}}(\mathrm{~W} / 2) /\left(\mathrm{W}^{3} \mathrm{~L} / 12\right)
$$

where:
$\mathrm{M}_{\mathrm{t}}=$ moment on transverse face from above ( k - ft )

$$
\begin{aligned}
\sigma_{5} & =1,374 /[12(12)]-(-121)(12 / 2) /\left[12^{3}(12) / 12\right] \\
& =9.54-(-0.420) \\
& =9.96 \mathrm{ksf} \\
\sigma_{6} & =9.54+(-0.420) \\
& =9.12 \mathrm{ksf}
\end{aligned}
$$

Interpolate to calculate $\sigma_{7}$, the stress at critical location for moment (at face of column, 4.45 ft . from the end of the footing along the length).

$$
\sigma_{7}=9.65 \mathrm{ksf}
$$

Therefore,

$$
\begin{aligned}
\mathrm{M}_{\mathrm{uy}} & =\sigma_{7} \mathrm{~L}_{3}\left(\mathrm{~L}_{3} / 2\right)+0.5\left(\sigma_{5}-\sigma_{7}\right)\left(\mathrm{L}_{3}\right)\left(2 \mathrm{~L}_{3} / 3\right) \\
& =9.65(4.45)(4.45 / 2)+0.5(9.96-9.65)(4.45)[2(4.45) / 3] \\
& =95.54+2.05 \\
& =97.6 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Factored applied design moment, Service I limit state, calculated using the same method as above:

$$
\begin{aligned}
& \mathrm{M}_{\mathrm{ux}, \mathrm{~s}}=75.9 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \\
& \mathrm{M}_{\mathrm{uy}, \mathrm{~s}}=72.0 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Where $\mathrm{M}_{\mathrm{ux}, \mathrm{s}}$ is the maximum service moment from combined forces at a longitudinal face at 4.45 ft . along the width and $\mathrm{M}_{\mathrm{uy}, \mathrm{s}}$ is the maximum service moment from combined forces at a transverse face at 7.55 ft . along the length.

## Shear

Factored applied design shear.
For $V_{u x}(k / f t)$, where $V_{u x}$ is the shear per unit length at a longitudinal face:

$$
\mathrm{V}_{\mathrm{ux}}=\sigma_{4} \mathrm{~L}_{2}+0.5\left(\sigma_{1}-\sigma_{4}\right) \mathrm{L}_{2}
$$

where:
$L_{2}=$ distance from the edge of footing to a distance $d_{v}$ from the effective column (ft.)

Based on the preliminary analysis of the footing, $\mathrm{d}_{\mathrm{v}}$ is estimated as 30.3 in . Generally, for load calculations, $d_{v}$ may be assumed equal to the effective depth of the reinforcement minus 1 inch. Small differences between $d_{v}$ assumed here for load calculations and the final $\mathrm{d}_{\mathrm{v}}$ will not result in significant difference in the final results.

The critical face along the $y$-axis $=4.45-30.3 / 12$

$$
=1.925 \mathrm{ft} . \text { from the edge of the footing }
$$

By interpolation between $\sigma_{1}$ and $\sigma_{2}, \sigma_{4}=11.01 \mathrm{ksf}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{ux}} & =11.01(1.925)+0.5(11.71-11.01)(1.925) \\
& =21.19+0.67 \\
& =21.9 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

For $\mathrm{V}_{\mathrm{uy}}(\mathrm{k} / \mathrm{ft})$, where $\mathrm{V}_{\mathrm{uy}}$ is the shear per unit length at a transverse face:

$$
\mathrm{V}_{\mathrm{ux}}=\sigma_{8} \mathrm{~L}_{4}+0.5\left(\sigma_{5}-\sigma_{8}\right) \mathrm{L}_{4}
$$

where:
$\mathrm{d}_{\mathrm{v}}=31.4$ in. for this direction (from preliminary design). Alternatively, for load calculations, $\mathrm{d}_{\mathrm{v}}$ may be assumed equal to the effective depth of the reinforcement minus 1 inch).

The critical face along the x -axis $=4.45-31.4 / 12$

$$
=1.833 \mathrm{ft} \text {. from the edge of the footing }
$$

By interpolation between $\sigma_{5}$ and $\sigma_{6}, \sigma_{8}=9.83 \mathrm{ksf}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{ux}} & =9.83(1.83)+0.5(9.96-9.83)(1.83) \\
& =17.99+0.12 \\
& =18.1 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$



Figure 7.2-11 - Stress at Critical Locations for Moment and Shear

## Design Step

Flexural resistance (S5.7.3.2)
7.2.4.1

Check the design moment strength (S5.7.3.2)
Article S5.13.3.5 allows the reinforcement in square footings to be uniformly distributed across the entire width of the footing.

Check the moment resistance for moment at the critical longitudinal face (S5.13.3.4)
The critical section is at the face of the effective square column ( 4.45 ft . from the edge of the footing along the width). In the case of columns that are not rectangular, the critical section is taken at the side of the concentric rectangle of equivalent area as in this example.

$$
\begin{equation*}
\mathrm{M}_{\mathrm{rx}}=\varphi \mathrm{M}_{\mathrm{nx}} \tag{S5.7.3.2.1-1}
\end{equation*}
$$

where:

$$
\begin{array}{ll}
\varphi & =0.9(\mathrm{~S} 5.5 .4 .2 .1) \\
\mathrm{M}_{\mathrm{nx}} & =\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{sx}}-\mathrm{a} / 2\right) \tag{S5.7.3.2.2-1}
\end{array}
$$

Determine $\mathrm{d}_{\mathrm{sX}}$, the distance from the top bars of the bottom reinforcing mat to the compression surface.
$\mathrm{d}_{\mathrm{sx}}=$ footing depth - bottom cvr - bottom bar dia. $-1 / 2$ top bar dia. in bottom mat $=3(12)-3-1.128-1 / 2(1.128)$
$=31.3 \mathrm{in}$.


Figure 7.2-12 - Footing Reinforcement Locations

Determine As per foot of length. The maximum bar spacing across the width of the footing is assumed to be 12.0 in . in each direction on all faces (S5.10.8.2). Use 13 \#9 bars and determine the actual spacing.

$$
\begin{aligned}
\text { Actual bar spacing } & =[\mathrm{L}-2(\text { side cover })-\mathrm{bar} \text { diameter }] /\left(\mathrm{n}_{\text {bars }}-1\right) \\
& =[12-2(3) / 12-1.128 / 12] /(13-1) \\
& =11.41 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}} & =1.0(12 / 11.41) \\
& =1.05 \mathrm{in}^{2}
\end{aligned}
$$

Determine "a", the depth of the equivalent stress block.

$$
\begin{equation*}
\mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} / 0.85 \mathrm{f}_{\mathrm{c}} \mathrm{~b} \tag{S5.7.3.1.1-4}
\end{equation*}
$$

for a strip 12 in . wide, $\mathrm{b}=12 \mathrm{in}$. and $\mathrm{A}_{\mathrm{s}}=1.05 \mathrm{in}^{2}$

$$
\begin{aligned}
\mathrm{a} & =1.05(60) /[0.85(3)(12)] \\
& =2.06 \mathrm{in} .
\end{aligned}
$$

Calculate $\varphi \mathrm{M}_{\mathrm{nx}}$, the factored flexural resistance.

$$
\begin{align*}
\mathrm{M}_{\mathrm{rx}} & =\varphi \mathrm{M}_{\mathrm{nx}} \\
& =0.9[1.05(60)(31.3-2.06 / 2)] / 12 \quad(\mathrm{~S} 5.7 .3 .2 .2-1)  \tag{S5.7.3.2.2-1}\\
& =143.0 \mathrm{k}-\mathrm{ft} / \mathrm{ft}>\text { applied factored moment, } \mathrm{M}_{\mathrm{ux}}=110.6 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \text { OK }
\end{align*}
$$

Check minimum temperature and shrinkage steel (S5.10.8)
According to S5.10.8.1, reinforcement for shrinkage and temperature stresses shall be provided near surfaces of concrete exposed to daily temperature changes and in structural mass concrete. Footings are not exposed to daily temperature changes and, therefore, are not checked for temperature and shrinkage reinforcement. Nominal reinforcement is provided at the top of the footing to arrest possible cracking during the concrete early age before the footing is covered with fill.

## Design Step <br> Limits for reinforcement (S5.7.3.3)

7.2.4.2

Check maximum reinforcement (S5.7.3.3.1)

$$
\begin{equation*}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \leq 0.42 \tag{S5.7.3.3.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{c} & =\mathrm{a} / \beta_{1} \\
& =2.06 / 0.85 \\
& =2.42 \mathrm{in} / \mathrm{ft}
\end{aligned}
$$

$$
\mathrm{c} / \mathrm{d}_{\mathrm{e}}=2.42 / 31.3
$$

$$
=0.077<0.42 \text { OK }
$$

## Minimum reinforcement check (S5.7.3.3.2)

Unless otherwise specified, at any section of a flexural component, the amount of nonprestressed tensile reinforcement shall be adequate to develop a factored flexural resistance, $\mathrm{M}_{\mathrm{r}}$, at least equal to the lesser of:

$$
1.2 \mathrm{M}_{\mathrm{cr}}=1.2 \mathrm{f}_{\mathrm{r}} \mathrm{~S}
$$

where:

$$
\begin{align*}
\mathrm{f}_{\mathrm{r}} & =0.24 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}}  \tag{S5.4.2.6}\\
& =0.24 \sqrt{3} \\
& =0.42 \mathrm{ksi}
\end{align*}
$$

For a 1 ft . wide strip, 3 ft . thick,

$$
\begin{aligned}
\mathrm{S} & =\mathrm{bh}^{2} / 6 \\
& =[1(12)][3(12)]^{2} / 6 \\
& =2,592 \mathrm{in}^{3} / \mathrm{ft}
\end{aligned}
$$

$$
\begin{aligned}
1.2 \mathrm{M}_{\mathrm{cr}} & =1.2(0.42)(2,592) / 12 \\
& =108.9 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
1.33 \mathrm{M}_{\mathrm{ux}} & =1.33(110.6) \\
& =147.1 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Therefore, the minimum required section moment resistance $=108.9 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Provided moment resistance $=143.0 \mathrm{k}-\mathrm{ft} / \mathrm{ft}>108.9 \mathrm{k}$-ft/ft OK

Check the moment resistance for moment at the critical transverse face
The critical face is at the equivalent length of the shaft ( 7.55 ft . from the edge of the footing along the length). In the case of columns that are not rectangular, the critical section is taken at the side of the concentric rectangle of equivalent area.

$$
\begin{align*}
\mathrm{M}_{\mathrm{ry}} & =\varphi \mathrm{M}_{\mathrm{ny}} \\
& =\varphi\left[\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}\left(\mathrm{~d}_{\mathrm{sy}}-\mathrm{a} / 2\right)\right] \tag{S5.7.3.2.2-1}
\end{align*}
$$

Determine $d_{\text {sy }}$, the distance from the bottom bars of the bottom reinforcing mat to the compression surface.

$$
\begin{aligned}
\mathrm{d}_{\text {sy }} & =\text { footing depth }- \text { cover }-1 / 2(\text { bottom bar diameter }) \\
& =3(12)-3-1 / 2(1.128) \\
& =32.4 \mathrm{in} .
\end{aligned}
$$

Determine $A_{s}$ per foot of length
Actual bar spacing $=[\mathrm{W}-2($ side cover $)-$ bar diameter $] /\left(n_{\text {bars }}-1\right)$

$$
=[12-2(3) / 12-1.128 / 12] /(13-1)
$$

$$
=11.41 \mathrm{in} .
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{s}} & =1.0(12 / 11.41) \\
& =1.05 \mathrm{in}^{2}
\end{aligned}
$$

Determine " a ", depth of the equivalent stress block.

$$
\mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} /\left(0.85 \mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{b}\right)
$$

For a strip 12 in. wide, $\mathrm{b}=12 \mathrm{in}$. and $\mathrm{A}_{\mathrm{s}}=1.05 \mathrm{in}^{2}$

$$
\begin{aligned}
\mathrm{a} & =1.05(60) /[0.85(3)(12)] \\
& =2.06 \mathrm{in} .
\end{aligned}
$$

Calculate $\varphi \mathrm{M}_{\mathrm{ny}}$, the factored flexural resistance

$$
\begin{aligned}
\mathrm{M}_{\mathrm{ry}} & =\varphi \mathrm{M}_{\mathrm{ny}} \\
& =0.9[1.05(60)(32.4-2.06 / 2)] / 12 \\
& =148.2 \mathrm{k}-\mathrm{ft} / \mathrm{ft}>\mathrm{M}_{\mathrm{uy}}=97.6 \mathrm{k}-\mathrm{ft} / \mathrm{ft} \quad \mathbf{O K}
\end{aligned}
$$

Check maximum reinforcement (S5.7.3.3.1)

$$
\begin{equation*}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} \leq 0.42 \tag{S5.7.3.3.1-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{c} & =\mathrm{a} / \beta_{1} \\
& =2.06 / 0.85 \\
& =2.42 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{c} / \mathrm{d}_{\mathrm{e}} & =2.42 / 32.4 \\
& =0.075<0.42 \text { OK }
\end{aligned}
$$

## Check minimum reinforcement (S5.7.3.3.2)

Unless otherwise specified, at any section of a flexural component, the amount of nonprestressed tensile reinforcement shall be adequate to develop a factored fexural resistance, $\mathrm{M}_{\mathrm{r}}$, at least equal to the lesser of:

$$
1.2 \mathrm{M}_{\mathrm{cr}}=1.2 \mathrm{f}_{\mathrm{r}} \mathrm{~S}
$$

where:

$$
\begin{align*}
\mathrm{f}_{\mathrm{r}} & =0.24 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}}  \tag{S5.4.2.6}\\
& =0.24 \sqrt{3} \\
& =0.42 \mathrm{ksi}
\end{align*}
$$

For a 1 ft . wide strip, 3 ft . thick,

$$
S=\mathrm{bh}^{2} / 6
$$

$$
=[1(12)][3(12)]^{2} / 6
$$

$$
=2,592 \mathrm{in}^{3}
$$

$$
\begin{aligned}
1.2 \mathrm{M}_{\mathrm{cr}} & =1.2(0.42)(2,592) / 12 \\
& =108.9 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

OR

$$
\begin{aligned}
1.33 \mathrm{M}_{\mathrm{uy}} & =1.33(97.6) \\
& =129.8 \mathrm{k}-\mathrm{ft} / \mathrm{ft}
\end{aligned}
$$

Therefore, the minimum required section moment resistance $=108.9 \mathrm{k}-\mathrm{ft} / \mathrm{ft}$
Provided moment resistance $=148.2 \mathrm{k}$ - ft/ft > 108.9 k -ft/ft OK

## Design Step

7.2.4.3

## Control of cracking by distribution of reinforcement (S5.7.3.4)

Check distribution about footing length, L

$$
\begin{equation*}
\mathrm{f}_{\mathrm{s} \text {, allow }}=\mathrm{Z} /\left(\mathrm{d}_{\mathrm{c}} \mathrm{~A}\right)^{1 / 3} \leq 0.60 \mathrm{f}_{\mathrm{y}} \tag{S5.7.3.4-1}
\end{equation*}
$$

where:
$\mathrm{Z}=170 \mathrm{k} / \mathrm{in}$. (moderate exposure conditions assumed, no dry/wet cycles and no harmful chemicals in the soil)

Notice that the value of the of the crack control factor, Z, used by different jurisdictions varies based on local conditions and past experience.
$d_{c}=$ bottom cover $+1 / 2$ bar diameter
$=2+1 / 2(1.128)$
$=2.56 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{A} & =2 \mathrm{~d}_{\mathrm{c}}(\text { bar spacing }) \\
& =2(2.56)(11.41) \\
& =58.4 \text { in }^{2}
\end{aligned}
$$

$\mathrm{f}_{\mathrm{s} \text {, allow }}=\mathrm{Z} /\left[\left(\mathrm{d}_{\mathrm{c}} \mathrm{A}\right)^{1 / 3}\right]$
$=170 /[2.56(58.4)]^{1 / 3}$
$=32.0 \mathrm{ksi}<0.6(60)=36 \mathrm{ksi}$ therefore, use $\mathrm{f}_{\mathrm{s} \text {, allow }}=32.0 \mathrm{ksi}$

## Check actual steel stress, $\mathrm{f}_{\mathrm{s} . \text { actual }}$

For 3.0 ksi concrete, the modular ratio, $n=9$
Maximum service load moment as shown earlier $=77.3 \mathrm{k}$ - ft

The transformed moment of inertia is calculated assuming elastic behavior, i.e., linear stress and strain distribution. In this case, the first moment of area of the transformed steel on the tension side about the neutral axis is assumed equal to that of the concrete in compression.

Assume the neutral axis at a distance " $y$ " from the compression face of the section.
Section width $=$ bar spacing $=11.41 \mathrm{in}$.
Transformed steel area $=($ bar area $)($ modular ratio $)=1.0(9)=9.0 \mathrm{in}^{2}$
By equating the first moment of area of the transformed steel about that of the concrete, both about the neutral axis:

$$
9.0(31.3-\mathrm{y})=11.41 \mathrm{y}(\mathrm{y} / 2)
$$

Solving the equation results in $\mathrm{y}=6.28 \mathrm{in}$.

$$
\begin{aligned}
\mathrm{I}_{\text {transformed }} & =\mathrm{A}_{\mathrm{ts}}\left(\mathrm{~d}_{\mathrm{sx}}-\mathrm{y}\right)^{2}+\mathrm{by}^{3} / 3 \\
& =9.0(31.3-6.28)^{2}+11.41(6.28)^{3} / 3 \\
& =6,576 \mathrm{in}^{4}
\end{aligned}
$$

Stress in the steel, $\mathrm{f}_{\mathrm{s}}$, actual $=\left(\mathrm{M}_{\mathrm{s}} \mathrm{c} / \mathrm{I}\right) \mathrm{n}$, where $\mathrm{M}_{\mathrm{s}}$ is the moment acting on the 11.41 in . wide section.

$$
\begin{aligned}
\mathrm{f}_{\mathrm{s}, \text { actual }} & =[77.3(11.41)(31.3-6.28) / 6,576] 9 \\
& =30.2 \mathrm{ksi}<\mathrm{f}_{\mathrm{s}, \text { allow }}=32.0 \mathrm{ksi} \text { OK }
\end{aligned}
$$



Figure 7.2-13 - Crack Control for Top Bar Reinforcement Under Service Load

## Check distribution about footing width, W

This check is conducted similarly to the check shown above for the distribution about the footing length and the reinforcement is found to be adequate.

## Design Step

Shear analysis
7.2.4.4

Check design shear strength (S5.8.3.3)
According to S5.13.3.6.1, the most critical of the following conditions shall govern the design for shear:

- One-way action, with a critical section extending in a plane across the entire width and located at a distance taken as specified in S5.8.3.2.
- Two-way action, with a critical section perpendicular to the plane of the slab and located so that its perimeter, $b_{o}$, is a minimum but not closer than $0.5 d_{v}$ to the perimeter of the concentrated load or reaction area.

The subscripts " $x$ " and " $y$ " in the next section refer to the shear at a longitudinal face and shear at a transverse face, respectively.

Determine the location of the critical face along the $y$-axis
Since the column has a circular cross-section, the column may be transformed into an effective square cross-section for the footing analysis.

As stated previously, the critical section for one-way shear is at a distance $d_{v}$, the shear depth calculated in accordance with S5.8.2.9, from the face of the column and for twoway shear at a distance of $d_{v} / 2$ from the face of the column.

Determine the effective shear depth, $\mathrm{d}_{\mathrm{vx}}$, for a longitudinal face.

$$
\begin{align*}
\mathrm{d}_{\mathrm{vx}} & =\text { effective shear depth for a longitudinal face per S5.8.2.9 (in.) } \\
& =\mathrm{d}_{\mathrm{sx}}-\mathrm{a} / 2  \tag{S5.8.2.9}\\
& =31.3-2.06 / 2 \\
& =30.3 \mathrm{in} .
\end{align*}
$$

but not less than:

$$
\begin{aligned}
0.9 \mathrm{~d}_{\mathrm{sx}} & =0.9(31.3) \\
& =28.2 \mathrm{in} . \\
0.72 \mathrm{~h} & =0.72(36) \\
& =25.9 \mathrm{in} .
\end{aligned}
$$

Therefore, use $\mathrm{d}_{\mathrm{vx}}=30.3 \mathrm{in}$.
The critical face along the $y$-axis $=4.45-30.3 / 12$

$$
=1.925 \mathrm{ft} . \text { from the edge of the footing }
$$

Determine the location of the critical face along the x -axis

Determine the effective shear depth, $\mathrm{d}_{\mathrm{vy}}$, for a transverse face.

$$
\begin{aligned}
\mathrm{d}_{\mathrm{vy}} & =\text { effective shear depth for a transverse face per S5.8.2.9 (in.) } \\
& =\mathrm{d}_{\mathrm{sy}}-\mathrm{a} / 2 \\
& =32.4-2.06 / 2 \\
& =31.4 \mathrm{in} .
\end{aligned}
$$

but not less than:

$$
\begin{aligned}
0.9 \mathrm{~d}_{\text {sy }} & =0.9(32.4) \\
& =29.2 \mathrm{in} . \\
0.72 \mathrm{~h} & =0.72(36) \\
& =25.9 \mathrm{in} .
\end{aligned}
$$

Therefore, use $\mathrm{d}_{\mathrm{vy}}=31.4 \mathrm{in}$.
The critical face along the x -axis $=4.45-31.4 / 12$

$$
=1.833 \mathrm{ft} . \text { from the edge of the footing }
$$

See Figure 7.2-14 for locations of the critical sections.


Figure 7.2-14 - Critical Sections for Shear

Determine one-way shear capacity for longitudinal face (S5.8.3.3)
For one-way action, the shear resistance of the footing of slab will satisfy the requirements specified in S5.8.3.

$$
\begin{equation*}
\mathrm{V}_{\mathrm{rx}}=\varphi \mathrm{V}_{\mathrm{nx}} \tag{S5.8.2.1-2}
\end{equation*}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{nx}}$, is taken as the lesser of:

$$
\begin{equation*}
V_{n x}=V_{c}+V_{s}+V_{p} \tag{S5.8.3.3-1}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{nx}}=0.25 \mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{vx}}+\mathrm{V}_{\mathrm{p}} \tag{S5.8.3.3-2}
\end{equation*}
$$

$$
\begin{equation*}
\mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{\mathrm{~F}_{\mathrm{c}}^{\mathrm{b}}}{ }_{\mathrm{v}} \mathrm{~d}_{\mathrm{vx}} \tag{S5.8.3.3-3}
\end{equation*}
$$

where:

$$
\begin{aligned}
\beta & =2.0 \\
\mathrm{~b}_{\mathrm{v}} & =12 \text { in. (to obtain shear per foot of footing) } \\
\mathrm{d}_{\mathrm{vx}} & =\text { effective shear depth for a longitudinal face per S5.8.2.9 (in.) } \\
& =30.3 \text { in. from above } \\
\mathrm{V}_{\mathrm{p}} & =0.0 \mathrm{k}
\end{aligned}
$$

The nominal shear resistance is then taken as the lesser of:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{nx}} & =0.0316(2.0) \sqrt{3}(12)(30.3) \\
& =39.8 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

AND

$$
\begin{aligned}
\mathrm{V}_{\mathrm{nx}} & =0.25 \mathrm{f}_{\mathrm{c}} \mathrm{~b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \\
& =0.25(3)(12)(30.3) \\
& =272.7 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Therefore, use $\mathrm{V}_{\mathrm{nx}}=39.8 \mathrm{k} / \mathrm{ft}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{rx}} & =\varphi \mathrm{V}_{\mathrm{nx}} \\
& =0.9(39.8) \\
& =35.8 \mathrm{k} / \mathrm{ft}>\text { applied shear, } \mathrm{V}_{\mathrm{ux}}=21.9 \mathrm{k} / \mathrm{ft} \text { (calculated earlier) } \mathbf{O K}
\end{aligned}
$$

Determine one-way shear capacity for transverse face

$$
\begin{equation*}
\mathrm{V}_{\mathrm{ry}}=\varphi \mathrm{V}_{\mathrm{ny}} \tag{S5.8.2.1-2}
\end{equation*}
$$

The nominal shear resistance, $\mathrm{V}_{\mathrm{nx}}$, is taken as the lesser of:

$$
\begin{equation*}
V_{n y}=V_{c}+V_{s}+V_{p} \tag{S5.8.3.3-1}
\end{equation*}
$$

OR

$$
\begin{equation*}
\mathrm{V}_{\mathrm{ny}}=0.25 \mathrm{f}_{\mathrm{c}} \mathrm{~b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{vy}}+\mathrm{V}_{\mathrm{p}} \tag{S5.8.3.3-2}
\end{equation*}
$$

$$
\begin{equation*}
\mathrm{V}_{\mathrm{c}}=0.0316 \beta \sqrt{{ }_{\mathrm{c}} \mathrm{c}_{\mathrm{c}}} \mathrm{~d}_{\mathrm{vy}} \tag{S5.8.3.3-3}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \beta=2.0 \\
& b_{v}=12 \text { in. (to obtain shear per foot of footing) }
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{d}_{\mathrm{vy}} & =\text { effective shear depth for a transverse face per S5.8.2.9 (in.) } \\
& =31.4 \text { in. from above } \\
\mathrm{V}_{\mathrm{p}} & =0.0 \mathrm{k}
\end{aligned}
$$

The nominal shear resistance is then taken as the lesser of:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{cy}} & =0.0316(2.0) \sqrt{3}(12)(31.4) \\
& =41.2 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

AND

$$
\begin{aligned}
\mathrm{V}_{\mathrm{ny}} & =0.25 \mathrm{f}_{\mathrm{c}} \mathrm{~b}_{\mathrm{v}} \mathrm{~d}_{\mathrm{v}} \\
& =0.25(3)(12)(31.4) \\
& =282.6 \mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Therefore, use $\mathrm{V}_{\mathrm{ny}}=41.2 \mathrm{k} / \mathrm{ft}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{ry}} & =\varphi \mathrm{V}_{\mathrm{ny}} \\
& =0.9(41.2) \\
& =37.1 \mathrm{k} / \mathrm{ft}>\text { applied shear, } \mathrm{V}_{\mathrm{uy}}=18.1 \mathrm{k} / \mathrm{ft} \text { (calculated earlier) } \mathbf{O K}
\end{aligned}
$$

Determine two-way (punching) shear capacity at the column (S5.13.3.6.3)
For two-way action for sections without transverse reinforcement, the nominal shear resistance, $\mathrm{V}_{\mathrm{n}}$ in kips, of the concrete shall be taken as:

$$
\mathrm{V}_{\mathrm{n}}=\left(0.063+0.126 / \beta_{\mathrm{c}}\right) \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \mathrm{b}_{\mathrm{o}} \mathrm{~d}_{\mathrm{v}} \leq 0.126 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime} \mathrm{b}_{\mathrm{o}}} \mathrm{~d}_{\mathrm{v}}(\text { S5.13.3.6.3-1 })
$$

where:
$\beta_{c}=$ ratio of long side to short side of the rectangular through which the concentrated load or reaction force is transmitted
$=$ (column equivalent length) / (column equivalent width)
= 3.10/3.10
$=1.0$ (notice, for circular columns this ratio is always 1.0)
$\mathrm{d}_{\mathrm{v}}=$ average effective shear depth (in.)
$=\left(\mathrm{d}_{\mathrm{vx}}+\mathrm{d}_{\mathrm{vy}}\right) / 2$
$=(30.3+31.4) / 2$
$=30.9$ in.
$b_{o}=$ perimeter of the critical section (in.), the critical section is $0.5 d_{v}$ from the reaction area (S5.13.3.6.1). Use the circular column crosssection and cylindrical surface for punching shear.

$$
\begin{aligned}
& =2 \pi(42 / 2+30.9 / 2) \\
& =229 \mathrm{in} .
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =(0.063+0.126 / 1.0) \sqrt{3}(229)(30.9) \\
& =2,316 \mathrm{k}
\end{aligned}
$$

The nominal shear resistance, $V_{n}$, cannot exceed $0.126 \sqrt{\mathrm{f}_{\mathrm{c}}^{\prime}} \mathrm{b}_{\mathrm{o}} \mathrm{d}_{\mathrm{v}}$

$$
\begin{aligned}
\mathrm{V}_{\mathrm{n}} & =0.126 \sqrt{3}(229)(30.9) \\
& =1,544 \mathrm{k}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\mathrm{V}_{\mathrm{r}} & =0.9(1,544) \\
& =1,390 \mathrm{k}
\end{aligned}
$$

The maximum factored vertical force for punching shear calculations equals the maximum factored axial load on the footing minus the factored weight of the footing.

$$
\begin{aligned}
\mathrm{P}_{2 \text { way }} & =1,374-1.25[12(12)(3)](0.150) \\
& =1,293 \mathrm{k}
\end{aligned}
$$

The maximum shear force for punching shear calculations fr a footing with the entire footing area under compression and the column at the center of the footing:

$$
\begin{aligned}
\mathrm{V}_{2 \text { way }} & =\mathrm{P}_{2 \text { way }}(1-\text { area within punching shear perimeter/footing area }) \\
& =1,293\left[1-\pi((42 / 2+30.9 / 2) / 12)^{2} / 12(12)\right] \\
& =1,293(1-0.201) \\
& =1,033 \mathrm{k}<\mathrm{V}_{\mathrm{r}}=1,390 \mathrm{k} \mathrm{OK}
\end{aligned}
$$

For footings with eccentric columns or with tension under some of the footing area, the design force for punching shear is calculated as the applied load, $\mathrm{P}_{2 \text { way }}$, minus the soil load in the area within the perimeter of the punching shear failure.

## Design Step

 7.2.4.5Foundation soil bearing resistance at the Strength Limit State (S10.6.3)
Foundation assumptions:
Footings rest on dry cohesionless soil
Angle of internal friction of the soil $\left(\varphi_{f}\right)=32$ degrees
Depth of the bottom of the footing from the ground surface $=6 \mathrm{ft}$.
Soil density $=120 \mathrm{lb} / \mathrm{ft}^{3}$
Footing plan dimensions are 12 ft . by 12 ft .

## Footing effective dimensions

According to S10.6.3.1.1, where loads are eccentric, the effective footing dimensions $L^{\prime}$ and $B^{\prime}$, as specified in S10.6.3.1.5, shall be used instead of the overall dimensions $L$ and $B$ in all equations, tables, and figures pertaining to bearing capacity.

Therefore, for each load case shown in Table 7.2-4, a unique combination of the footing effective dimensions is used. In the following section, the case of maximum axial load on the footing will be used to illustrate the bearing capacity calculations.

The footing effective dimensions are calculated using S10.6.3.1.5 and Figure SC10.6.3.1.5-1 (shown below).

$$
\begin{equation*}
\mathrm{B}^{\prime}=\mathrm{B}-2 \mathrm{e}_{\mathrm{B}} \tag{S10.6.3.1.5-1}
\end{equation*}
$$

where:
$\mathrm{e}_{\mathrm{B}}=$ eccentricity parallel to dimension $\mathrm{B}(\mathrm{ft}$.

$$
\begin{align*}
\mathrm{B}^{\prime} & =12-2(121 / 1,374) \\
& =11.82 \mathrm{ft} . \\
\mathrm{L}^{\prime} & =\mathrm{L}-2 \mathrm{e}_{\mathrm{L}} \tag{S10.6.3.1.5-2}
\end{align*}
$$

where:
$\mathrm{e}_{\mathrm{L}}=$ eccentricity parallel to dimension $\mathrm{L}(\mathrm{ft}$.

$$
\begin{aligned}
\mathrm{L}^{\prime} & =12-2(626 / 1,374) \\
& =11.09 \mathrm{ft} .
\end{aligned}
$$



Figure SC10.6.3.1.5-1 - Reduced Footing Dimensions (Reproduced from the Specifications)

According to S10.6.3.1.2c, for cohesionless soil, the nominal bearing resistance of a layer of the soil in TSF may be determined as:

$$
\begin{equation*}
\mathrm{q}_{\mathrm{ult}}=0.5 \gamma \mathrm{BC}_{\mathrm{w} 1} \mathrm{~N}_{\gamma \mathrm{m}}+\gamma \mathrm{C}_{\mathrm{w} 2} \mathrm{D}_{\mathrm{f}} \mathrm{~N}_{\mathrm{qm}} \tag{S10.6.3.1.2c-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
D_{f} & =\text { depth of footing from ground level (ft.) } \\
& =6 \mathrm{ft} .
\end{aligned}
$$

$\gamma=$ total, i.e., moist density of sand or gravel (TCF)

$$
=120 / 2,000
$$

$$
=0.06 \mathrm{TCF}
$$

$$
\mathrm{B}=\text { footing width (ft.) }
$$

$$
=\text { smaller of } 11.82 \text { and } 11.09 \mathrm{ft} .
$$

$$
=11.09 \mathrm{ft}
$$

$\mathrm{C}_{\mathrm{w} 1}, \mathrm{C}_{\mathrm{w} 2}=$ coefficients as specified in Table $\mathrm{S} 10.6 .3 .1 .2 \mathrm{c}-1$ as a function of $\mathrm{D}_{\mathrm{w}}$ (dimensionless)

$$
=\text { for dry soil with a large depth, } \mathrm{C}_{\mathrm{w} 1}=\mathrm{C}_{\mathrm{w} 2}=1.0
$$

$$
\begin{aligned}
\mathrm{D}_{\mathrm{w}} & =\text { depth to water surface taken from the ground surface (ft.) } \\
& =\text { assume a large distance relative to the footing dimensions } \\
\mathrm{N}_{\gamma \mathrm{m}}, \mathrm{~N}_{\mathrm{qm}} & =\text { modified bearing capacity factor (dimensionless) }
\end{aligned}
$$

Substituting in Eq. S10.6.3.1.2c-1:

$$
\begin{aligned}
\mathrm{q}_{\mathrm{ult}} & =0.5(0.06)(11.09)(1.0) \mathrm{N}_{\gamma \mathrm{m}}+0.06(1.0)(6) \mathrm{N}_{\mathrm{qm}} \\
& =0.334 \mathrm{~N}_{\gamma \mathrm{m}}+0.36 \mathrm{~N}_{\mathrm{qm}}
\end{aligned}
$$

From Eqs. S10.6.3.1.2c-2 and -3

$$
\begin{align*}
& \mathrm{N}_{\gamma \mathrm{m}}=\mathrm{N}_{\gamma} \mathrm{S}_{\gamma} \mathrm{c}_{\gamma \mathrm{i} \gamma}  \tag{S10.6.3.1.2c-2}\\
& \mathrm{~N}_{\mathrm{qm}}=\mathrm{N}_{\mathrm{q}} \mathrm{~S}_{\mathrm{q}} \mathrm{c}_{\mathrm{q}} \mathrm{i}_{\mathrm{q}} \mathrm{~d}_{\mathrm{q}} \tag{S10.6.3.1.2c-3}
\end{align*}
$$

where:
$\mathrm{N}_{\gamma} \quad=$ bearing capacity factor as specified in Table S10.6.3.1.2c-2 for footings on relatively level ground
$\mathrm{N}_{\mathrm{q}} \quad=$ bearing capacity factor as specified in Table S10.6.3.1.2c-2 for relatively level ground
$\mathrm{S}_{\mathrm{q}}, \mathrm{S}_{\gamma}=$ shape factors specified in Tables S10.6.3.1.2c-3 and -4, respectively
$\mathrm{c}_{\mathrm{q}}, \mathrm{c}_{\gamma}=$ soil compressibility factors specified in Tables S10.6.3.1.2c-5
$\mathrm{i}_{\mathrm{q}}, \mathrm{i}_{\mathrm{y}} \quad=$ load inclination factors specified in Tables S10.6.3.1.2c-7 and -8
$\mathrm{d}_{\mathrm{q}} \quad=$ depth factor specified in Table S10.6.3.1.2c-9

From Table S10.6.3.1.2c-2: $\mathrm{N}_{\gamma}=30$ for $\varphi_{\mathrm{f}}=32$ degrees
From Table $\mathrm{S} 10.6 \cdot 3.1 .2 \mathrm{c}-2$ : $\mathrm{N}_{\mathrm{q}}=23$ for $\varphi_{\mathrm{f}}=32$ degrees

$$
\begin{aligned}
\mathrm{L}^{\prime} / \mathrm{B}^{\prime} & =11.82 / 11.09 \\
& =1.07
\end{aligned}
$$

From Table $\mathrm{S} 10.6 .3 .1 .2 \mathrm{c}-3: \mathrm{S}_{\mathrm{q}}=1.62$ for $\mathrm{L}^{\prime} / \mathrm{B}^{\prime}=1.0$ and $\varphi_{\mathrm{f}}=30$ degrees
From Table S10.6.3.1.2c-4: $\mathrm{S}_{\gamma}=0.6$ for $\mathrm{L}^{\prime} / \mathrm{B}^{\prime}=1.0$ and $\varphi_{\mathrm{f}}=30$ degrees
Soil stress at the footing depth before excavation, $\mathrm{q}=0.06(6)=0.36 \mathrm{TSF}$
For Tables S10.6.3.1.2c-5 and -6, either interpolate between $\mathrm{q}=0.25$ and $\mathrm{q}=0.5$ or, as a conservative approach, use the value corresponding to $\mathrm{q}=0.5$. For this example, the value corresponding to $\mathrm{q}=0.5 \mathrm{TSF}$ is used.

From Table S10.6.3.1.2c-5: $\mathrm{c}_{\mathrm{q}}, \mathrm{c}_{\gamma}=1.0$ for $\mathrm{q}=0.5$ and $\varphi_{\mathrm{f}}=32$ degrees
The maximum factored horizontal load on the bottom of the column from the bent analysis equals 46.0 and 26.0 kips in the transverse and longitudinal directions, respectively. In Table $\mathrm{S} 10.6 .3 .1 .2 \mathrm{c}-7$, it is intended to use the unfactored horizontal and vertical loads. However, due to the small ratio of horizontal to vertical loads, using the factored loads does not affect the results.

Horizontal-to- vertical load ratio:

$$
\begin{aligned}
\mathrm{H} / \mathrm{V} & =44.8 / 1,374 \\
& =0.033 \text { in the transverse direction } \\
\mathrm{H} / \mathrm{V} & =26.0 / 1,374 \\
& =0.019 \text { in the longitudinal direction }
\end{aligned}
$$

Table S10.6.3.1.2-7 lists values for $\mathrm{i}_{\mathrm{q}}$, $\mathrm{i}_{\mathrm{y}}$, that correspond to horizontal to-vertical load ratios of 0.0 and 0.1. Interpolation between the two values is acceptable. A more conservative approach is to use the value corresponding to $\mathrm{H} / \mathrm{V}=0.1$.

From Table S10.6.3.1.2c-7: $\mathrm{i}_{\mathrm{q}}=0.85$ for square footing with $\mathrm{H} / \mathrm{V}=0.1$
From Table S10.6.3.1.2c-7: $\mathrm{i}_{\boldsymbol{\gamma}}=0.77$ for square footing with $\mathrm{H} / \mathrm{V}=0.1$

Table $\mathrm{S} 10.6 .3 .1 .2 \mathrm{c}-9$ lists values for $\mathrm{d}_{\mathrm{q}}$ that correspond to a friction angle, $\varphi_{\mathrm{f}}=32$ degrees and for $D_{f} / B=1.0$. For this example, $\varphi_{f}=30$ degrees and $D_{f} / B=6 / 11.13=0.54$

By extrapolation from Table S10.6.3.1.2c-9, use $\mathrm{d}_{\mathrm{q}}=1.05$
Substituting in Eqs. S10.6.3.1.2c-2 and -3:

$$
\begin{aligned}
\mathrm{N}_{\mathrm{\gamma m}} & =\mathrm{N}_{\gamma} \mathrm{S}_{\gamma} \mathrm{c}_{\gamma} \mathrm{i}_{\gamma} \\
& =30(0.6)(1.0)(0.77) \\
& =13.86
\end{aligned}
$$

(S10.6.3.1.2c-2)

$$
\begin{aligned}
\mathrm{N}_{\mathrm{qm}} & =\mathrm{N}_{\mathrm{q}} \mathrm{~S}_{\mathrm{q}} \mathrm{c}_{\mathrm{q}} \mathrm{i}_{\mathrm{q}} \mathrm{~d}_{\mathrm{q}} \\
& =23(1.62)(1.0)(0.85)(1.05) \\
& =33.3
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\mathrm{q}_{\mathrm{ult}} & =0.333 \mathrm{~N}_{\gamma \mathrm{m}}+0.36 \mathrm{~N}_{\mathrm{qm}} \\
& =0.333(13.86)+0.36(33.3) \\
& =16.6 \mathrm{TSF}
\end{aligned}
$$

## Resistance factor

From Table S10.5.5-1, several resistance factors are listed for cohesionless soil (sand). The selection of a particular resistance factor depends on the method of soil exploration used to determine the soil properties. Assuming that $\varphi$ was estimated from SPT data, the resistance factor $=0.35$

According to S10.6.3.1.1,

$$
\begin{aligned}
q_{\mathrm{R}} & =\varphi \mathrm{q}_{\mathrm{n}}=\varphi \mathrm{qulth} \\
& =0.35(16.6) \\
& =5.81 \mathrm{TSF}
\end{aligned}
$$

Footing load resistance $=\left(\mathrm{q}_{\mathrm{R}}\right)$ (footing effective area)

$$
\begin{aligned}
& =5.81(11.82)(11.09) \\
& =762.0 \text { Tons } \\
& =1,524 \mathrm{k}>1,374 \mathrm{k} \text { applied } \mathbf{O K}
\end{aligned}
$$

The soil load resistance check may be repeated using the same procedures for other load cases.

## APPENDIX A - COMPUTER PROGRAM RESULTS

The results of the hand calculations presented in the example are compared to the results from computer design programs in this appendix. The following programs are included:

QConBridge: This program is a load analysis program developed by Washington State Department of Transportation and is available free of charge from the Department's web site. For continuous structures, this program considers the structure continuous for all loads. This does not match the cond itions for simple-spans made continuous for live loads where the loads applied before the continuity connection is made are actually acting on the simple span structures. This results in differences between the example and QConBridge in the noncomposite dead load effects.

Opis: Opis is a computer program developed by AASHTO as part of the AASHTOWare computer programs suite.

## Section A1 - QConBridge Input

```
Washington State Department of Transporation
Bridge and Structures Office
QConBridge Version 1.0
Code: LRFD First Edition 1994
Span Data
_--------
Span 1 Length: 110.000 ft
Section Properties
Location Ax Iz Mod. E Unit Wgt
    (ft) 
Live Load Distribution Factors
Location Str/Serv Limit States Fatigue Limit State
    (ft) gM gV gM gV
    0.000 0.809 0.984 0.458
Strength Limit State Factors: Ductility 1.00 Redundancy 1.00 Importance 1.00
Service Limit State Factors: Ductility 1.00 Redundancy 1.00 Importance 1.00
Span 2 Length: 110.000 ft
Section Properties
Location Ax Iz Mod. E Unit Wgt
    (ft) (in^2) (in^4) (psi) (pcf)
        0.000 1.764e+03 1.384e+06 4.724e+06 149.999e+00
Live Load Distribution Factors
Location Str/Serv Limit States Fatigue Limit State
    (ft) gM gV gM gV
    0.000 0.796 0.973 0.452 0.652
```

```
Strength Limit State Factors: Ductility 1.00 Redundancy 1.00 Importance 1.00
Service Limit State Factors: Ductility 1.00 Redundancy 1.00 Importance 1.00
Support Data
Support 1 Roller
Support 2 Pinned
Support 3 Roller
```

```
Loading Data
```

Loading Data
-------
-------
DC Loads
DC Loads
Self Weight Generation Disabled
Self Weight Generation Disabled
Traffic Barrier Load Disabled
Traffic Barrier Load Disabled
Span 2 W 2.487e+03 plf from 0.000 ft to 109.999 ft
Span 2 W 2.487e+03 plf from 0.000 ft to 109.999 ft
Span 2 W 0.000e+00 plf from 0.000 ft to 109.999 ft
Span 2 W 0.000e+00 plf from 0.000 ft to 109.999 ft
Span 1 W 2.487e+03 plf from 0.000 ft to 109.999 ft
Span 1 W 2.487e+03 plf from 0.000 ft to 109.999 ft
Span 1 W 0.000e+00 plf from 0.000 ft to 109.999 ft
Span 1 W 0.000e+00 plf from 0.000 ft to 109.999 ft
DW Loads
DW Loads
Utility Load Disabled
Utility Load Disabled
Wearing Surface Load 289.999e+00 plf
Wearing Surface Load 289.999e+00 plf
Live Load Data
Live Load Data
--------------
--------------
Live Load Generation Parameters
Live Load Generation Parameters
Design Tandem : Enabled
Design Tandem : Enabled
Design Truck : 1 rear axle spacing increments
Design Truck : 1 rear axle spacing increments
Dual Truck Train : Headway Spacing varies from 49.213 ft to 49.213 ft using 1 increments
Dual Truck Train : Headway Spacing varies from 49.213 ft to 49.213 ft using 1 increments
Headway Spacing varies from 49.213 ft to 60.000 ft using 1 increments
Headway Spacing varies from 49.213 ft to 60.000 ft using 1 increments
Dual Tandem Train: Disabled
Dual Tandem Train: Disabled
Fatigue Truck : Enabled
Fatigue Truck : Enabled
Live Load Impact
Live Load Impact
Truck Loads 33.000%
Truck Loads 33.000%
Lane Loads 0.000%
Lane Loads 0.000%
Fatigue Truck 15.000%
Fatigue Truck 15.000%
Pedestrian Live Load 0.000e+00 plf
Pedestrian Live Load 0.000e+00 plf
Load Factors
Load Factors
Strength I DC min 0.900 DC max 1.250 DW min 0.650 DW max 1.500 LL 1.750
Strength I DC min 0.900 DC max 1.250 DW min 0.650 DW max 1.500 LL 1.750
Service I DC 1.000 DW 1.000 LL 1.000
Service I DC 1.000 DW 1.000 LL 1.000
Service II DC 1.000 DW 1.000 LL 1.300
Service II DC 1.000 DW 1.000 LL 1.300
Service III DC 1.000 DW 1.000 LL 0.800
Service III DC 1.000 DW 1.000 LL 0.800
Fatigue DC 0.000 DW 0.000 LL 0.750

```
    Fatigue DC 0.000 DW 0.000 LL 0.750
```


## Section A2 - QConBridge Output

Washington State Department of Transporation
Bridge and Structures Office QConBridge Version 1.0

| Analysis Results |  |  |  |
| :---: | :---: | :---: | :---: |
| DC Dead Load |  |  |  |
| Span | Point | Shear(lbs) | Moment (ft-lbs) |
| 1 | 0 | 102.629e+03 | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $75.261 e+03$ | $978.405 e+03$ |
| 1 | 2 | $47.893 e+03$ | $1.655 \mathrm{e}+06$ |
| 1 | 3 | $20.525 e+03$ | $2.032 \mathrm{e}+06$ |
| 1 | 4 | -6.841e+03 | $2.107 e+06$ |
| 1 | 5 | -34.209e+03 | $1.881 \mathrm{e}+06$ |
| 1 | 6 | -61.577e+03 | $1.354 \mathrm{e}+06$ |
| 1 | 7 | -88.945e+03 | $526.833 e+03$ |
| 1 | 8 | $-116.313 e+03$ | -602.095e+03 |
| 1 | 9 | -143.681e+03 | -2.032e+06 |
| 1 | 10 | $-171.047 e+03$ | -3.763e+06 |
| 2 | 0 | $171.049 \mathrm{e}+03$ | $-3.763 e+06$ |
| 2 | 1 | $143.681 e+03$ | -2.032e+06 |
| 2 | 2 | $116.313 e+03$ | -602.095e+03 |
| 2 | 3 | $88.945 \mathrm{e}+03$ | $526.833 e+03$ |
| 2 | 4 | $61.577 e+03$ | $1.354 \mathrm{e}+06$ |
| 2 | 5 | $34.209 \mathrm{e}+03$ | $1.881 \mathrm{e}+06$ |
| 2 | 6 | $6.841 e+03$ | $2.107 e+06$ |
| 2 | 7 | $-20.525 e+03$ | $2.032 \mathrm{e}+06$ |
| 2 | 8 | -47.893e+03 | $1.655 \mathrm{e}+06$ |
| 2 | 9 | -75.261e+03 | $978.405 e+03$ |
| 2 | 10 | -102.627e+03 | $0.000 \mathrm{e}+00$ |


| DW Dead Load |  |  |  |
| ---: | ---: | ---: | ---: |
| Span Point | Shear(lbs) | Moment (ft-lbs) |  |
| 1 | 0 | $11.962 e+03$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $8.772 e+03$ | $114.042 e+03$ |
| 1 | 2 | $5.582 e+03$ | $192.994 e+03$ |
| 1 | 3 | $2.392 e+03$ | $236.857 e+03$ |
| 1 | 4 | $-797.499 e+00$ | $245.629 e+03$ |
| 1 | 5 | $-3.987 e+03$ | $219.312 e+03$ |
| 1 | 6 | $-7.177 e+03$ | $157.904 e+03$ |
| 1 | 7 | $-10.367 e+03$ | $61.407 e+03$ |
| 1 | 8 | $-13.557 e+03$ | $-70.179 e+03$ |
| 1 | 9 | $-16.747 e+03$ | $-236.857 e+03$ |
| 1 | 10 | $-19.937 e+03$ | $-438.624 e+03$ |
| 2 | 0 | $19.937 e+03$ | $-438.624 e+03$ |
| 2 | 1 | $16.747 e+03$ | $-236.857 e+03$ |
| 2 | 2 | $13.557 e+03$ | $-70.179 e+03$ |
| 2 | 3 | $10.367 e+03$ | $61.407 e+03$ |
| 2 | 4 | $7.177 e+03$ | $157.904 e+03$ |
| 2 | 5 | $3.987 e+03$ | $219.312 e+03$ |
| 2 | 6 | $797.499 e+00$ | $245.629 e+03$ |
| 2 | 7 | $-2.392 e+03$ | $236.857 e+03$ |
| 2 | 8 | $-5.582 e+03$ | $192.994 e+03$ |
| 2 | 9 | $-8.772 e+03$ | $114.042 e+03$ |
| 2 | 10 | $-11.962 e+03$ | $0.000 e+00$ |


| Live Load Envelopes (Per Lane) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Span | Point | Min Shear (lbs) | Max Shear(lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | -13.341e+03 | $117.656 \mathrm{e}+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | -13.341e+03 | $102.204 \mathrm{e}+03$ | -146.752e+03 | $1.124 \mathrm{e}+06$ |
| 1 | 2 | $-13.840 \mathrm{e}+03$ | $84.016 \mathrm{e}+03$ | -293.504e+03 | $1.914 \mathrm{e}+06$ |
| 1 | 3 | $-34.021 e+03$ | $65.643 e+03$ | -440.256e+03 | $2.388 e+06$ |
| 1 | 4 | $-34.558 \mathrm{e}+03$ | $51.974 \mathrm{e}+03$ | -587.009e+03 | $2.597 e+06$ |
| 1 | 5 | $-63.460 e+03$ | $37.680 \mathrm{e}+03$ | $-733.761 e+03$ | $2.550 \mathrm{e}+06$ |
| 1 | 6 | $-78.483 e+03$ | $26.024 e+03$ | -880.513e+03 | $2.276 e+06$ |
| 1 | 7 | -93.440e+03 | $16.112 e+03$ | $-1.027 e+06$ | $1.765 e+06$ |
| 1 | 8 | -101.698e+03 | $8.468 \mathrm{e}+03$ | -1.174e+06 | $1.053 \mathrm{e}+06$ |
| 1 | 9 | -110.990e+03 | $3.304 e+03$ | -1.469e+06 | $374.566 e+03$ |
| 1 | 10 | $-135.743 e+03$ | $0.000 \mathrm{e}+00$ | -2.592e+06 | $0.000 \mathrm{e}+00$ |
| 2 | 0 | $0.000 \mathrm{e}+00$ | $132.939 \mathrm{e}+03$ | -2.592e+06 | $0.000 \mathrm{e}+00$ |
| 2 | 1 | $0.000 \mathrm{e}+00$ | 125.632e+03 | -1.469e+06 | $374.568 e+03$ |
| 2 | 2 | -3.304e+03 | $110.990 \mathrm{e}+03$ | -1.174e+06 | $1.053 e+06$ |
| 2 | 3 | $-16.112 \mathrm{e}+03$ | $93.440 \mathrm{e}+03$ | $-1.027 e+06$ | $1.765 e+06$ |
| 2 | 4 | $-16.284 \mathrm{e}+03$ | $80.355 e+03$ | -880.513e+03 | $2.276 e+06$ |
| 2 | 5 | $-37.680 e+03$ | $63.460 \mathrm{e}+03$ | $-733.761 e+03$ | $2.550 \mathrm{e}+06$ |
| 2 | 6 | $-50.919 \mathrm{e}+03$ | $48.575 \mathrm{e}+03$ | -587.008e+03 | $2.597 e+06$ |
| 2 | 7 | $-65.643 e+03$ | $34.021 e+03$ | -440.256e+03 | $2.388 e+06$ |
| 2 | 8 | $-67.233 e+03$ | $21.193 e+03$ | -293.504e+03 | $1.914 \mathrm{e}+06$ |
| 2 | 9 | -84.016e+03 | $13.840 \mathrm{e}+03$ | -146.752e+03 | $1.124 \mathrm{e}+06$ |
| 2 | 10 | $-117.656 \mathrm{e}+03$ | $13.341 e+03$ | $0.000 e+00$ | $0.000 e+00$ |
| Design Tandem + Lane Envelopes (Per Lane) |  |  |  |  |  |
| Span | Point | Min Shear (lbs) | Max Shear (lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | -10.630e+03 | $95.017 e+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $-10.630 \mathrm{e}+03$ | $83.324 e+03$ | -116.935e+03 | $916.565 e+03$ |
| 1 | 2 | $-11.579 \mathrm{e}+03$ | $68.741 e+03$ | -233.871e+03 | $1.578 \mathrm{e}+06$ |
| 1 | 3 | $-31.053 e+03$ | $53.774 \mathrm{e}+03$ | -350.806e+03 | $1.992 \mathrm{e}+06$ |
| 1 | 4 | $-31.590 \mathrm{e}+03$ | $43.263 e+03$ | -467.741e+03 | $2.170 e+06$ |
| 1 | 5 | $-52.774 e+03$ | $31.844 \mathrm{e}+03$ | -584.677e+03 | $2.136 e+06$ |
| 1 | 6 | -64.109e+03 | $22.735 e+03$ | -701.612e+03 | $1.908 \mathrm{e}+06$ |
| 1 | 7 | $-75.554 \mathrm{e}+03$ | $14.885 \mathrm{e}+03$ | -818.548e+03 | $1.497 e+06$ |
| 1 | 8 | $-82.265 e+03$ | $8.468 e+03$ | $-935.483 e+03$ | $929.199 \mathrm{e}+03$ |
| 1 | 9 | $-89.847 e+03$ | $3.304 e+03$ | $-1.184 e+06$ | $374.566 e+03$ |
| 1 | 10 | $-108.838 \mathrm{e}+03$ | $0.000 e+00$ | -1.646e+06 | $0.000 \mathrm{e}+00$ |
| 2 | 0 | $0.000 \mathrm{e}+00$ | $106.420 \mathrm{e}+03$ | -1.646e+06 | $0.000 \mathrm{e}+00$ |
| 2 | 1 | $0.000 \mathrm{e}+00$ | $101.408 e+03$ | $-1.184 e+06$ | $374.568 e+03$ |
| 2 | 2 | $-3.304 e+03$ | $89.847 e+03$ | $-935.483 e+03$ | $929.201 e+03$ |
| 2 | 3 | $-14.885 e+03$ | $75.554 \mathrm{e}+03$ | -818.548e+03 | $1.497 e+06$ |
| 2 | 4 | $-15.057 e+03$ | $65.981 e+03$ | -701.612e+03 | $1.908 \mathrm{e}+06$ |
| 2 | 5 | -31.844e+03 | $52.774 \mathrm{e}+03$ | -584.677e+03 | $2.136 e+06$ |
| 2 | 6 | $-42.208 e+03$ | $41.707 e+03$ | -467.741e+03 | $2.170 e+06$ |
| 2 | 7 | $-53.774 e+03$ | $31.053 e+03$ | -350.806e+03 | $1.992 \mathrm{e}+06$ |
| 2 | 8 | $-55.364 e+03$ | $21.193 e+03$ | -233.870e+03 | $1.578 e+06$ |
| 2 | 9 | -68.741e+03 | $11.578 \mathrm{e}+03$ | $-116.935 e+03$ | $916.562 e+03$ |
| 2 | 10 | -95.017e+03 | $10.630 \mathrm{e}+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |


| Design Truck |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Span Point | Min Shear (lbs) | Max | Shear (lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | $-13.341 e+03$ | $117.656 e+03$ | $0.000 e+00$ | $0.000 e+00$ |
| 1 | 1 | $-13.341 e+03$ | $102.204 e+03$ | $-146.752 e+03$ | $1.124 e+06$ |
| 1 | 2 | $-13.840 e+03$ | $84.016 e+03$ | $-293.504 e+03$ | $1.914 e+06$ |
| 1 | 3 | $-34.021 e+03$ | $65.643 e+03$ | $-440.256 e+03$ | $2.388 e+06$ |
| 1 | 4 | $-34.558 e+03$ | $51.974 e+03$ | $-587.009 e+03$ | $2.597 e+06$ |
| 1 | 5 | $-63.460 e+03$ | $37.680 e+03$ | $-733.761 e+03$ | $2.550 e+06$ |
| 1 | 6 | $-78.483 e+03$ | $26.024 e+03$ | $-880.513 e+03$ | $2.276 e+06$ |
| 1 | 7 | $-93.440 e+03$ | $16.112 e+03$ | $-1.027 e+06$ | $1.765 e+06$ |
| 1 | 8 | $-101.698 e+03$ | $8.212 e+03$ | $-1.174 e+06$ | $1.053 e+06$ |
| 1 | 9 | $-110.990 e+03$ | $2.695 e+03$ | $-1.452 e+06$ | $329.425 e+03$ |
| 1 | 10 | $-135.743 e+03$ | $0.000 e+00$ | $-1.945 e+06$ | $0.000 e+00$ |
| 2 | 0 | $0.000 e+00$ | $132.939 e+03$ | $-1.945 e+06$ | $0.000 e+00$ |
| 2 | 1 | $0.000 e+00$ | $125.632 e+03$ | $-1.452 e+06$ | $329.427 e+03$ |
| 2 | 2 | $-2.695 e+03$ | $110.990 e+03$ | $-1.174 e+06$ | $1.053 e+06$ |
| 2 | 3 | $-16.112 e+03$ | $93.440 e+03$ | $-1.027 e+06$ | $1.765 e+06$ |
| 2 | 4 | $-16.284 e+03$ | $80.355 e+03$ | $-880.513 e+03$ | $2.276 e+06$ |
| 2 | 5 | $-37.680 e+03$ | $63.460 e+03$ | $-733.761 e+03$ | $2.550 e+06$ |
| 2 | 6 | $-50.919 e+03$ | $48.575 e+03$ | $-587.008 e+03$ | $2.597 e+06$ |
| 2 | 7 | $-65.643 e+03$ | $34.021 e+03$ | $-440.256 e+03$ | $2.388 e+06$ |
| 2 | 8 | $-67.233 e+03$ | $20.963 e+03$ | $-293.504 e+03$ | $1.914 e+06$ |
| 2 | 9 | $-84.016 e+03$ | $13.840 e+03$ | $-146.752 e+03$ | $1.124 e+06$ |
| 2 | 10 | $-117.656 e+03$ | $13.341 e+03$ | $0.000 e+00$ | $0.000 e+00$ |


| Span | Point | Min Shear (lbs) | Max Shear(lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 2 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 e+00$ |
| 1 | 3 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 4 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 5 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 6 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 7 | $0.000 e+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 8 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $-1.066 e+06$ | $0.000 \mathrm{e}+00$ |
| 1 | 9 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | -1.469e+06 | $0.000 \mathrm{e}+00$ |
| 1 | 10 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | -2.592e+06 | $0.000 \mathrm{e}+00$ |
| 2 | 0 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | -2.592e+06 | $0.000 e+00$ |
| 2 | 1 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | -1.469e+06 | $0.000 \mathrm{e}+00$ |
| 2 | 2 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $-1.066 e+06$ | $0.000 \mathrm{e}+00$ |
| 2 | 3 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 4 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 e+00$ |
| 2 | 5 | $0.000 e+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 6 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 e+00$ | $0.000 e+00$ |
| 2 | 7 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 8 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 9 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 e+00$ |
| 2 | 10 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |


| Dual Tandem Train + Lane Envelopes (Per Lane) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Span | Point | Min Shear (lbs) | Max Shear(lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 2 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 e+00$ |
| 1 | 3 | $0.000 e+00$ | $0.000 e+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 4 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 5 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 6 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 7 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 e+00$ |
| 1 | 8 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 9 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 10 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 0 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 1 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 2 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 3 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 4 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 5 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 6 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 7 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 8 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 e+00$ |
| 2 | 9 | $0.000 \mathrm{e}+00$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 2 | 10 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| Fatigue Truck Envelopes (Per Lane) |  |  |  |  |  |
| Span | Point | Min Shear (lbs) | Max Shear(lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | -7.232e+03 | $67.296 e+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $-7.232 e+03$ | $57.232 e+03$ | $-79.555 e+03$ | $629.555 e+03$ |
| 1 | 2 | -7.232e+03 | $47.499 \mathrm{e}+03$ | -159.110e+03 | $1.044 \mathrm{e}+06$ |
| 1 | 3 | $-15.733 e+03$ | $38.223 e+03$ | $-238.665 e+03$ | $1.304 \mathrm{e}+06$ |
| 1 | 4 | $-15.733 \mathrm{e}+03$ | $29.529 \mathrm{e}+03$ | -318.220e+03 | $1.384 e+06$ |
| 1 | 5 | $-34.143 e+03$ | $21.514 \mathrm{e}+03$ | -397.775e+03 | $1.341 e+06$ |
| 1 | 6 | $-43.545 e+03$ | $14.396 \mathrm{e}+03$ | -477.330e+03 | $1.229 \mathrm{e}+06$ |
| 1 | 7 | $-52.395 e+03$ | $8.877 e+03$ | $-556.885 e+03$ | $966.113 e+03$ |
| 1 | 8 | $-56.304 e+03$ | $5.169 \mathrm{e}+03$ | $-636.440 e+03$ | $581.739 \mathrm{e}+03$ |
| 1 | 9 | $-60.568 e+03$ | $2.146 e+03$ | -715.995e+03 | $219.754 e+03$ |
| 1 | 10 | $-74.413 e+03$ | $0.000 \mathrm{e}+00$ | -795.550e+03 | $0.000 e+00$ |
| 2 | 0 | $0.000 e+00$ | $74.208 \mathrm{e}+03$ | $-795.550 e+03$ | $0.000 \mathrm{e}+00$ |
| 2 | 1 | $0.000 \mathrm{e}+00$ | $67.938 \mathrm{e}+03$ | -715.995e+03 | $219.754 \mathrm{e}+03$ |
| 2 | 2 | $-2.146 e+03$ | $60.568 e+03$ | -636.440e+03 | $581.740 \mathrm{e}+03$ |
| 2 | 3 | -8.877e+03 | $52.395 e+03$ | $-556.885 e+03$ | $966.113 e+03$ |
| 2 | 4 | -8.877e+03 | $43.545 e+03$ | -477.330e+03 | $1.229 \mathrm{e}+06$ |
| 2 | 5 | $-21.514 e+03$ | $34.143 e+03$ | -397.775e+03 | $1.341 e+06$ |
| 2 | 6 | $-29.529 \mathrm{e}+03$ | $24.315 e+03$ | -318.220e+03 | $1.384 e+06$ |
| 2 | 7 | $-38.223 e+03$ | $15.733 e+03$ | $-238.665 e+03$ | $1.304 \mathrm{e}+06$ |
| 2 | 8 | $-38.223 e+03$ | $10.106 \mathrm{e}+03$ | $-159.110 e+03$ | $1.044 \mathrm{e}+06$ |
| 2 | 9 | -47.499e+03 | $7.232 \mathrm{e}+03$ | $-79.555 e+03$ | $629.555 e+03$ |
| 2 | 10 | -67.296e+03 | $7.232 \mathrm{e}+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |



| Service I Limit State Envelopes |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: |
| Span Point | Min Shear (lbs) | Max | Shear (lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | $101.464 e+03$ | $230.365 e+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $70.906 e+03$ | $184.603 e+03$ | $973.725 e+03$ | $2.001 e+06$ |
| 1 | 2 | $39.857 e+03$ | $136.148 e+03$ | $1.611 e+06$ | $3.397 e+06$ |
| 1 | 3 | $-10.558 e+03$ | $87.511 e+03$ | $1.912 e+06$ | $4.200 e+06$ |
| 1 | 4 | $-41.645 e+03$ | $43.503 e+03$ | $1.878 e+06$ | $4.454 e+06$ |
| 1 | 5 | $-100.642 e+03$ | $-1.119 e+03$ | $1.507 e+06$ | $4.164 e+06$ |
| 1 | 6 | $-145.983 e+03$ | $-43.147 e+03$ | $800.284 e+03$ | $3.354 e+06$ |
| 1 | 7 | $-191.259 e+03$ | $-83.458 e+03$ | $-242.817 e+03$ | $2.016 e+06$ |
| 1 | 8 | $-229.942 e+03$ | $-121.538 e+03$ | $-1.622 e+06$ | $180.339 e+03$ |
| 1 | 9 | $-269.644 e+03$ | $-157.177 e+03$ | $-3.457 e+06$ | $-1.965 e+06$ |
| 1 | 10 | $-324.556 e+03$ | $-190.984 e+03$ | $-6.298 e+06$ | $-4.201 e+06$ |
| 2 | 0 | $190.987 e+03$ | $321.799 e+03$ | $-6.298 e+06$ | $-4.201 e+06$ |
| 2 | 1 | $160.429 e+03$ | $284.051 e+03$ | $-3.457 e+06$ | $-1.965 e+06$ |
| 2 | 2 | $126.619 e+03$ | $239.086 e+03$ | $-1.622 e+06$ | $180.340 e+03$ |
| 2 | 3 | $83.458 e+03$ | $191.258 e+03$ | $-242.816 e+03$ | $2.016 e+06$ |
| 2 | 4 | $52.731 e+03$ | $147.825 e+03$ | $800.284 e+03$ | $3.354 e+06$ |
| 2 | 5 | $1.119 e+03$ | $100.642 e+03$ | $1.507 e+06$ | $4.164 e+06$ |
| 2 | 6 | $-42.465 e+03$ | $55.437 e+03$ | $1.878 e+06$ | $4.454 e+06$ |
| 2 | 7 | $-87.511 e+03$ | $10.558 e+03$ | $1.912 e+06$ | $4.200 e+06$ |
| 2 | 8 | $-119.634 e+03$ | $-32.622 e+03$ | $1.611 e+06$ | $3.397 e+06$ |
| 2 | 9 | $-166.706 e+03$ | $-70.415 e+03$ | $973.725 e+03$ | $2.001 e+06$ |
| 2 | 10 | $-230.363 e+03$ | $-101.462 e+03$ | $0.000 e+00$ | $0.000 e+00$ |


| Service II Limit State Envelopes |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Span Point | Min | Shear (lbs) | Max | Shear (lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | $97.526 e+03$ | $265.098 e+03$ | $0.000 e+00$ | $0.000 \mathrm{e}+00$ |  |
| 1 | 1 | $66.968 e+03$ | $214.774 e+03$ | $938.108 e+03$ | $2.274 e+06$ |  |
| 1 | 2 | $35.771 e+03$ | $160.950 e+03$ | $1.540 e+06$ | $3.862 e+06$ |  |
| 1 | 3 | $-20.601 e+03$ | $106.889 e+03$ | $1.805 e+06$ | $4.780 e+06$ |  |
| 1 | 4 | $-51.846 e+03$ | $58.846 e+03$ | $1.735 e+06$ | $5.084 e+06$ |  |
| 1 | 5 | $-119.376 e+03$ | $10.003 e+03$ | $1.329 e+06$ | $4.782 e+06$ |  |
| 1 | 6 | $-169.151 e+03$ | $-35.465 e+03$ | $586.583 e+03$ | $3.907 e+06$ |  |
| 1 | 7 | $-218.842 e+03$ | $-78.702 e+03$ | $-492.134 e+03$ | $2.445 e+06$ |  |
| 1 | 8 | $-259.963 e+03$ | $-119.038 e+03$ | $-1.906 e+06$ | $436.123 e+03$ |  |
| 1 | 9 | $-302.409 e+03$ | $-156.201 e+03$ | $-3.814 e+06$ | $-1.874 e+06$ |  |
| 1 | 10 | $-364.627 e+03$ | $-190.984 e+03$ | $-6.927 e+06$ | $-4.201 e+06$ |  |
| 2 | 0 | $190.987 e+03$ | $361.042 e+03$ | $-6.927 e+06$ | $-4.201 e+06$ |  |
| 2 | 1 | $160.429 e+03$ | $321.138 e+03$ | $-3.814 e+06$ | $-1.874 e+06$ |  |
| 2 | 2 | $125.643 e+03$ | $271.851 e+03$ | $-1.906 e+06$ | $436.125 e+03$ |  |
| 2 | 3 | $78.702 e+03$ | $218.842 e+03$ | $-492.134 e+03$ | $2.445 e+06$ |  |
| 2 | 4 | $47.924 e+03$ | $171.546 e+03$ | $586.583 e+03$ | $3.907 e+06$ |  |
| 2 | 5 | $-10.003 e+03$ | $119.375 e+03$ | $1.329 e+06$ | $4.782 e+06$ |  |
| 2 | 6 | $-57.496 e+03$ | $69.776 e+03$ | $1.735 e+06$ | $5.084 e+06$ |  |
| 2 | 7 | $-106.889 e+03$ | $20.601 e+03$ | $1.805 e+06$ | $4.780 e+06$ |  |
| 2 | 8 | $-139.481 e+03$ | $-26.366 e+03$ | $1.540 e+06$ | $3.862 e+06$ |  |
| 2 | 9 | $-191.508 e+03$ | $-66.329 e+03$ | $938.108 e+03$ | $2.274 e+06$ |  |
| 2 | 10 | $-265.095 e+03$ | $-97.524 e+03$ | $0.000 e+00$ | $0.000 e+00$ |  |


| Span | Point | Min Shear (lbs) | Max Shear(lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | $104.090 \mathrm{e}+03$ | 207.211e+03 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | $73.532 e+03$ | $164.489 \mathrm{e}+03$ | $997.469 \mathrm{e}+03$ | $1.820 \mathrm{e}+06$ |
| 1 | 2 | $42.581 e+03$ | $119.614 \mathrm{e}+03$ | $1.658 \mathrm{e}+06$ | $3.087 e+06$ |
| 1 | 3 | $-3.863 e+03$ | $74.593 e+03$ | $1.983 e+06$ | $3.814 e+06$ |
| 1 | 4 | $-34.844 e+03$ | $33.274 \mathrm{e}+03$ | 1.973e+06 | $4.033 e+06$ |
| 1 | 5 | -88.153e+03 | -8.535e+03 | $1.625 e+06$ | $3.751 e+06$ |
| 1 | 6 | -130.537e+03 | -48.269e+03 | $942.751 e+03$ | $2.986 e+06$ |
| 1 | 7 | -172.869e+03 | -86.629e+03 | -76.605e+03 | $1.730 \mathrm{e}+06$ |
| 1 | 8 | -209.928e+03 | -123.204e+03 | $-1.432 e+06$ | $9.816 e+03$ |
| 1 | 9 | -247.801e+03 | -157.827e+03 | -3.219e+06 | -2.026e+06 |
| 1 | 10 | -297.841e+03 | $-190.984 e+03$ | $-5.879 e+06$ | -4.201e+06 |
| 2 | 0 | $190.987 e+03$ | $295.636 \mathrm{e}+03$ | $-5.879 e+06$ | -4.201e+06 |
| 2 | 1 | $160.429 e+03$ | $259.327 e+03$ | -3.219e+06 | $-2.026 e+06$ |
| 2 | 2 | $127.269 \mathrm{e}+03$ | $217.243 e+03$ | $-1.432 e+06$ | $9.817 e+03$ |
| 2 | 3 | $86.629 \mathrm{e}+03$ | $172.869 \mathrm{e}+03$ | $-76.605 e+03$ | $1.730 \mathrm{e}+06$ |
| 2 | 4 | $55.936 e+03$ | $132.011 e+03$ | $942.751 e+03$ | $2.986 e+06$ |
| 2 | 5 | $8.535 e+03$ | $88.153 e+03$ | $1.625 e+06$ | $3.751 e+06$ |
| 2 | 6 | $-32.444 e+03$ | $45.877 e+03$ | $1.973 e+06$ | $4.033 e+06$ |
| 2 | 7 | -74.593e+03 | $3.862 e+03$ | $1.983 e+06$ | $3.814 \mathrm{e}+06$ |
| 2 | 8 | -106.402e+03 | $-36.793 e+03$ | $1.658 e+06$ | $3.087 e+06$ |
| 2 | 9 | -150.172e+03 | -73.139e+03 | $997.469 e+03$ | $1.820 e+06$ |
| 2 | 10 | -207.208e+03 | -104.087e+03 | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |

## Appendix A

Prestressed Concrete Bridge Design Example

| Fatigue Limit State Envelopes |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Span | Point | Min Shear (lbs) | Max | Shear (lbs) Min | Moment (ft-lbs) Max | Moment (ft-lbs) |
| 1 | 0 | -3.531e+03 |  | $32.857 e+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |
| 1 | 1 | -3.531e+03 |  | $27.943 e+03$ | $-27.327 e+03$ | $216.252 e+03$ |
| 1 | 2 | -3.531e+03 |  | $23.191 e+03$ | -54.654e+03 | $358.952 e+03$ |
| 1 | 3 | -7.681e+03 |  | 18.662e+03 | -81.981e+03 | $448.201 e+03$ |
| 1 | 4 | -7.681e+03 |  | $14.417 e+03$ | $-109.308 e+03$ | $475.633 e+03$ |
| 1 | 5 | $-16.670 \mathrm{e}+03$ |  | $10.504 \mathrm{e}+03$ | -136.635e+03 | $460.659 \mathrm{e}+03$ |
| 1 | 6 | -21.261e+03 |  | $7.029 \mathrm{e}+03$ | -163.962e+03 | $422.252 e+03$ |
| 1 | 7 | -25.582e+03 |  | $4.334 \mathrm{e}+03$ | -191.290e+03 | $331.859 \mathrm{e}+03$ |
| 1 | 8 | -27.490e+03 |  | $2.524 e+03$ | -218.617e+03 | 199.827e+03 |
| 1 | 9 | -29.572e+03 |  | $1.047 e+03$ | -245.944e+03 | $75.485 e+03$ |
| 1 | 10 | $-36.332 e+03$ |  | $0.000 \mathrm{e}+00$ | -273.271e+03 | $0.000 \mathrm{e}+00$ |
| 2 | 0 | $0.000 \mathrm{e}+00$ |  | $36.232 \mathrm{e}+03$ | -273.271e+03 | $0.000 \mathrm{e}+00$ |
| 2 | 1 | $0.000 \mathrm{e}+00$ |  | $33.170 \mathrm{e}+03$ | -245.944e+03 | $75.485 e+03$ |
| 2 | 2 | -1.047e+03 |  | $29.572 \mathrm{e}+03$ | -218.617e+03 | $199.827 e+03$ |
| 2 | 3 | -4.334e+03 |  | $25.582 \mathrm{e}+03$ | -191.290e+03 | $331.859 \mathrm{e}+03$ |
| 2 | 4 | -4.334e+03 |  | $21.261 e+03$ | -163.962e+03 | $422.252 e+03$ |
| 2 | 5 | $-10.504 e+03$ |  | $16.670 \mathrm{e}+03$ | $-136.635 e+03$ | $460.659 \mathrm{e}+03$ |
| 2 | 6 | -14.417e+03 |  | $11.872 \mathrm{e}+03$ | $-109.308 e+03$ | $475.633 e+03$ |
| 2 | 7 | $-18.662 e+03$ |  | $7.681 e+03$ | -81.981e+03 | $448.201 e+03$ |
| 2 | 8 | -18.662e+03 |  | $4.934 e+03$ | -54.654e+03 | $358.952 e+03$ |
| 2 | 9 | -23.191e+03 |  | $3.531 e+03$ | $-27.327 e+03$ | $216.252 e+03$ |
| 2 | 10 | -32.857e+03 |  | $3.531 e+03$ | $0.000 \mathrm{e}+00$ | $0.000 \mathrm{e}+00$ |

## Section A3 - Opis Input

The computer program Opis is used to analyze the prestressed concrete example problem. This program is part of the AASHTOware software suite. The input data for Opis is provided on the following pages.

```
4-1.1
    ANALYSIS
    B, 2, REV, S
    1. Analysis Model : B
    2. Loading Sequence : 2
    3. Analysis Type : REV
    4. Element : S
4-1.2 POINT-OF-INTEREST T, ON, ON
    1. Point of Interest Control : T
    2. Specification Checks : ON
    3. Load Factoring/Combination : ON
4-3.1
4-3.2
3-1.1
4-3.3
4-3.5
5-1.1
5-4.1
5-4.2
5-4.2
5-4.2
OUTPUT-LIMIT-STATE ST, 3, ON, ON
    1. Limit State : ST
    2. Limit State Level : 3
```




```
        3. Top Flange Thickness : 5.000
        4. Top Web Thickness : 8.000
        5. Bottom Web Thickness : 8.000
        6. Bottom Flange Width : 28.000
        7. Bottom Flange Thickness : 8.000
8-2.7
    CONC-FILLETS
                            2, 3.000, 0.000, 4.000, 4.000,
            10.000, 0.000, 0.000, 0.000
            1. Cross Section Number : 2
            2. Top Tapers Height : 3.000
            3. Top Tapers Distance : 0.000
            4. Top Fillets Height : 4.000
            5. Top Fillets Width : 4.000
            6. Bottom Tapers Height : 10.000
            7. Bottom Tapers Distance : 0.000
            8. Bottom Fillets Height : 0.000
            9. Bottom Fillets Width : 0.000
10-2.1 COMPOSITE-SLAB 2, 111.0000, 7.5000, 0.0000
            1. Cross Section Number : 2
            2. Effective Width : 111.000
            3. Effective Thickness : 7.500
            4. Gap Distance : 0.000
10-2.2 COMPOSITE-REBAR 2, B, 12.000, 6, 2.0000
            1. Cross Section Number : 2
            2. Row Designation : B
            3. Number of Reinforcing Bars : 12.000
            4. Bar Size
                            6
                            5. Distance to Bar Center : 2.000
10-2.2
COMPOSITE-REBAR 2, B, 21.000, 6, 3.6250
    1. Cross Section Number : 2
    2. Row Designation : B
    3. Number of Reinforcing Bars : 21.000
    4. Bar Size : 6
    5. Distance to Bar Center : 3.625
3-1.1
3-1.1
8-2.4
8-2.7
8-2.8 CONC-REBAR 3, 1, 5.000, 5, 4.0000
10-2.1
COMMENT Cross Section 3
COMMENT Beam Name: AASHTO TYPE VI
CONC-I-SECTION 3, 42.00, 5.00, 8.00, 8.00, 28.00, 8.00
    1. Cross Section Number : 3
    2. Top Flange Width : 42.000
    3. Top Flange Thickness : 5.000
    4. Top Web Thickness : 8.000
    5. Bottom Web Thickness : 8.000
    6. Bottom Flange Width : 28.000
    7. Bottom Flange Thickness : 8.000
CONC-FILLETS 3, 3.000, 0.000, 4.000, 4.000, &
                        10.000, 0.000, 0.000, 0.000
            1. Cross Section Number : 3
            2. Top Tapers Height : 3.000
            3. Top Tapers Distance : 0.000
            4. Top Fillets Height : 4.000
            5. Top Fillets Width : 4.000
            6. Bottom Tapers Height : 10.000
            7. Bottom Tapers Distance : 0.000
            8. Bottom Fillets Height : 0.000
            9. Bottom Fillets Width : 0.000
    1. Cross Section Number : 3
    2. Row Number : 1
    3. Number of Reinforcing Bars : 5.000
    4. Bar Size : 5
    5. Distance to Bar Center : 4.000
COMPOSITE-SLAB 3, 111.0000, 7.5000, 0.0000
    1. Cross Section Number : 3
    2. Effective Width : 111.000
```







|  | 1. Span Number | : 2 |
| :---: | :---: | :---: |
|  | 2. Stirrup Number | : 2 |
|  | 3. Stirrup Spacing | 3.000 |
|  | 4. Start Distance | 13.560 |
|  | 5. Range | 3.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 10, 6.0000, 1 | 16.5600, 90.0000 |
|  | 1. Span Number | : 2 |
|  | 2. Stirrup Number | 10 |
|  | 3. Stirrup Spacing | 6.000 |
|  | 4. Start Distance | 16.560 |
|  | 5. Range | 90.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 5, 16.0000, <br> 1. Span Number | $\begin{aligned} & 106.5600,32.0000 \\ & \quad: \quad 2 \end{aligned}$ |
|  | 2. Stirrup Number | 5 |
|  | 3. Stirrup Spacing | 16.000 |
|  | 4. Start Distance | 106.560 |
|  | 5. Range | 32.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 1, 18.0400, 138 | 138.5600, 18.0400 |
|  | 1. Span Number | 2 |
|  | 2. Stirrup Number | 1 |
|  | 3. Stirrup Spacing | 18.040 |
|  | 4. Start Distance | 138.560 |
|  | 5. Range | 18.040 |
| 3-1.1 | COMMENT Stirrup Group 11 | 1: \#4 Vert Shear R |
| 8-4.2 | STIRRUP-GROUP 11, $0.4000,90.0$ | 000, 250.000 |
|  | 1. Stirrup Number | 11 |
|  | 2. Stirrup Area | 0.400 |
|  | 3. Stirrup Angle | 90.000 |
|  | 4. \% Stir. Area for Horz Shear | 250.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 11, 18.0000, | 156.6000, 54.0000 |
|  | 1. Span Number | : 2 |
|  | 2. Stirrup Number | 11 |
|  | 3. Stirrup Spacing | 18.000 |
|  | 4. Start Distance | 156.600 |
|  | 5. Range | 54.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 7, 20.0000, 2 | 210.6000, 140.0000 |
|  | 1. Span Number | 2 |
|  | 2. Stirrup Number | 7 |
|  | 3. Stirrup Spacing | 20.000 |
|  | 4. Start Distance | 210.600 |
|  | 5. Range | 140.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 8, 24.0000, 3 | 350.6000, 648.0001 |
|  | 1. Span Number | : 2 |
|  | 2. Stirrup Number | 8 |
|  | 3. Stirrup Spacing | 24.000 |
|  | 4. Start Distance | 350.600 |
|  | 5. Range | : 648.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 11, 19.0000, | 998.6001, 56.9999 |
|  | 1. Span Number | : 2 |
|  | 2. Stirrup Number | 11 |
|  | 3. Stirrup Spacing | 19.000 |
|  | 4. Start Distance | 998.600 |
|  | 5. Range | 57.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 7, 11.0000, 1 | 1055.6000, 77.0000 |
|  | 1. Span Number | : 2 |
|  | 2. Stirrup Number | 7 |
|  | 3. Stirrup Spacing | 11.000 |
|  | 4. Start Distance | 1055.600 |
|  | 5. Range | 77.000 |
| 8-4.3 | STIRRUP-SCHEDULE 2, 9, 7.0000, 11 | 132.6000, 84.0000 |
|  | 1. Span Number | : 2 |
|  | 2. Stirrup Number | : 9 |
|  | 3. Stirrup Spacing | $: \quad 7.000$ |



| 9-7.4 | SHEAR-FRICTION-COEFF $0.100,1.000$, <br> 2. Friction Factor <br> . <br> 1.000 <br> 3. Interface Width <br> : |
| :---: | :---: |
| 3-1.1 | COMMENT Point of Interest: (100.1591) = Span 1-21.0000 |
| 3-1.1 | COMMENT The r/h data on the following command are BRASS defaults. |
| 3-1.1 | COMMENT This data is not currently available in Virtis/Opis. |
| 10-3.1 | COMPOSITE-FATIGUE 100.1591, $0.300,0.300$ |
|  | 1. Point of Interest : 100.1591 |
|  | 2. r/h (Bottom Rebar) : 0.300 |
|  | 3. r/h (Top Rebar) : 0.300 |
| 9-7.3 | PRESTRESS-FATIGUE 100.1591, 18.0000 |
|  | 1. Point of Interest : 100.1591 |
|  | 2. Stress Range : 18.000 |
| 5-2.1 | OUTPUT-INTERMEDIATE 100.1591, ON, ON |
|  | 1. Point of Interest : 100.1591 |
|  | 2. Specification Checks : ON |
|  | 3. Load Factoring/Combination : ON |
| 3-1.1 | COMMENT Point of Interest: (100.6364) = Span 1-84.0000 |
| 3-1.1 | COMMENT The r/h data on the following command are BRASS defaults. |
| 3-1.1 | COMMENT This data is not currently available in Virtis/opis. |
| 10-3.1 | COMPOSITE-FATIGUE 100.6364, $0.300,0.300$ |
|  | 1. Point of Interest : 100.6364 |
|  | 2. r/h (Bottom Rebar) : 0.300 |
|  | 3. r/h (Top Rebar) : 0.300 |
| 9-7.3 | PRESTRESS-FATIGUE 100.6364, 18.0000 |
|  | 1. Point of Interest : 100.6364 |
|  | 2. Stress Range : 18.000 |
| 5-2.1 | OUTPUT-INTERMEDIATE 100.6364, ON, ON |
|  | 1. Point of Interest : 100.6364 |
|  | 2. Specification Checks : ON |
|  | 3. Load Factoring/Combination : ON |
| 3-1.1 | COMMENT DC1 |
| 12-1.2 | LOAD-DEAD-DESCR 1, DC, 1, DC1 |
|  | 1. Load Group Number : 1 |
|  | 2. Dead Load Type : DC |
|  | 3. Stage : 1 |
|  | 4. Load Group Name : DC1 |
| 12-1.3 | LOAD-DEAD-UNIFORM 1, 1, 0.000, 0.014583, 1320.000, 0.014583 |
|  | 1. Load Group Number : 1 |
|  | 2. Span Number : 1 |
|  | 3. Distance to Start of Load : 0.000 |
|  | 4. Magnitude of Load (Beginning) : 0.015 |
|  | 5. Distance to End of Load : 1320.000 |
|  | 6. Magnitude of Load (End) : 0.015 |
| 12-1.3 | LOAD-DEAD-UNIFORM 1, 2, 0.000, 0.014583, 1320.000, 0.014583 |
|  | 1. Load Group Number : 1 |
|  | 2. Span Number : 2 |
|  | 3. Distance to Start of Load : 0.000 |
|  | 4. Magnitude of Load (Beginning) : 0.015 |
|  | 5. Distance to End of Load : 1320.000 |
|  | 6. Magnitude of Load (End) : 0.015 |
| 12-1.4 | LOAD-DEAD-POINT 1, 1, $0.0000,5.0630,654.0000$ |
|  | 1. Load Group Number : 1 |
|  | 2. Span Number : 1 |
|  | 3. Mag of Point Load (Horizontal): 0.000 |
|  | 4. Mag of Point Load (Vertical) : 5.063 |
|  | 5. Distance to Start of Load : 654.000 |
| 12-1.4 | LOAD-DEAD-POINT 1, 2, 0.0000 , 5.0600, 660.0000 |
|  | 1. Load Group Number : 1 |
|  | 2. Span Number : 2 |
|  | 3. Mag of Point Load (Horizontal): 0.000 |
|  | 4. Mag of Point Load (Vertical) : 5.060 |




```
            6. Scale Factor : 1.000
            6. Scale Factor ( Lanes Loaded ( CRIT 1.
            8. Notional Load Control
        | CRIT 1.0000
            9. Dynamic Load Allowance :
            10. Special Trk/Lane No.
    11. Variable Axle Spacing
12-4.3
12-4.3
12-4.6
12-4.7
12-4.7
12-4.6
12-4.6
9-2.3
```

```
    11. Variable Axle Spacing
        lol
TKT, D, 100.0000, 1.0000, CRIT, YES
            1. Live Load Number : 3
        lol
```



```
        lu
        lol
```



```
        lol
    CRIT
        lol
    YES
        lol
        lol
        lol
            LOAD-LIVE-DEFINITION 4, DLN_HL-93_~5, DLN, D, 100.0000, 1.0000, CRIT, YES
            1. Live Load Number : 4
            2. Live Load Code
    : DLN_HL-93_~5
            3. Live Load Type
                            : DLN
            4. Design/Rating Procedure
            5. % of Dynamic Load Allow.
            : D
        100.000
            6. Scale Factor
            7. Lanes Loaded
            8. Notional Load Control
        CRIT
            9. Dynamic Load Allowance
            10. Special Trk/Lane No.
            11. Variable Axle Spacing
    LOAD-LIVE-COMBO 1, 4
            1. Live Load Number: Truck
            2. Live Load Number: Lane
            1
            4
            3. Combination Factor: Truck
            4. Combination Factor: Lane
    LOAD-LIVE-DEFLECTION 1, , 1.0,
            1. Live Load Number: Truck
            2. Live Load Number: Lane
            3. Combination Factor: Truck
                1.000
            4. Combination Factor: Lane
            5. Allowable Defl. Denom.
            6. Absolute Allowable Defl.
LOAD-LIVE-DEFLECTION 1, 4, 0.25, 1.0
12-4. Live Load Number: Truck
            2. Live Load Number: Lane
            3. Combination Factor: Truck
        1
            3. Combination Factor: Truck : 0. 0.250
            5. Allowable Defl. Denom. :
            6. Absolute Allowable Defl. :
        LOAD-LIVE-COMBO 2, 4
            1. Live Load Number: Truck
            2
            2. Live Load Number: Lane
                                4
            3. Combination Factor: Truck
            4. Combination Factor: Lane :
LOAD-LIVE-COMBO 3, 4
            1. Live Load Number: Truck
            1
            4. Combination Factor: Lane
```



```
            1.000
            :
    2. Live Load Number: Lane
        3
        4
    3. Combination Factor: Truck :
    4. Combination Factor: Lane :
PS-BEAM-OVERHANG 1, 9.000, 9.000
            1. Span Number
    1
    2. Beam Overhang (Left)
    : 100.000
    :
    10. Special Trk/Lane No.
        4
            T
CRIT
    D
                00.000
    :
        1. Live Load Number 
    \square
            4
```



```
:
        | % 100.000
            .000
```



```
:
```











```
12-5.1
12-5.2 DIST-REACTION 1, 0.9730, 0.7960, 0.6670, 0.9730, 0.7960, 0.6670
12-5.2 DIST-REACTION 1, 0.9730, 0.7960, 0.6670, 0.9730, 0.7960, 0.6670
    1. Support Number : 1
    2. g(Shear-1) : 0.973
    3.g(Moment-1) : 0.796
    4. g(Deflection-1) : 0.667
    5. g(Shear-M) : 0.973
    6. g(Moment-M) : 0.796
    7. g(Deflection-M) : 0.667
12-5.1 DIST-BEAM-SCHEDULE 2, D, 0.6670, 0.6670, 0.0000, 1320.0000
    1. Span Number : 2
    2. Action Code : D
    3. mg(one-lane) : 0.667
    4. mg(mult-lanes) : 0.667
    5. Start Distance : 0.000
    6. Range : 1320.000
12-5.1 DIST-BEAM-SCHEDULE 2, M, 0.7960, 0.7960, 0.0000, 1320.0000
    1. Span Number : 2
    2. Action Code : M
    3. mg(one-lane) : 0.796
    4.mg(mult-lanes) : 0.796
    5. Start Distance : 0.000
    6. Range : 1320.000
12-5.1 DIST-BEAM-SCHEDULE 2, V, 0.9730, 0.9730, 0.0000, 1320.0000
    1. Span Number : 2
    2. Action Code : V
    3. mg(one-lane) : 0.973
    4. mg(mult-lanes) : 0.973
    5. Start Distance : 0.000
    6. Range : 1320.000
12-5.2 DIST-REACTION 2, 0.9730, 0.7960, 0.6670,0.9730,0.7960, 0.6670
    1. Support Number : 2
    2. g(Shear-1) : 0.973
    3.g(Moment-1) : 0.796
    4.g(Deflection-1) : 0.667
    5. g(Shear-M) : 0.973
    6. g(Moment-M) : 0.796
    7. g(Deflection-M) : 0.667
12-5.2 DIST-REACTION 3, 0.9730, 0.7960, 0.6670, 0.9730, 0.7960, 0.6670
    1. Support Number : 3
    2. g(Shear-1) : 0.973
    3. g(Moment-1) : 0.796
    4.g(Deflection-1) : 0.667
    5. g(Shear-M) : 0.973
    6. g(Moment-M) : 0.796
    7. g(Deflection-M) : 0.667
3-1.1 COMMENT Using system default LRFD load factors.
13-1.1 FACTORS-LOAD-MOD ST, 1, 1.000, 1.000, 1.000, 1.000, 1.000
    1. Limit State : ST
    2. Limit State Level : 1
    3. eta D : 1.000
    4. eta R : 1.000
    5. eta I : 1.000
    6. eta (max) : 1.000
    7. eta (min) : 1.000
13-1.2
ST, 1, 1.250, 0.900, 1.500, 0.650
    DIST-BEAM-SCHEDULE 1, V, 0.9730, 0.9730, 0.0000, 1320.0000
    1. Span Number : 1
    2. Action Code : V
    3. mg(one-lane) : 0.973
    4. mg(mult-lanes) : 0.973
    5. Start Distance : 0.000
    . Start Distance . . 1320.000
FACTORS-LOAD-DL
    1. Limit State : ST
```







End of Input File No. 1

Appendix A
Prestressed Concrete Bridge Design Example

DECK GEOMETRY AND LOAD SUMMARY REPORT

```
    No. Girders: 6
    Girder Spacing, in
        Bay No. Spacing
1116.004
\(2 \quad 116.004\)
            3 116.004
            4 116.004
            5 116.004
Cantilevers:
    Left = 42.250 in
    Right = 42.230 in
Deck Width = 664.500 in
Slab Thickness = 8.000 in
```

DECK GEOMETRY AND LOAD SUMMARY REPORT (continued)


GIRDER LOADS SUMMARY REPORT

Units: Loads are in k/ft.

Girder Loads Due to Deck Components:

| Component | Slab | Soffit | Curbs | Median | Topping | Wearing Surface |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stage | 1 | 1 | 2 | 2 | 1 | 2 |
| DL Type | DC | DC | DC | DC | DC | DW |
| Girder No. |  |  |  |  |  |  |
| 1 | 0.835 | 0.000 | 0.000 | 0.000 | 0.000 | 0.260 |
| 2 | 0.967 | 0.000 | 0.000 | 0.000 | 0.000 | 0.260 |
| 3 | 0.967 | 0.000 | 0.000 | 0.000 | 0.000 | 0.260 |
| 4 | 0.967 | 0.000 | 0.000 | 0.000 | 0.000 | 0.260 |
| 5 | 0.967 | 0.000 | 0.000 | 0.000 | 0.000 | 0.260 |
| 6 | 0.835 | 0.000 | 0.000 | 0.000 | 0.000 | 0.260 |


| Load Group | 1 | 2 |  | 3 |  | 4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stage | 1 | 2 |  | N/A |  | N/A |  |
| DL Type | DC | DC |  | N/A |  | N/A |  |
| Line Loads |  |  |  |  |  |  |  |
| Girder No. |  |  |  |  |  |  |  |
| 1 | 0.649 | 0.000 |  | 0.000 |  | 0.000 |  |
| 2 | 0.000 | 0.000 |  | 0.000 |  | 0.000 |  |
| 3 | 0.000 | 0.000 |  | 0.000 |  | 0.000 |  |
| 4 | 0.000 | 0.000 |  | 0.000 |  | 0.000 |  |
| 5 | 0.000 | 0.000 |  | 0.000 |  | 0.000 |  |
| 6 | 0.649 | 0.000 |  | 0.000 |  | 0.000 |  |
| GIRDER LOADS SUMMARY REPORT (continued) |  |  |  |  |  |  |  |
| Units: Loads are in k/ft. |  |  |  |  |  |  |  |
| Girder of Interest: 2 |  |  |  |  |  |  |  |
| Total Loads Due to Superimposed Dead Loads |  |  |  |  |  |  |  |
| Stage | 1 |  |  | 2 |  |  |  |
| DL Type | DC | DW | DC |  | DW | DC | DW |
| Girder No. |  |  |  |  |  |  |  |
| 1 | 0.835 | 0.000 | 0.000 |  | 0.260 | 0.000 | 0.000 |
| => 2 | 0.967 | 0.000 | 0.000 |  | 0.260 | 0.000 | 0.000 |
| 3 | 0.967 | 0.000 | 0.000 |  | 0.260 | 0.000 | 0.000 |
| 4 | 0.967 | 0.000 | 0.000 |  | 0.260 | 0.000 | 0.000 |
| 5 | 0.967 | 0.000 | 0.000 |  | 0.260 | 0.000 | 0.000 |
| 6 | 0.835 | 0.000 | 0.000 |  | 0.260 | 0.000 | 0.000 |

Total Loads Due to Load Groups:

Load Group 112 | 4 | 3 | 4 |
| :--- | :--- | :--- | :--- |

        Girder No.
    | 1 | 0.649 | 0.000 | 0.000 | 0.000 |
| :--- | :--- | :--- | :--- | :--- |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 |
| 3 | 0.000 | 0.000 | 0.000 | 0.000 |
| 4 | 0.000 | 0.000 | 0.000 | 0.000 |
| 5 | 0.000 | 0.000 | 0.000 | 0.000 |
| 6 | 0.649 | 0.000 | 0.000 | 0.000 |

Total Loads:

| Stage | 1 | 2 | 3 | $2+3$ |
| :---: | :---: | :---: | :---: | :---: |
| Girder No. |  |  |  |  |
| 1 | 1.485 | 0.260 | 0.000 | 1.745 |
| $=>2$ | 0.967 | 0.260 | 0.000 | 1.227 |
| 3 | 0.967 | 0.260 | 0.000 | 1.227 |
| 4 | 0.967 | 0.260 | 0.000 | 1.227 |
| 5 | 0.967 | 0.260 | 0.000 | 1.227 |
| 6 | 1.484 | 0.260 | 0.000 | 1.744 |

Self-Load Summary:

| Span No. | Beginning of Load |  | End of Load |  |
| :---: | :---: | :---: | :---: | :---: |
|  | ance | agnitude | Distance | Magnitud |
| 1 | 0.00 | 0.094184 | 1320.00 | 0.094184 |
| 2 | 0.00 | 0.094184 | 1320.00 | 0.094184 |

Distributed Dead Load Summary:
Load Group No. 1: DC1

Load Group No. 1: DC1
Load Group No. 2: DC2

| Load | Span | Beginning of Load |  | End of Load |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Group No. | No. | Distance, | Magnitude, | Distance, | gnitude, |
| DC1 | All |  | 0.08056 |  | 0.08056 |
| DW2 | All |  | 0.02167 |  | 0.02167 |
| 1 | 1 | 0.00 | 0.01458 | 1320.00 | 0.01458 |
| 1 | 2 | 0.00 | 0.01458 | 1320.00 | 0.01458 |
| 2 | 1 | 0.00 | 0.01800 | 1320.00 | 0.01800 |
| 2 | 2 | 0.00 | 0.01800 | 1320.00 | 0.01800 |

Note: A span number denoted as "*" indicates the distances reference the left end of the bridge and the load may extend over one or more spans.

Beam Properties: General span segments variation.
Construction Stage: 1
Span No. 1 Span Length $=110.000$ (ft) Span Ratio $=1.000 \quad \mathrm{E}=4696.0$ (ksi)
Input Dimensions and Cross-Section Geometry: (in)

| Span | Dist | Web | Web Width |  | Flange top | Thickness bot | Flange top | Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Point | (ft) | Depth | top | bot |  |  |  | bot |
| 1.000 | 0.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.016 | 1.750 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.064 | 7.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.091 | 10.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.100 | 11.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.114 | 12.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.200 | 22.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.223 | 24.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.300 | 33.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.400 | 44.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.500 | 55.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.600 | 66.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.700 | 77.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.750 | 82.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.777 | 85.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.800 | 88.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.886 | 97.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.900 | 99.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.909 | 100.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.984 | 108.250 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 2.000 | 110.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |

Calculated Properties:

| Span <br> Point | $\begin{gathered} \text { Dist } \\ \text { (ft) } \end{gathered}$ | $\begin{gathered} \mathrm{A} \\ \left(\mathrm{in}^{\wedge} 2\right) \end{gathered}$ | $\begin{gathered} I \\ \left(i n^{\wedge} 4\right) \end{gathered}$ | $\begin{aligned} & \text { X-bar } \\ & \text { (in) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.000 | 0.000 | 1085.0 | 733320.3 | 36.38 |
| 1.016 | 1.750 | 1085.0 | 733320.3 | 36.38 |
| 1.064 | 7.000 | 1085.0 | 733320.3 | 36.38 |
| 1.091 | 10.000 | 1085.0 | 733320.3 | 36.38 |
| 1.100 | 11.000 | 1085.0 | 733320.3 | 36.38 |
| 1.114 | 12.500 | 1085.0 | 733320.3 | 36.38 |
| 1.200 | 22.000 | 1085.0 | 733320.3 | 36.38 |
| 1.223 | 24.500 | 1085.0 | 733320.3 | 36.38 |
| 1.300 | 33.000 | 1085.0 | 733320.3 | 36.38 |
| 1.400 | 44.000 | 1085.0 | 733320.3 | 36.38 |
| 1.500 | 55.000 | 1085.0 | 733320.3 | 36.38 |
| 1.600 | 66.000 | 1085.0 | 733320.3 | 36.38 |
| 1.700 | 77.000 | 1085.0 | 733320.3 | 36.38 |
| 1.750 | 82.500 | 1085.0 | 733320.3 | 36.38 |
| 1.777 | 85.500 | 1085.0 | 733320.3 | 36.38 |
| 1.800 | 88.000 | 1085.0 | 733320.3 | 36.38 |
| 1.886 | 97.500 | 1085.0 | 733320.3 | 36.38 |
| 1.900 | 99.000 | 1085.0 | 733320.3 | 36.38 |
| 1.909 | 100.000 | 1085.0 | 733320.3 | 36.38 |
| 1.984 | 108.250 | 1085.0 | 733320.3 | 36.38 |
| 2.000 | 110.000 | 1085.0 | 733320.3 | 36.38 |

CONCRETE PROPERTIES:


PRESTRESSING STRAND PROPERTIES:



Notes:
$\Rightarrow$ Debond, transfer, and/or development lengths are measured from the end of the beam.
=> Search for the report header "Suggested Development Length Commands" for generated commands containing the development lengths computed by BRASS for each prestress row.

This report is only available if a mid-span point of interest is entered in the data file.

SUMMARY OF BEAM OVERHANGS:

| Span | Beam Overhangs (in) |  |
| :---: | :---: | ---: |
| No. | Left End | Right End |
| $-------------------------1000 ~$ | 9.000 |  |

PRESTRESS LOSS INPUT DATA: AASHTO LRFD 5.9.5

Relative Humidity $=70.00 \%$

| Strand | Steel | Relaxation Loss | Coefficients | of of DL Applied |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Base | FR | ES | SR \& CR | Time of Release |
| $------------------------------------------------------------------~$ |  |  |  |  |  |

STRAND PROPERTIES: (cont.)

| Span No. | Row <br> No. | Path Type | Strand Type No. | No. <br> Strands | Stage <br> Strand Tensioned | No. <br> Debonded Strands | Debond <br> Left <br> (in) | gth <br> Right <br> (in) | Development Length (in) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | Straight | 1 | 8 | 1 | N/A | N/A | N/A | 82.500 |
| 1 | 2 | Straight | 1 | 2 | 1 | 2 | 129.000 | 129.000 | 82.500 |
| 1 | 3 | Straight | 1 | 2 | 1 | 2 | 273.000 | 273.000 | 82.500 |
| 1 | 4 | Straight | 1 | 8 | 1 | N/A | N/A | N/A | 82.500 |
| 1 | 5 | Straight | 1 | 2 | 1 | 2 | 129.000 | 129.000 | 82.500 |
| 1 | 6 | Straight | 1 | 2 | 1 | 2 | 273.000 | 273.000 | 82.500 |
| 1 | 7 | Straight | 1 | 6 | 1 | N/A | N/A | N/A | 82.500 |
| 1 | 8 | Straight | 1 | 2 | 1 | 2 | 129.000 | 129.000 | 82.500 |
| 1 | 9 | Straight | 1 | 2 | 1 | 2 | 273.000 | 273.000 | 82.500 |
| 1 | 10 | Straight | 1 | 6 | 1 | N/A | N/A | N/A | 82.500 |
| 1 | 11 | Straight | 1 | 4 | 1 | N/A | N/A | N/A | 82.500 |
| 2 | 1 | Straight | 1 | 8 | 1 | N/A | N/A | N/A | 82.500 |
| 2 | 2 | Straight | 1 | 2 | 1 | 2 | 129.000 | 129.000 | 82.500 |
| 2 | 3 | Straight | 1 | 2 | 1 | 2 | 273.000 | 273.000 | 82.500 |
| 2 | 4 | Straight | 1 | 8 | 1 | N/A | N/A | N/A | 82.500 |
| 2 | 5 | Straight | 1 | 2 | 1 | 2 | 129.000 | 129.000 | 82.500 |
| 2 | 6 | Straight | 1 | 2 | 1 | 2 | 273.000 | 273.000 | 82.500 |
| 2 | 7 | Straight | 1 | 6 | 1 | N/A | N/A | N/A | 82.500 |
| 2 | 8 | Straight | 1 | 2 | 1 | 2 | 129.000 | 129.000 | 82.500 |
| 2 | 9 | Straight | 1 | 2 | 1 | 2 | 273.000 | 273.000 | 82.500 |
| 2 | 10 | Straight | 1 | 6 | 1 | N/A | N/A | N/A | 82.500 |
| 2 | 11 | Straight | 1 | 4 | 1 | N/A | N/A | N/A | 82.500 |

STRAIGHT STRAND DETAILS:


| 2 | 2 | 70.000 | Not Continuous Over Either Support |
| ---: | ---: | ---: | :--- |
| 2 | 3 | 70.000 | Not Continuous Over Either Support |
| 2 | 4 | 68.000 | Not Continuous Over Either Support |
| 2 | 5 | 68.000 | Not Continuous Over Either Support |
| 2 | 6 | 68.000 | Not Continuous Over Either Support |
| 2 | 7 | 66.000 | Not Continuous Over Either Support |
| 2 | 8 | 66.000 | Not Continuous Over Either Support |
| 2 | 9 | 66.000 | Not Continuous Over Either Support |
| 2 | 10 | 64.000 | Not Continuous Over Either Support |
| 2 | 11 | 62.000 | Not Continuous Over Either Support |

Self-Load Summary:

| Span | Beginning of Load |  | End of Load |  |
| :---: | :---: | :---: | :---: | :---: |
| No. | ance, | Magnitude, | Distance | Magnitude |
| 1 | 0.00 | 0.094184 | 1320.00 | 0.094184 |
| 2 | 0.00 | 0.094184 | 1320.00 | 0.094184 |

Distributed Dead Load Summary:
Load Group No. 1: DC1
Load Group No. 2: DC2

| Load | Span <br> No. | Beginning of Load <br> Droup No. |  | End of Load |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Nonce, in Magnitude, k/in | Distance, in | Magnitude, k/in |  |  |  |

Note: A span number denoted as "*" indicates the distances reference the left end of the bridge and the load may extend over one or more spans.

```
Beam Properties: General span segments variation.
    Construction Stage: 2
    Span No. 1 Span Length = 110.000 (ft) Span Ratio = 1.000 E = 4696.0 (ksi)
```

    Input Dimensions and Cross-Section Geometry: (in)
    | Span <br> Point | $\begin{gathered} \text { Dist } \\ \text { (ft) } \end{gathered}$ | Web Depth | $\begin{aligned} & \text { Web } \\ & \text { top } \end{aligned}$ | th bot | Flange top | Thickness bot | Flange top | Width bot |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.000 | 0.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.016 | 1.750 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.064 | 7.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.091 | 10.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.100 | 11.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.114 | 12.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.200 | 22.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.223 | 24.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.300 | 33.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.400 | 44.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.500 | 55.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.600 | 66.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.700 | 77.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.750 | 82.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.777 | 85.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.800 | 88.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |


| 1.886 | 97.500 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1.900 | 99.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.909 | 100.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 1.984 | 108.250 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |
| 2.000 | 110.000 | 59.00 | 8.000 | 8.000 | 5.000 | 8.000 | 42.00 | 28.00 |

Calculated Properties:

| Span <br> Point | Dist <br> (ft) | A <br> (in^2) | I <br> (in^4) | X-bar <br> (in) |
| :--- | ---: | :---: | :---: | ---: |
| ---000 | 0.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.000 | 1.750 | 1731.0 | 1363966.1 | 51.07 |
| 1.016 | 7.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.064 | 10.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.091 | 11.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.100 | 12.500 | 1731.0 | 1363966.1 | 51.07 |
| 1.114 | 22.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.200 | 24.500 | 1731.0 | 1363966.1 | 51.07 |
| 1.223 | 33.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.300 | 44.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.400 | 55.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.500 | 66.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.600 | 77.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.700 | 82.500 | 1731.0 | 1363966.1 | 51.07 |
| 1.750 | 85.500 | 1731.0 | 1363966.1 | 51.07 |
| 1.777 | 88.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.800 | 97.500 | 1731.0 | 1363966.1 | 51.07 |
| 1.886 | 99.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.900 | 100.000 | 1731.0 | 1363966.1 | 51.07 |
| 1.909 | 108.250 | 1731.0 | 1363966.1 | 51.07 |
| 1.984 | 110.000 | 1731.0 | 1363966.1 | 51.07 |

Slab Geometry and Reinforcement: (in, in^2)

| Span <br> Point | $\begin{gathered} \text { Dist } \\ \text { (ft) } \end{gathered}$ | Eff. <br> Width | Thickness | Gap | $\begin{aligned} & \text { Top } \\ & \text { Area } \end{aligned}$ | Row Dist | Bottom Area | Row <br> Dist |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.000 | 0.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.016 | 1.750 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.064 | 7.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.091 | 10.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.100 | 11.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.114 | 12.500 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.200 | 22.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.223 | 24.500 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.300 | 33.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.400 | 44.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.500 | 55.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.600 | 66.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.700 | 77.000 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.750 | 82.500 | 111.00 | 7.50 | 0.00 | 2.00 | 4.25 | 3.72 | 1.94 |
| 1.777 | 85.500 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |
| 1.800 | 88.000 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |
| 1.886 | 97.500 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |
| 1.900 | 99.000 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |
| 1.909 | 100.000 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |
| 1.984 | 108.250 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |
| 2.000 | 110.000 | 111.00 | 7.50 | 0.00 | 0.00 | 0.00 | 14.52 | 3.03 |


| Beam Distribution Factor Schedule: Shear |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Span No. | Distan Start | End | mg (1-1ane) | mg (M-lanes) |
| 1 | 0.000 | 1320.000 | 0.973 | 0.973 |
|  |  |  | (USER) | ( M, USER) |
| 2 | 0.000 | 1320.000 | 0.973 | 0.973 |
|  |  |  | (USER) | ( M, USER) |
| Beam Distribution Factor Schedule: Moment |  |  |  |  |
|  | Distanc |  |  |  |
| Span No. | Start | End | mg (1-lane) | mg (M-lanes) |
| 1 | 0.000 | 1320.000 | 0.796 | 0.796 |
|  |  |  | (USER) | ( M, USER) |
| 2 | 0.000 | 1320.000 | 0.796 | 0.796 |
|  |  |  | (USER) | ( M, USER) |
| Beam Distribution Factor Schedule: Deflection |  |  |  |  |
|  | Distanc |  |  |  |
| Span No. | Start | End | mg (1-1ane) | mg (M-lanes) |
| 1 | 0.000 | 1320.000 | 0.667 | 0.667 |
|  |  |  | (USER) | ( M, USER) |
| 2 | 0.000 | 1320.000 | 0.667 | 0.667 |
|  |  |  | (USER) | ( M, USER) |

Reaction Distribution Factors:

|  | One-Lane Loaded |  |  | Multiple-Lanes Loaded |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Support No. | Moment | Shear | Deflection | Moment | Shear | Deflection |
| 1 | $0.796$ <br> (USER) | $0.973$ <br> (USER) | $\begin{aligned} & 0.667 \\ & \text { (USER) } \end{aligned}$ | $\begin{gathered} 0.796 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ | $\begin{gathered} 0.973 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ | $\begin{gathered} 0.667 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ |
| 2 | $\begin{aligned} & 0.796 \\ & \text { (USER) } \end{aligned}$ | $0.973$ <br> (USER) | $\begin{aligned} & 0.667 \\ & \text { (USER) } \end{aligned}$ | $\begin{gathered} 0.796 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ | $\begin{gathered} 0.973 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ | $\begin{gathered} 0.667 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ |
| 3 | $0.796$ <br> (USER) | $0.973$ <br> (USER) | $\begin{aligned} & 0.667 \\ & \text { (USER) } \end{aligned}$ | $\begin{gathered} 0.796 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ | $\begin{gathered} 0.973 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ | $\begin{gathered} 0.667 \\ (\mathrm{M}, \mathrm{USER}) \end{gathered}$ |

Notes:
=> Below each distribution factor, the method used to determine the distribution factor is included in parenthesis. USER = User Input LR-T = Lever Rule Specified in AASHTO LRFD Table LRFD $=$ AASHTO LRFD Formulas $\quad$ LR-O $=$ Lever Rule Override RG-O = Rigid Method Override
=> Additionally, for multiple-lanes loaded, the number of lanes loaded is shown. An 'M' is used with the USER and LRFD methods because the number of multiple lanes is unknown.
=> The Lever Rule Override is invoked when the ranges of applicability are not satisfied for the AASHTO LRFD distribution factor formulas.

LIVE LOAD SETTINGS SUMMARY:

|  |  | Scale | Percent | Fixed | Live Load | Rating |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. | Name | Description | Impact | Impact | Type | Procedure |

LIVE LOAD COMBINATIONS SUMMARY:

| Comb . |  |  |  | Truck | Lane | Combination |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Factors |  |  |  |  |  |  |
| No. | Name | Description | No. | No. | Truck | Lane |
| 1 | DTK_HL-93_~1 | DTK_HL-93_~1 + DLN_HL-93_~5 | 1 | 4 | 1.000 | 1.000 |
| 2 | DTM_HL-93_~2 | DTM_HL-93_~2 + DLN_HL-93_~5 | 2 | 4 | 1.000 | 1.000 |
| 3 | TKT_HL-93_~3 | TKT_HL-93_~3 + DLN_HL-93_~5 | 3 | 4 | 0.900 | 0.900 |

LOAD FACTORS SUMMARY:

| Limit State | eta D eta R | eta I | eta T | eta T |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| MAX |  |  |  |  |


| Limit State | DC |  | DW |  | LL |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | MAX | MIN | MAX | MIN |  |
| STRENGTH I | 1.25 | 0.90 | 1.50 | 0.65 | 1.75 |
| STRENGTH II | 1.25 | 0.90 | 1.50 | 0.65 | 1.35 |
| STRENGTH III | 1.25 | 0.90 | 1.50 | 0.65 | 0.00 |
| STRENGTH IV | 1.50 | 1.50 | 1.50 | 0.65 | 0.00 |
| SERVICE I | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| SERVICE II | 1.00 | 1.00 | 1.00 | 1.00 | 1.30 |
| SERVICE III | 1.00 | 1.00 | 1.00 | 1.00 | 0.80 |
| FATIGUE | 1.00 | 1.00 | 1.00 | 1.00 | 0.75 |


| Limit State | TU |  | SE |  | PS |  | MS |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: |
| MAX | MIN | MAX | MIN | MAX | MIN | MAX | MIN |  |
| $===================================================================$ |  |  |  |  |  |  |  |  |
| STRENGTH I | 1.20 | 1.20 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| STRENGTH II | 1.20 | 1.20 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| STRENGTH III | 1.20 | 1.20 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| STRENGTH IV | 1.20 | 1.20 | 0.00 | 0.00 | 1.00 | 1.00 | 1.00 | 1.00 |


| SERVICE I | 1.20 | 1.20 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SERVICE II | 1.20 | 1.20 | 0.00 | 0.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| SERVICE III | 1.20 | 1.20 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| FAtigue | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |


| RESISTANCE FACTORS SUMM |  |
| :--- | :--- |
|  |  |
| Resistance |  |
| Type | phi |
| $=================$ |  |
| Flexure | 1.00 |
| Flx/Tens (R/C) | 0.90 |
| Shear | 0.90 |
| Fatigue | 1.00 |

## Section A4 - Opis Output

## Noncomposite Effects

-Girder

| Span | Location <br> (ft.) | \%Span | Moment $(\mathrm{k}-\mathrm{ft})$ | Shear <br> (k) | Axial <br> (k) | Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 62.16 | 0 | 62.16 |
| 1 | 1.75 | 1.6 | 107.06 | 60.18 | 0 |  |
| 1 | 10.0 | 9.1 | 565.12 | 50.86 | 0 |  |
| 1 | 11.0 | 10 | 615.44 | 49.73 | 0 |  |
| 1 | 12.5 | 11.4 | 688.73 | 48.03 | 0 |  |
| 1 | 22.0 | 20 | 1094.06 | 37.3 | 0 |  |
| 1 | 24.5 | 22.3 | 1183.75 | 34.47 | 0 |  |
| 1 | 33.0 | 30 | 1435.93 | 24.86 | 0 |  |
| 1 | 44.0 | 40 | 1641.06 | 12.43 | 0 |  |
| 1 | 55.0 | 50 | 1709.44 | 0 | 0 |  |
| 1 | 66.0 | 60 | 1641.07 | -12.43 | 0 |  |
| 1 | 77.0 | 70 | 1435.93 | -24.86 | 0 |  |
| 1 | 85.5 | 77.7 | 1183.76 | -34.47 | 0 |  |
| 1 | 88.0 | 80 | 1094.07 | -37.3 | 0 |  |
| 1 | 97.5 | 88.6 | 688.75 | -48.03 | 0 |  |
| 1 | 99.0 | 90 | 615.45 | -49.73 | 0 |  |
| 1 | 100.0 | 90.9 | 565.13 | -50.86 | 0 |  |
| 1 | 108.25 | 98.4 | 107.08 | -60.18 | 0 |  |
| 1 | 110.0 | 100 | 0 | -62.16 | 0 | 124.32 |
| 2 | 0 | 0 | 0 | 62.16 | 0 | 124.32 |
| 2 | 1.75 | 1.6 | 107.08 | 60.18 | 0 |  |
| 2 | 10.0 | 9.1 | 565.14 | 50.86 | 0 |  |
| 2 | 11.0 | 10 | 615.45 | 49.73 | 0 |  |
| 2 | 12.5 | 11.4 | 688.75 | 48.03 | 0 |  |
| 2 | 22.0 | 20 | 1094.07 | 37.3 | 0 |  |
| 2 | 24.5 | 22.3 | 1183.77 | 34.47 | 0 |  |
| 2 | 33.0 | 30 | 1435.94 | 24.86 | 0 |  |
| 2 | 44.0 | 40 | 1641.07 | 12.43 | 0 |  |
| 2 | 55.0 | 50 | 1709.45 | 0 | 0 |  |
| 2 | 66.0 | 60 | 1641.08 | -12.43 | 0 |  |
| 2 | 77.0 | 70 | 1435.94 | -24.86 | 0 |  |
| 2 | 85.5 | 77.7 | 1183.77 | -34.47 | 0 |  |
| 2 | 88.0 | 80 | 1094.07 | -37.3 | 0 |  |
| 2 | 97.5 | 88.6 | 688.75 | -48.03 | 0 |  |
| 2 | 99.0 | 90 | 615.45 | -49.73 | 0 |  |
| 2 | 100.0 | 90.9 | 565.14 | -50.86 | 0 |  |
| 2 | 108.25 | 98.4 | 107.09 | -60.18 | 0 |  |
| 2 | 110.0 | 100 | 0 | -62.16 | 0 | 62.16 |

-Slab

| Span | Location <br> (ft.) | \%Span | Moment $(\mathrm{k}-\mathrm{ft})$ | Shear <br> (k) | Axial <br> (k) | Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 53.17 | 0 | 53.17 |
| 1 | 1.75 | 1.6 | 91.57 | 51.48 | 0 |  |
| 1 | 10.0 | 9.1 | 483.36 | 43.5 | 0 |  |
| 1 | 11.0 | 10 | 526.4 | 42.53 | 0 |  |
| 1 | 12.5 | 11.4 | 589.09 | 41.08 | 0 |  |
| 1 | 22.0 | 20 | 935.78 | 31.9 | 0 |  |
| 1 | 24.5 | 22.3 | 1012.5 | 29.48 | 0 |  |
| 1 | 33.0 | 30 | 1228.19 | 21.27 | 0 |  |
| 1 | 44.0 | 40 | 1403.65 | 10.63 | 0 |  |
| 1 | 55.0 | 50 | 1462.14 | 0 | 0 |  |
| 1 | 66.0 | 60 | 1403.65 | -10.63 | 0 |  |
| 1 | 77.0 | 70 | 1228.2 | -21.27 | 0 |  |
| 1 | 85.5 | 77.7 | 1012.51 | -29.48 | 0 |  |
| 1 | 88.0 | 80 | 935.79 | -31.9 | 0 |  |
| 1 | 97.5 | 88.6 | 589.1 | -41.08 | 0 |  |
| 1 | 99.0 | 90 | 526.41 | -42.53 | 0 |  |
| 1 | 100.0 | 90.9 | 483.38 | -43.5 | 0 |  |
| 1 | 108.25 | 98.4 | 91.59 | -51.48 | 0 |  |
| 1 | 110.0 | 100 | 0 | -53.17 | 0 | 106.34 |
| 2 | 0 | 0 | 0 | 53.17 | 0 | 106.34 |
| 2 | 1.75 | 1.6 | 91.59 | 51.48 | 0 |  |
| 2 | 10.0 | 9.1 | 483.38 | 43.5 | 0 |  |
| 2 | 11.0 | 10 | 526.41 | 42.53 | 0 |  |
| 2 | 12.5 | 11.4 | 589.11 | 41.08 | 0 |  |
| 2 | 22.0 | 20 | 935.79 | 31.9 | 0 |  |
| 2 | 24.5 | 22.3 | 1012.51 | 29.48 | 0 |  |
| 2 | 33.0 | 30 | 1228.2 | 21.27 | 0 |  |
| 2 | 44.0 | 40 | 1403.66 | 10.63 | 0 |  |
| 2 | 55.0 | 50 | 1462.14 | 0 | 0 |  |
| 2 | 66.0 | 60 | 1403.66 | -10.63 | 0 |  |
| 2 | 77.0 | 70 | 1228.2 | -21.27 | 0 |  |
| 2 | 85.5 | 77.7 | 1012.51 | -29.48 | 0 |  |
| 2 | 88.0 | 80 | 935.79 | -31.9 | 0 |  |
| 2 | 97.5 | 88.6 | 589.11 | -41.08 | 0 |  |
| 2 | 99.0 | 90 | 526.41 | -42.53 | 0 |  |
| 2 | 100.0 | 90.9 | 483.38 | -43.5 | 0 |  |
| 2 | 108.25 | 98.4 | 91.59 | -51.48 | 0 |  |
| 2 | 110.0 | 100 | 0 | -53.17 | 0 | 53.17 |

-Haunch

| Span | Location <br> (ft.) | \%Span | Moment <br> (k-ft) | Shear <br> (k) | Axial <br> (k) | Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 12.18 | 0 | 12.18 |
| 1 | 1.75 | 1.6 | 21.05 | 11.87 | 0 |  |
| 1 | 10.0 | 9.1 | 113.05 | 10.43 | 0 |  |
| 1 | 11.0 | 10 | 123.39 | 10.25 | 0 |  |
| 1 | 12.5 | 11.4 | 138.57 | 9.99 | 0 |  |
| 1 | 22.0 | 20 | 225.6 | 8.33 | 0 |  |
| 1 | 24.5 | 22.3 | 245.87 | 7.89 | 0 |  |
| 1 | 33.0 | 30 | 306.63 | 6.4 | 0 |  |
| 1 | 44.0 | 40 | 366.49 | 4.48 | 0 |  |
| 1 | 55.0 | 50 | 402.65 | -2.51 | 0 |  |
| 1 | 66.0 | 60 | 364.47 | -4.43 | 0 |  |
| 1 | 77.0 | 70 | 305.11 | -6.36 | 0 |  |
| 1 | 85.5 | 77.7 | 244.75 | -7.85 | 0 |  |
| 1 | 88.0 | 80 | 224.59 | -8.28 | 0 |  |
| 1 | 97.5 | 88.6 | 138 | -9.95 | 0 |  |
| 1 | 99.0 | 90 | 122.89 | -10.21 | 0 |  |
| 1 | 100.0 | 90.9 | 112.59 | -10.38 | 0 |  |
| 1 | 108.25 | 98.4 | 20.97 | -11.83 | 0 |  |
| 1 | 110.0 | 100 | 0 | -12.13 | 0 | 24.29 |
| 2 | 0 | 0 | 0 | 12.15 | 0 | 24.29 |
| 2 | 1.75 | 1.6 | 21.01 | 11.85 | 0 |  |
| 2 | 10.0 | 9.1 | 112.8 | 10.4 | 0 |  |
| 2 | 11.0 | 10 | 123.13 | 10.23 | 0 |  |
| 2 | 12.5 | 11.4 | 138.27 | 9.97 | 0 |  |
| 2 | 22.0 | 20 | 225.06 | 8.3 | 0 |  |
| 2 | 24.5 | 22.3 | 245.27 | 7.87 | 0 |  |
| 2 | 33.0 | 30 | 305.82 | 6.38 | 0 |  |
| 2 | 44.0 | 40 | 365.42 | 4.45 | 0 |  |
| 2 | 55.0 | 50 | 403.83 | -2.53 | 0 |  |
| 2 | 66.0 | 60 | 365.42 | -4.45 | 0 |  |
| 2 | 77.0 | 70 | 305.83 | -6.38 | 0 |  |
| 2 | 85.5 | 77.7 | 245.27 | -7.87 | 0 |  |
| 2 | 88.0 | 80 | 225.06 | -8.3 | 0 |  |
| 2 | 97.5 | 88.6 | 138.27 | -9.97 | 0 |  |
| 2 | 99.0 | 90 | 123.13 | -10.23 | 0 |  |
| 2 | 100.0 | 90.9 | 112.81 | -10.4 | 0 |  |
| 2 | 108.25 | 98.4 | 21.01 | -11.85 | 0 |  |
| 2 | 110.0 | 100 | 0 | -12.15 | 0 | 12.15 |

-Prestress Loads

| Span | Location <br> (ft.) | \%Span | Moment $(\mathrm{k}-\mathrm{ft})$ | Shear <br> (k) | Axial <br> (k) | Reaction (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | -683.1 | 0.02 | -264.38 | 0.02 |
| 1 | 1.75 | 1.6 | -1986.69 | 0.02 | -768.91 |  |
| 1 | 10.0 | 9.1 | -2057.51 | 0.02 | -796.33 |  |
| 1 | 11.0 | 10 | -2187.89 | 0.02 | -844.25 |  |
| 1 | 12.5 | 11.4 | -2374.03 | 0.02 | -912.66 |  |
| 1 | 22.0 | 20 | -2449.38 | 0.02 | -941.51 |  |
| 1 | 24.5 | 22.3 | -2743.38 | 0.02 | -1048.38 |  |
| 1 | 33.0 | 30 | -2796.01 | 0.02 | -1069.07 |  |
| 1 | 44.0 | 40 | -2838.12 | 0.02 | -1085.66 |  |
| 1 | 55.0 | 50 | -2850.72 | 0.02 | -1090.7 |  |
| 1 | 66.0 | 60 | -2830.88 | 0.02 | -1083.03 |  |
| 1 | 77.0 | 70 | -2781.69 | 0.02 | -1063.87 |  |
| 1 | 85.5 | 77.7 | -2723.58 | 0.02 | -1041.19 |  |
| 1 | 88 | 80 | -2430.89 | 0.02 | -934.81 |  |
| 1 | 97.5 | 88.6 | -2352.53 | 0.02 | -904.06 |  |
| 1 | 99.0 | 90 | -2166.55 | 0.02 | -836.21 |  |
| 1 | 100.0 | 90.9 | -2036.39 | 0.02 | -788.69 |  |
| 1 | 108.25 | 98.4 | -1963.5 | 0.02 | -759.88 |  |
| 1 | 110.0 | 100 | -675.87 | 0.02 | -261.58 | -7.24 |
| 2 | 0 | 0 | 117.17 | -7.22 | -261.58 | -7.24 |
| 2 | 1.75 | 1.6 | -1183.04 | -7.22 | -759.88 |  |
| 2 | 10.0 | 9.1 | -1315.27 | -7.22 | -788.7 |  |
| 2 | 11.0 | 10 | -1452.63 | -7.22 | -836.21 |  |
| 2 | 12.5 | 11.4 | -1649.4 | -7.22 | -904.06 |  |
| 2 | 22.0 | 20 | -1796.11 | -7.22 | -934.82 |  |
| 2 | 24.5 | 22.3 | -2106.79 | -7.22 | -1041.2 |  |
| 2 | 33.0 | 30 | -2226.04 | -7.22 | -1063.89 |  |
| 2 | 44.0 | 40 | -2354.37 | -7.22 | -1083.05 |  |
| 2 | 55.0 | 50 | -2453.34 | -7.22 | -1090.73 |  |
| 2 | 66.0 | 60 | -2519.72 | -7.22 | -1085.64 |  |
| 2 | 77.0 | 70 | -2556.75 | -7.22 | -1069.06 |  |
| 2 | 85.5 | 77.7 | -2565.26 | -7.22 | -1048.37 |  |
| 2 | 88.0 | 80 | -2289.25 | -7.22 | -941.5 |  |
| 2 | 97.5 | 88.6 | -2284.53 | -7.22 | -912.66 |  |
| 2 | 99.0 | 90 | -2107.85 | -7.22 | -844.25 |  |
| 2 | 100.0 | 90.9 | -1983.8 | -7.22 | -796.33 |  |
| 2 | 108.25 | 98.4 | -1974.16 | -7.22 | -768.91 |  |
| 2 | 110.0 | 100 | -683.1 | -7.22 | -264.38 | 7.22 |

-Initial Prestress Loads

| Span | Location <br> $(\mathrm{ft})$. | $\%$ Span | Moment <br> $(\mathrm{k}-\mathrm{ft})$ | Shear <br> $(\mathrm{k})$ | Axial <br> $(\mathrm{k})$ | Reaction <br> $(\mathrm{k})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | -752.99 | 0 | -291.43 | 0 |
| 1 | 1.75 | 1.6 | -2393.44 | 0 | -926.32 |  |
| 1 | 10.0 | 9.1 | -2411.31 | 0 | -933.21 |  |
| 1 | 11.0 | 10 | -2585.16 | 0 | -997.43 |  |
| 1 | 12.5 | 11.4 | -2840.93 | 0 | -1091.94 |  |
| 1 | 22.0 | 20 | -2859.89 | 0 | -1099.17 |  |
| 1 | 24.5 | 22.3 | -3275.5 | 0 | -1252.16 |  |
| 1 | 33.0 | 30 | -3288.78 | 0 | -1257.36 |  |
| 1 | 44.0 | 40 | -3299.59 | 0 | -1261.59 |  |
| 1 | 55.0 | 50 | -3303.2 | 0 | -1263 |  |
| 1 | 66.0 | 60 | -3299.61 | 0 | -1261.59 |  |
| 1 | 77.0 | 70 | -3288.81 | 0 | -1257.36 |  |
| 1 | 85.5 | 77.7 | -3275.55 | 0 | -1252.16 |  |
| 1 | 88.0 | 80 | -2859.95 | 0 | -1099.17 |  |
| 1 | 97.5 | 88.6 | -2841.57 | 0 | -1091.94 |  |
| 1 | 99.0 | 90 | -2585.15 | 0 | -997.43 |  |
| 1 | 100.0 | 90.9 | -2410.88 | 0 | -933.21 |  |
| 1 | 108.25 | 98.4 | -2393.5 | 0 | -926.32 |  |
| 2 | 110.0 | 100 | -752.99 | 0 | -291.43 | -8.03 |
| 2 | 0 | 0 | 130.53 | -8.03 | -291.43 | -8.03 |
| 2 | 99.0 | 90 | -2496.8 | -8.03 | -997.43 |  |
| 2 | 100.0 | 90.9 | -2330.56 | -8.03 | -933.21 |  |
| 2 | 108.25 | 98.4 | -2379.45 | -8.03 | -926.32 |  |
| 2 | 110.0 | 100 | -752.99 | -8.03 | -291.43 | 8.03 |
| 2 | 10.0 | 9.0 | 10 | -1789.97 | -8.03 | -997.43 |

## Composite Effects

## -Parapets

| Span | Location <br> (ft.) | \%Span | Moment <br> (k-ft) | Shear <br> (k) | Axial <br> (k) | Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 8.91 | 0 | 8.91 |
| 1 | 1.75 | 1.6 | 15.26 | 8.53 | 0 |  |
| 1 | 10.0 | 9.1 | 78.29 | 6.75 | 0 |  |
| 1 | 11.0 | 10 | 84.94 | 6.53 | 0 |  |
| 1 | 12.5 | 11.4 | 94.5 | 6.21 | 0 |  |
| 1 | 22.0 | 20 | 143.74 | 4.16 | 0 |  |
| 1 | 24.5 | 22.3 | 153.46 | 3.62 | 0 |  |
| 1 | 33.0 | 30 | 176.41 | 1.78 | 0 |  |
| 1 | 44.0 | 40 | 182.95 | -0.59 | 0 |  |
| 1 | 55.0 | 50 | 163.35 | -2.97 | 0 |  |
| 1 | 66.0 | 60 | 117.61 | -5.35 | 0 |  |
| 1 | 77.0 | 70 | 45.74 | -7.72 | 0 |  |
| 1 | 85.5 | 77.7 | -27.7 | -9.56 | 0 |  |
| 1 | 88.0 | 80 | -52.27 | -10.1 | 0 |  |
| 1 | 97.5 | 88.6 | -157.95 | -12.15 | 0 |  |
| 1 | 99.0 | 90 | -176.42 | -12.47 | 0 |  |
| 1 | 100.0 | 90.9 | -189 | -12.69 | 0 |  |
| 1 | 108.25 | 98.4 | -301.04 | -14.47 | 0 |  |
| 1 | 110.0 | 100 | -326.7 | -14.85 | 0 | 29.7 |
| 2 | 0 | 0 | -326.7 | 14.85 | 0 | 29.7 |
| 2 | 1.75 | 1.6 | -301.04 | 14.47 | 0 |  |
| 2 | 10.0 | 9.1 | -189 | 12.69 | 0 |  |
| 2 | 11.0 | 10 | -176.42 | 12.47 | 0 |  |
| 2 | 12.5 | 11.4 | -157.95 | 12.15 | 0 |  |
| 2 | 22.0 | 20 | -52.27 | 10.1 | 0 |  |
| 2 | 24.5 | 22.3 | -27.7 | 9.56 | 0 |  |
| 2 | 33.0 | 30 | 45.74 | 7.72 | 0 |  |
| 2 | 44.0 | 40 | 117.61 | 5.35 | 0 |  |
| 2 | 55.0 | 50 | 163.35 | 2.97 | 0 |  |
| 2 | 66.0 | 60 | 182.95 | 0.59 | 0 |  |
| 2 | 77.0 | 70 | 176.42 | -1.78 | 0 |  |
| 2 | 85.5 | 77.7 | 153.47 | -3.62 | 0 |  |
| 2 | 88.0 | 80 | 143.75 | -4.16 | 0 |  |
| 2 | 97.5 | 88.6 | 94.5 | -6.21 | 0 |  |
| 2 | 99.0 | 90 | 84.94 | -6.53 | 0 |  |
| 2 | 100.0 | 90.9 | 78.3 | -6.75 | 0 |  |
| 2 | 108.25 | 98.4 | 15.26 | -8.53 | 0 |  |
| 2 | 110.0 | 100 | 0 | -8.91 | 0 | 8.91 |

-Future Wearing Surface

| Span | Location <br> (ft.) | \%Span | Moment <br> (k-ft) | Shear <br> (k) | Axial <br> (k) | Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 10.73 | 0 | 10.73 |
| 1 | 1.75 | 1.6 | 18.37 | 10.27 | 0 |  |
| 1 | 10.0 | 9.1 | 94.24 | 8.13 | 0 |  |
| 1 | 11.0 | 10 | 102.24 | 7.87 | 0 |  |
| 1 | 12.5 | 11.4 | 113.74 | 7.48 | 0 |  |
| 1 | 22.0 | 20 | 173.03 | 5.01 | 0 |  |
| 1 | 24.5 | 22.3 | 184.72 | 4.36 | 0 |  |
| 1 | 33.0 | 30 | 212.35 | 2.15 | 0 |  |
| 1 | 44.0 | 40 | 220.22 | -0.71 | 0 |  |
| 1 | 55.0 | 50 | 196.62 | -3.57 | 0 |  |
| 1 | 66.0 | 60 | 141.57 | -6.43 | 0 |  |
| 1 | 77.0 | 70 | 55.05 | -9.29 | 0 |  |
| 1 | 85.5 | 77.7 | -33.35 | -11.5 | 0 |  |
| 1 | 88.0 | 80 | -62.92 | -12.15 | 0 |  |
| 1 | 97.5 | 88.6 | -190.12 | -14.62 | 0 |  |
| 1 | 99.0 | 90 | -212.35 | -15.01 | 0 |  |
| 1 | 100.0 | 90.9 | -227.5 | -15.27 | 0 |  |
| 1 | 108.25 | 98.4 | -362.36 | -17.42 | 0 |  |
| 1 | 110.0 | 100 | -393.25 | -17.87 | 0 | 35.75 |
| 2 | 0 | 0 | -393.25 | 17.87 | 0 | 35.75 |
| 2 | 1.75 | 1.6 | -362.36 | 17.42 | 0 |  |
| 2 | 10.0 | 9.1 | -227.5 | 15.27 | 0 |  |
| 2 | 11.0 | 10 | -212.35 | 15.01 | 0 |  |
| 2 | 12.5 | 11.4 | -190.12 | 14.62 | 0 |  |
| 2 | 22.0 | 20 | -62.92 | 12.15 | 0 |  |
| 2 | 24.5 | 22.3 | -33.34 | 11.5 | 0 |  |
| 2 | 33.0 | 30 | 55.06 | 9.29 | 0 |  |
| 2 | 44.0 | 40 | 141.57 | 6.43 | 0 |  |
| 2 | 55.0 | 50 | 196.63 | 3.57 | 0 |  |
| 2 | 66.0 | 60 | 220.22 | 0.71 | 0 |  |
| 2 | 77.0 | 70 | 212.35 | -2.15 | 0 |  |
| 2 | 85.5 | 77.7 | 184.73 | -4.36 | 0 |  |
| 2 | 88.0 | 80 | 173.03 | -5.01 | 0 |  |
| 2 | 97.5 | 88.6 | 113.75 | -7.48 | 0 |  |
| 2 | 99.0 | 90 | 102.24 | -7.87 | 0 |  |
| 2 | 100.0 | 90.9 | 94.25 | -8.13 | 0 |  |
| 2 | 108.25 | 98.4 | 18.37 | -10.27 | 0 |  |
| 2 | 110.0 | 100 | 0 | -10.73 | 0 | 10.73 |

-Live Load - Axle

| Span | Location <br> (ft.) | \%Span | Positive <br> Moment $(\mathrm{k}-\mathrm{ft})$ | Negative Moment $(\mathrm{k}-\mathrm{ft})$ | Positive Shear <br> (k) | Negative Shear <br> (k) | Positive Axial <br> (k) | Negative Axial <br> (k) | Positive Reaction <br> (k) | Negative Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 82.58 | -8.68 | 0 | 0 | 82.58 | -8.68 |
| 1 | 1.75 | 1.6 | 114.9 | -12.42 | 81.25 | -8.68 | 0 | 0 |  |  |
| 1 | 10.0 | 9.1 | 590.15 | -71.02 | 72.04 | -8.68 | 0 | 0 |  |  |
| 1 | 11.0 | 10 | 639.51 | -78.12 | 72.04 | -8.68 | 0 | 0 |  |  |
| 1 | 12.5 | 11.4 | 711.33 | -88.78 | 69.76 | -8.68 | 0 | 0 |  |  |
| 1 | 22.0 | 20 | 1085.74 | -156.27 | 60.77 | -13.28 | 0 | 0 |  |  |
| 1 | 24.5 | 22.3 | 1158.79 | -174.02 | 57.47 | -16.36 | 0 | 0 |  |  |
| 1 | 33.0 | 30 | 1342.86 | -234.4 | 49.91 | -23.97 | 0 | 0 |  |  |
| 1 | 44.0 | 40 | 1454.58 | -312.55 | 39.59 | -35.15 | 0 | 0 |  |  |
| 1 | 55.0 | 50 | 1426.41 | -390.69 | 29.95 | -45.9 | 0 | 0 |  |  |
| 1 | 66.0 | 60 | 1275.16 | -468.83 | 21.14 | -56.06 | 0 | 0 |  |  |
| 1 | 77.0 | 70 | 998.84 | -546.97 | 13.29 | -65.51 | 0 | 0 |  |  |
| 1 | 85.5 | 77.7 | 721.36 | -607.35 | 7.99 | -72.45 | 0 | 0 |  |  |
| 1 | 88.0 | 80 | 630.85 | -625.11 | 6.82 | -74.09 | 0 | 0 |  |  |
| 1 | 97.5 | 88.6 | 267.94 | -692.6 | 2.52 | -80.97 | 0 | 0 |  |  |
| 1 | 99.0 | 90 | 210.54 | -703.25 | 2.25 | -81.67 | 0 | 0 |  |  |
| 1 | 100.0 | 90.9 | 172.66 | -710.35 | 1.99 | -82.37 | 0 | 0 |  |  |
| 1 | 108.25 | 98.4 | 28.13 | -768.96 | 0.32 | -86.92 | 0 | 0 |  |  |
| 1 | 110.0 | 100 | 0 | -781.39 | 0 | -88.11 | 0 | 0 | 92.2 | 0 |
| 2 | 0 | 0 | 0 | -781.39 | 88.11 | 0 | 0 | 0 | 92.2 | 0 |
| 2 | 1.75 | 1.6 | 28.13 | -768.95 | 86.92 | -0.32 | 0 | 0 |  |  |
| 2 | 10.0 | 9.1 | 172.66 | -710.34 | 82.37 | -1.99 | 0 | 0 |  |  |
| 2 | 11.0 | 10 | 210.54 | -703.24 | 81.67 | -2.25 | 0 | 0 |  |  |
| 2 | 12.5 | 11.4 | 267.94 | -692.59 | 80.97 | -2.52 | 0 | 0 |  |  |
| 2 | 22.0 | 20 | 630.85 | -625.1 | 74.09 | -6.82 | 0 | 0 |  |  |
| 2 | 24.5 | 22.3 | 721.36 | -607.34 | 72.45 | -7.99 | 0 | 0 |  |  |
| 2 | 33.0 | 30 | 998.85 | -546.96 | 65.51 | -13.29 | 0 | 0 |  |  |
| 2 | 44.0 | 40 | 1275.17 | -468.83 | 56.06 | -21.14 | 0 | 0 |  |  |
| 2 | 55.0 | 50 | 1426.43 | -390.69 | 45.9 | -29.95 | 0 | 0 |  |  |
| 2 | 66.0 | 60 | 1454.6 | -312.55 | 35.15 | -39.59 | 0 | 0 |  |  |
| 2 | 77.0 | 70 | 1342.88 | -234.41 | 23.97 | -49.91 | 0 | 0 |  |  |
| 2 | 85.5 | 77.7 | 1158.81 | -174.03 | 16.36 | -57.47 | 0 | 0 |  |  |
| 2 | 88.0 | 80 | 1085.76 | -156.28 | 13.28 | -60.77 | 0 | 0 |  |  |
| 2 | 97.5 | 88.6 | 711.36 | -88.79 | 8.68 | -69.76 | 0 | 0 |  |  |
| 2 | 99.0 | 90 | 639.54 | -78.14 | 8.68 | -72.04 | 0 | 0 |  |  |
| 2 | 100.0 | 90.9 | 590.18 | -71.03 | 8.68 | -72.04 | 0 | 0 |  |  |
| 2 | 108.25 | 98.4 | 114.9 | -12.43 | 8.68 | -81.25 | 0 | 0 |  |  |
| 2 | 110.0 | 100 | 0 | 0 | 8.68 | -82.58 | 0 | 0 | 82.58 | -8.68 |

-Live Load - Truck Pair

| Span | Location <br> (ft.) | \%Span | Positive Moment (k-ft) | Negative Moment $(\mathrm{k}-\mathrm{ft})$ | Positive Shear $\qquad$ | Negative Shear (k) | Positive Axial $\qquad$ | Negative Axial (k) | Positive Reaction (k) | Negative Reaction (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1.75 | 1.6 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 10.0 | 9.1 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 11.0 | 10 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 12.5 | 11.4 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 22.0 | 20 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 24.5 | 22.3 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 33.0 | 30 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 44.0 | 40 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 55.0 | 50 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 66.0 | 60 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 77.0 | 70 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 85.5 | 77.7 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 88.0 | 80 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 97.5 | 88.6 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 99.0 | 90 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 100.0 | 90.9 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 108.25 | 98.4 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 1 | 110.0 | 100 | 0 | -1561.47 | 0 | 0 | 0 | 0 | 153.7 | 0 |
| 2 | 0 | 0 | 0 | -1561.47 | 0 | 0 | 0 | 0 | 153.7 | 0 |
| 2 | 1.75 | 1.6 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 10.0 | 9.1 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 11.0 | 10 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 12.5 | 11.4 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 22.0 | 20 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 24.5 | 22.3 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 33.0 | 30 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 44.0 | 40 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 55.0 | 50 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 66.0 | 60 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 77.0 | 70 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 85.5 | 77.7 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 88.0 | 80 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 97.5 | 88.6 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 99.0 | 90 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 100.0 | 90.9 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 108.25 | 98.4 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| 2 | 110.0 | 100 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

-Live Load - Lane

| Span | Location <br> (ft.) | \%Span | Positive <br> Moment $(\mathrm{k}-\mathrm{ft})$ | Negative Moment (k-ft) | Positive Shear (k) | Negative Shear <br> (k) | Positive <br> Axial <br> (k) | Negative Axial <br> (k) | Positive <br> Reaction <br> (k) | Negative Reaction <br> (k) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 29.97 | -4.28 | 0 | 0 | 29.97 | -4.28 |
| 1 | 1.75 | 1.6 | 42.04 | -6.12 | 28.95 | -4.29 | 0 | 0 |  |  |
| 1 | 10.0 | 9.1 | 219.67 | -35.02 | 23.82 | -4.67 | 0 | 0 |  |  |
| 1 | 11.0 | 10 | 238.84 | -38.52 | 23.82 | -4.67 | 0 | 0 |  |  |
| 1 | 12.5 | 11.4 | 266.59 | -43.77 | 22.62 | -4.85 | 0 | 0 |  |  |
| 1 | 22.0 | 20 | 416.06 | -77.05 | 18.18 | -5.92 | 0 | 0 |  |  |
| 1 | 24.5 | 22.3 | 447.72 | -85.8 | 16.66 | -6.46 | 0 | 0 |  |  |
| 1 | 33.0 | 30 | 531.63 | -115.57 | 13.39 | -8.01 | 0 | 0 |  |  |
| 1 | 44.0 | 40 | 585.57 | -154.1 | 9.42 | -10.92 | 0 | 0 |  |  |
| 1 | 55.0 | 50 | 577.87 | -192.63 | 6.22 | -14.61 | 0 | 0 |  |  |
| 1 | 66.0 | 60 | 508.52 | -231.16 | 3.77 | -19.04 | 0 | 0 |  |  |
| 1 | 77.0 | 70 | 377.54 | -269.68 | 1.99 | -24.15 | 0 | 0 |  |  |
| 1 | 85.5 | 77.7 | 234.1 | -299.45 | 1.01 | -28.68 | 0 | 0 |  |  |
| 1 | 88.0 | 80 | 184.91 | -308.21 | 0.82 | -29.87 | 0 | 0 |  |  |
| 1 | 97.5 | 88.6 | 50.03 | -422.53 | 0.23 | -35.47 | 0 | 0 |  |  |
| 1 | 99.0 | 90 | 37.65 | -453.74 | 0.19 | -36.12 | 0 | 0 |  |  |
| 1 | 100.0 | 90.9 | 30.54 | -476.31 | 0.15 | -36.77 | 0 | 0 |  |  |
| 1 | 108.25 | 98.4 | 0.85 | -710.81 | 0.01 | -41.44 | 0 | 0 |  |  |
| 1 | 110.0 | 100 | 0 | -770.52 | 0 | -42.81 | 0 | 0 | 85.62 | 0 |
| 2 | 0 | 0 | 0 | -770.52 | 42.81 | 0 | 0 | 0 | 85.62 | 0 |
| 2 | 1.75 | 1.6 | 0.85 | -710.81 | 41.44 | -0.01 | 0 | 0 |  |  |
| 2 | 10.0 | 9.1 | 30.54 | -476.31 | 36.77 | -0.15 | 0 | 0 |  |  |
| 2 | 11.0 | 10 | 37.65 | -453.74 | 36.12 | -0.19 | 0 | 0 |  |  |
| 2 | 12.5 | 11.4 | 50.02 | -422.53 | 35.47 | -0.23 | 0 | 0 |  |  |
| 2 | 22.0 | 20 | 184.91 | -308.21 | 29.87 | -0.82 | 0 | 0 |  |  |
| 2 | 24.5 | 22.3 | 234.1 | -299.45 | 28.68 | -1.01 | 0 | 0 |  |  |
| 2 | 33.0 | 30 | 377.54 | -269.68 | 24.15 | -1.99 | 0 | 0 |  |  |
| 2 | 44.0 | 40 | 508.53 | -231.15 | 19.04 | -3.77 | 0 | 0 |  |  |
| 2 | 55.0 | 50 | 577.87 | -192.63 | 14.61 | -6.22 | 0 | 0 |  |  |
| 2 | 66.0 | 60 | 585.58 | -154.1 | 10.92 | -9.42 | 0 | 0 |  |  |
| 2 | 77.0 | 70 | 531.64 | -115.58 | 8.01 | -13.39 | 0 | 0 |  |  |
| 2 | 85.5 | 77.7 | 447.74 | -85.81 | 6.46 | -16.66 | 0 | 0 |  |  |
| 2 | 88.0 | 80 | 416.07 | -77.05 | 5.92 | -18.18 | 0 | 0 |  |  |
| 2 | 97.5 | 88.6 | 266.6 | -43.78 | 4.85 | -22.62 | 0 | 0 |  |  |
| 2 | 99.0 | 90 | 238.85 | -38.52 | 4.67 | -23.82 | 0 | 0 |  |  |
| 2 | 100.0 | 90.9 | 219.69 | -35.02 | 4.67 | -23.82 | 0 | 0 |  |  |
| 2 | 108.25 | 98.4 | 42.05 | -6.13 | 4.29 | -28.95 | 0 | 0 |  |  |
| 2 | 110.0 | 100 | 0 | 0 | 4.28 | -29.97 | 0 | 0 | 29.97 | -4.28 |

Section A5 - Comparison Between the Hand Calculations and the Two Computer Programs
Moment Comparison

| Method | Location | Girder | Slab, Haunch and Ext. Diaphragm | Parapets | FWS | $\underset{\substack{\text { Positive } \\ \text { LL } \\ \text { (3) }}}{ }$ | Negative LL ${ }^{(4)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (ft.) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) | (k-ft) |
| Opis |  | $615.5{ }^{(1)}$ | $649.8{ }^{(1)}$ | 84.9 | 102.2 | 878.4 | - |
| Qcon | 11 | (5) | - ${ }^{5}$ | - | 114.0 | 909.3 | - |
| Table 5.3 |  | $656.0^{(2)}$ | $643.0{ }^{(2)}$ | 85.0 | 114.0 | 886.0 | - |
| Opis |  | 1,709.5 ${ }^{(1)}$ | 1,864.8 ${ }^{(1)}$ | 163.4 | 196.6 | 2004.3 | - |
| QCon | 55 | - |  | - | 219.3 | 2,063.0 | - |
| Table 5.3 |  | 1,725.0 ${ }^{(2)}$ | 1,832.0 ${ }^{(2)}$ | 164.0 | 220.0 | 2,010.0 | - |
| Opis |  | 0 | 0 | -326.7 | -393.3 | - | -2,098.8 |
| QCon | ~ 110 | - | - | - | -438.6 | - | -2,096.9 |
| Table 5.3 |  | 0 | 0 | -326.0 | -438.0 |  | -2,095.0 |

## Shear Comparison

| Method | Location | Girder | Slab, Haunch and Ext. Diaphragm | Parapets | FWS | Positive $\mathrm{LL}^{(3)}$ | Negative LL ${ }^{(4)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (ft.) | (k) | (k) | (k) | (k) | (k) | (k) |
| Opis |  | $49.7{ }^{(1)}$ | $52.8{ }^{(1)}$ | 6.5 | 7.9 | 95.9 | -14.9 |
| QCon | 11 | (5) | (5) |  | 8.8 | 99.4 | -13.0 |
| Table 5.3 |  | $49.2{ }^{(2)}$ | $52.2{ }^{(2)}$ | 6.5 | 8.8 | 95.5 | -13.4 |
| Opis |  | $0{ }^{(1)}$ | $-2.5{ }^{(1)}$ | -3.0 | -3.6 | 36.2 | -60.5 |
| QCon | 55 | - | - | - | -4.0 | 36.7 | -61.7 |
| Table 5.3 |  | $-0.6{ }^{(2)}$ | $-3.1^{(2)}$ | -3.0 | -4.0 | 36.2 | -61.2 |
| Opis |  | 0 | 0 | -14.9 | -17.9 | 0 | -130.9 |
| QCon | - 110 | - | - | - | -19.9 | 0 | -132.1 |
| Table 5.3 |  | 0 | 0 | -14.8 | -19.9 | 0 | -131.1 |

## Notes:

1- Calculated based on a 110 ft simple span length and the force effects are calculated at the distance shown in the table measured from the centerline of the abutment neoprene pads.
2- Calculated based on a 109 ft simple span length (distance between the centerline of the neoprene pads) and the force effects are calculated at the distance shown in the table measured from the centerline of the abutment neoprene pads.
3- Truck + Lane including impact
4- 0.90(Truck Pair + Lane including impact) as specified in S3.6.1.3.1
5- QConBridge does not apply the noncomposite loads to the simple span girder, the program applies the girder, slab, haunch and diaphragm loads to the continuous girder, therefore, these results are not comparable.

## Section A6 - Flexural Resistance Sample Calculation from Opis to Compare with Hand Calculations

The following is sample Opis output for flexure at 55 ft . and 110 ft . from the end bearing. These results may be compared to the hand calculations in Design Step 5.6 for the positive and negative regions.

Positive Bending Region

```
PERFORMING AASHTO LRFD SPECIFICATION CHECKS - 5.7.3.2 Flexural Resistance
    Point of Interest : 105.00 (55.0 ft.)
    Construction Stage: 2
    Prestress Summary:
        dp = 74.502 in (from top)
        Aps = 6.732 in^2
        fps = 264.532 ksi (avg. for all rows)
        POSITIVE Flexural Resistance:
\begin{tabular}{|c|c|c|c|c|c|}
\hline Layer & Area, in^2 & ** Analyzed Stress, ksi & a RECTANGULAR Force, kips & Section ** Lever-Arm, in & Moment i, in-k \\
\hline CS & 507.832 & \(-0.85 * \mathrm{f}^{\prime} \mathrm{C}\) & -1726.627 & 3.095 & 5343.728 \\
\hline RT & 2.000 & -32.515 & -65.029 & 2.132 & 138.670 \\
\hline RB & 3.720 & 2.911 & 10.828 & -0.180 & 1.950 \\
\hline PS11 & 0.612 & 264.145 & 161.657 & -64.118 & 10365.045 \\
\hline PS10 & 0.918 & 264.309 & 242.636 & -66.118 & 16042.478 \\
\hline PS 9 & 0.306 & 264.464 & 80.926 & -68.118 & 5512.478 \\
\hline PS 8 & 0.306 & 264.464 & 80.926 & -68.118 & 5512.478 \\
\hline PS 7 & 0.918 & 264.464 & 242.778 & -68.118 & 16537.434 \\
\hline PS 6 & 0.306 & 264.610 & 80.971 & -70.118 & 5677.476 \\
\hline PS 5 & 0.306 & 264.610 & 80.971 & -70.118 & 5677.476 \\
\hline PS 4 & 1.224 & 264.610 & 323.883 & -70.118 & 22709.904 \\
\hline PS 3 & 0.306 & 264.750 & 81.013 & -72.118 & 5842.487 \\
\hline PS 2 & 0.306 & 264.750 & 81.013 & -72.118 & 5842.487 \\
\hline PS 1 & 1.224 & 264.750 & 324.053 & -72.118 & 23369.949 \\
\hline
\end{tabular}
Flexural Resistance Summary:
\begin{tabular}{lll} 
beta 1 & \(=\) & 0.850 \\
c & \(=\) & 5.382 in \\
a & \(=\) & 4.575 in (from top) \\
\(\mathrm{f}^{\prime} \mathrm{c}\) & \(=4.000 \mathrm{ksi}\) (slab)
\end{tabular}
```



```
                                    Mn = 128574.031 in-k
    f'c = 4.000 ksi (slab)
(COMPARED TO 10,697 ft-k from hand calculations)
```

```
Effective Shear Depth: [AASHTO LRFD 5.8.2.7]
```

Effective Shear Depth: [AASHTO LRFD 5.8.2.7]
Tensile Force = 1791.655 kips
Tensile Force = 1791.655 kips
dv = Mn / Tensile Force = 71.763 in
dv = Mn / Tensile Force = 71.763 in
Tensile Capacity of Reinforcement on Flexural Tension Side: [AASHTO 5.8.3.5]
Tensile Capacity of Reinforcement on Flexural Tension Side: [AASHTO 5.8.3.5]
Rebar = 0.000 kips
Rebar = 0.000 kips
P/S = 1780.827 kips
P/S = 1780.827 kips
T(Cap) = 1780.827 kips

```
    T(Cap) = 1780.827 kips
```

```
Layer Codes:
    => C_ : C = Concrete, where _ may be:
                        S = Slab, TF = Top Flange, W = Web, BF = Bottom Flange,
                            ^T = Top fillets and tapers, ^B = Bottom fillets and tapers
    => R_ : R = Reinforcement, where _ is the row number (1-5, B (bottom), T (top))
    => PS__ : PS = Prestress, where _ is the row number
Notes:
    => The flexural resistance is determined based on:
        * Equilibrium
        * Strain compatibility
        * Strain in extreme compressive concrete fiber is 0.003
    => The stress in the mild compression steel includes an adjustment for
        the displaced concrete. fs = (es * Es) + (0.85 f'c ABS(es / ey))
```


## Negative Bending Region

```
PERFORMING AASHTO LRFD SPECIFICATION CHECKS - 5.7.3.2 Flexural Resistance
    Point of Interest : 110.00 (110.0 ft.)
    Construction Stage: 2
    NEGATIVE Flexural Resistance:
```



```
Flexural Resistance Summary:
    beta 1= 0.750 phi f = 0.900
    c = 7.590 in Mn = 62822.840 in-k
    a = 5.692 in (from bottom)
\begin{tabular}{rlrl}
Mn & \(=\) & 62822.840 & \(\mathrm{in}-\mathrm{k}\) \\
& \(=\) & 5235.237 & \(\mathrm{ft}-\mathrm{k}\)
\end{tabular}
phi*Mn = 56540.555 in-k
    [AASHTO LRFD (5.7.3.2.1-1)]
                                    4711.713 ft-k
    f'c = 6.000 ksi (flange)
    f'c = 6.000 ksi (stem)
Effective Shear Depth: [AASHTO LRFD 5.8.2.7]
    Tensile Force = 871.200 kips
    dv = Mn / Tensile Force = 72.111 in
Tensile Capacity of Reinforcement on Flexural Tension Side: [AASHTO 5.8.3.5]
    Rebar = 871.200 kips
    T(Cap) = 871.200 kips
Layer Codes:
    => C_ : C = Concrete, where _ may be:
                        S = Slab, TF = Top Flange, W = Web, BF = Bottom Flange,
                        ^T = Top fillets and tapers, ^B = Bottom fillets and tapers
    => R_ : R = Reinforcement, where _ is the row number (1-5, B (bottom), T (top))
    => PS_ : PS = Prestress, where _ is the row number
Notes:
    => The flexural resistance is determined based on:
        * Equilibrium
        * Strain compatibility
        * Strain in extreme compressive concrete fiber is 0.003
    => The stress in the mild compression steel includes an adjustment for
            the displaced concrete. fs = (es * Es) + (0.85 f'c ABS(es / ey))
```


## Appendix B

GENERAL GUIDELINES FOR REFINED ANALYSIS OF DECK SLABS


#### Abstract

Traditionally, deck slabs have been analyzed using approximate methods. The approximate methods are based on calculating moments per unit width of the deck and design the reinforcement to resist these moments. This approach has been used successfully for many decades. However, the approximate methods were generally based on laboratory testing and/or refined analysis of typical decks supported on parallel girders and no skews. In case of deck slabs with unusual geometry, such as sharply skewed decks, the results of the approximate methods may not be accurate. For example, negative moments may develop at the acute corner of a sharply skewed deck. These moments are not accounted for in the approximate methods as they rely on assuming that the deck is behaving as a continuous beam.


In cases of unusual deck geometry, bridge designers may find it beneficial to employ refined methods of analysis. Typically the use of the refined methods of analysis is meant for the design of both of the girders and the deck slab. The design method of analysis most used is the finite element analysis. However, for deck slabs, other methods such as the yield line method and the finite differences method may be used. Following is a general description of the use of the finite elements in analyzing deck slabs.

## Finite element modeling of decks

## Type of elements

The finite element method is based on dividing a component into a group of small components or "finite elements". Depending on the type of the element, the number of displacements (translations and rotations) varies at each end or corner of the element varies. The displacements are typically referred to as 'degrees of freedom". The basic output of the analysis is the displacements at each node. These displacements are then converted into forces at the nodes. The force output corresponding to a rotational degrees of freedom is in the form of a moment while forces correspond to translational degrees of freedom. Following are the types of elements typically used to model a plate structure and the advantage and disadvantages of each type.

Plate elements: Plate elements are developed assuming that the thickness of the plate component is small relative to the other two dimensions. The plate is modeled by its middle surface. Each element typically has four corners or nodes. Most computer programs have the ability of handling three-node or triangular plate elements, which are typically treated as a special case of the fournode basic element. Following the general plate theory, plate elements are assumed have three allowed displacements at each node; translation perpendicular to the plate and rotations about two perpendicular axes in the plane of the plate. The typical output includes the moments (usually given as moment per unit width of the face of the elements) and the shear in the plate. This form of output is convenient because the moments may be directly used to design the deck.

The main disadvantage of plate elements is that they do not account for the forces in the plane of the plate. This results in ignoring the stiffness of the plate elements in this plane. This precludes them from being used as part of a three-dimensional model to analyze both the deck and the girders.

The deck supports are modeled as rigid supports along the lines of the supporting components, i.e. girders, diaphragms and/or floor beams. Where it is desirable to consider the effect of the flexibility of the supporting components on the deck moments, the model may include these components that are typically modeled as beams. As the plate elements, theoretically, have no inplane stiffness, the effect of the composite action on the stiffness of the beams should be considered when determining the stiffness of the beam elements.

Shell elements: Shell elements are also developed assuming that the thickness of the component is small relative to the other two dimensions and are also modeled by their middle surface. They differ from plate elements in that they are considered to have six degrees of freedom at each node, three translations and three rotations. Typically the rotation about the axis perpendicular to the surface at a node is eliminated leaving only five degrees of freedom per node. Shell elements may be used to model two dimensional (plate) components or three-dimensional (shell) components. Commercially available computer programs typically allow three-node and four-node elements. The typical output includes the moments (usually given as moment per unit width of the face of the elements) and the shear and axial loads in the element. This form of output is convenient because the moments may be directly used to design the deck.

Due to the inclusion of the translations in the plane of the elements, shell elements may be used as part of a three-dimensional model to analyze both the deck and the girders. When the supporting components are modeled using beam elements, only the stiffness of the noncomposite beams is introduced when defining the stiffness of the beams. The effect of the composite action between the deck and the supporting components is automatically included due to the presence of the inplane stiffness of the shell elements representing the deck.

Solid elements: Solid elements may be used to model both thin and thick components. The thickness of the component may be divided into several layers or, for thin components such as decks, may be modeled using one layer. The solid elements are developed assuming three translations at each node and the rotations are not considered in the development. The typical output includes the forces in the direction of the three degrees of freedom at the nodes. Most computer programs have the ability to determine the surface stresses of the solid elements. This form of output is not convenient because these forces or stresses need to be converted to moments that may be used to design the deck. Notice that, theoretically, there should be no force perpendicular to the free surface of an element. However, due to rounding off errors, a small force is typically calculated.

Similar to shell elements, due to the inclusion of all translations in the development of the elements, solid elements may be used as part of a three-dimensional model to analyze both the deck and the girders. When the supporting components are modeled using beam elements, only the stiffness of the noncomposite beams is introduced when defining the stiffness of the beams.

Element size and aspect ratio: The accuracy of the results of a finite element model increases as the element size decreases. The required size of elements is smaller at areas where high loads exist such as location of applied concentrated loads and reactions. For a deck slab, the dividing the width between the girders to five or more girders typically yields accurate results. The aspect ratio of the element (length-
to-width ratio for plate and shell elements and longest-to-shortest side length ratio for solid elements) and the corner angles should be kept within the values recommended by the developer of the computer program. Typically an aspect ratio less than 3 and corner angles between 60 and 120 degrees are considered acceptable. In case the developer recommendations are not bllowed, the inaccurate results are usually limited to the nonconformant elements and the surrounding areas. When many of the elements do not conform to the developer recommendation, it is recommended that a finer model be developed and the results of the two models compared. If the difference is within the acceptable limits for design, the coarser model may be used. If the difference is not acceptable, a third, finer model should be developed and the results are then compared to the previous model. This process should be repeated until the difference between the results of the last two models is within the acceptable limits.

For deck slabs with constant thickness, the results are not very sensitive to element size and aspect ratio.
Load application: Local stress concentrations take place at the locations of concentrated loads applied to a finite element model. For a bridge deck, wheel loads should preferably be applied as uniform load distributed over the tire contact area specified in Article S3.6.1.2.5. To simplify live load application to the deck model, the size of the elements should be selected to eliminate the partial loading of some finite elements, i.e. the tire contact area preferably match the area of one or a group of elements.


Design Step C1.2

Calculate the creep coefficient, $\Psi_{(\mathrm{t}, \mathrm{ti})}$, for the beam at infinite time according to S5.4.2.3.2.

Calculate the concrete strength factor, $\mathrm{k}_{\mathrm{f}}$

$$
\begin{align*}
\mathrm{k}_{\mathrm{f}} & =1 /\left[0.67+\left(\mathrm{f}_{\mathrm{c}} / 9\right)\right]  \tag{S5.4.2.3.2-2}\\
& =1 /[0.67+(6.0 / 9)] \\
& =0.748
\end{align*}
$$

Calculate the volume to surface area factor, $\mathrm{k}_{\mathrm{c}}$

$$
\begin{equation*}
\mathrm{k}_{\mathrm{c}}=\left[\frac{\left(\frac{\mathrm{t}}{26 \mathrm{e}^{0.36(V / S)_{\mathrm{b}}}+\mathrm{t}}\right)}{\left(\frac{\mathrm{t}}{45+\mathrm{t}}\right)}\right]\left[\frac{1.80+1.77 \mathrm{e}^{-0.54(\mathrm{~V} /)_{\mathrm{b}}}}{2.587}\right] \tag{SC5.4.2.3.2-1}
\end{equation*}
$$

where:
$\begin{aligned} \mathrm{t} & =\text { maturity of concrete } \\ & =\text { infinite days }\end{aligned}$
$\mathrm{e}=$ natural log base (approx. 2.71828)

$$
\begin{aligned}
(\mathrm{V} / \mathrm{S})_{\mathrm{b}}= & \text { volume to surface ratio for the beam } \\
& =\text { beam surface area is } 2,955.38 \mathrm{in}^{2} / \mathrm{ft}(\text { see Figure } 2-3 \text { for beam } \\
& \text { dimensions) and the volume is } 13,020 \mathrm{in}^{3} / \mathrm{ft} \\
= & (13,020 / 2,955.38) \\
& =4.406 \mathrm{in} .
\end{aligned}
$$

The creep coefficient is the ratio between creep strain and the strain due to permanent stress (SC5.4.2.3.2)

Calculate creep coefficient according to Eq. S5.4.2.3.2-1.

$$
\psi_{(\infty, 1)}=3.5 \mathrm{k}_{\mathrm{c}} \mathrm{k}_{\mathrm{f}}(1.58-\mathrm{H} / 120) \mathrm{t}_{\mathrm{i}}^{-0.118}\left[\left(\mathrm{t}-\mathrm{t}_{\mathrm{i}}\right)^{0.6} /\left(10.0+\left(\mathrm{t}-\mathrm{t}_{\mathrm{i}}\right)^{0.6}\right]\right.
$$

where:

$$
\begin{aligned}
\mathrm{k}_{\mathrm{c}} & =0.759 \text { (see above) } \\
\mathrm{k}_{\mathrm{f}} & =0.748 \text { (see above) } \\
\mathrm{H} & =\text { relative humidity } \\
& =70 \%
\end{aligned}
$$

$t_{i}=$ age of concrete when load is initially applied
$=1$ day
t = infinite days

$$
\begin{aligned}
\Psi_{(\infty, 1)} & =3.5(0.759)(0.748)(1.58-70 / 120)(1)^{(-0.118)}[1] \\
& =1.98
\end{aligned}
$$

Design Step C1.3

Calculate the creep coefficient, $\psi_{(t, t i)}$, in the beam at the time the slab is cast according to S5.4.2.3.2.

$$
\mathrm{t}=450 \text { days (maximum time) }
$$

Calculate the volume to surface area factor, $\mathrm{k}_{\mathrm{c}}$

$$
\begin{equation*}
\mathrm{k}_{\mathrm{c}}=\left[\frac{\left(\frac{\mathrm{t}}{26 \mathrm{e}^{0.36\left(\mathrm{~V} / S_{\mathrm{b}}\right.}+\mathrm{t}}\right)}{\left(\frac{\mathrm{t}}{45+\mathrm{t}}\right)}\right]\left[\frac{1.80+1.77 \mathrm{e}^{-0.54(\mathrm{~V} / \mathrm{S})_{\mathrm{b}}}}{2.587}\right] \tag{SC5.4.2.3.2-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \mathrm{t}=450 \text { days } \\
& \mathrm{e}=\text { natural log base (approx. 2.71828) } \\
&(\mathrm{V} / \mathrm{S})_{\mathrm{b}}=4.406 \mathrm{in} .
\end{aligned} \mathrm{k}_{\mathrm{c}}=\left[\frac{\left(\frac{450}{26 \mathrm{e}^{0.36(4.406}+450}\right)}{\left(\frac{450}{45+450}\right)}\right]\left[\frac{1.80+1.77 \mathrm{e}^{-0.54(4.406)}}{2.587}\right] \quad\left[\begin{array}{l}
\mathrm{k}_{\mathrm{c}}= \\
\end{array}\right.
$$

Calculate the creep coefficient, $\psi_{(\mathrm{t}, \mathrm{ti})}$, according to Eq. S5.4.2.3.2-1.

$$
\psi_{(450,1)}=3.5 \mathrm{k}_{\mathrm{c}} \mathrm{k}_{\mathrm{f}}(1.58-\mathrm{H} / 120) \mathrm{t}_{\mathrm{i}}^{-0.118}\left[\left(\mathrm{t}-\mathrm{t}_{\mathrm{i}}\right)^{0.6} /\left[10.0+\left(\mathrm{t}-\mathrm{t}_{\mathrm{i}}\right)^{0.6}\right]\right]
$$

where:

$$
\begin{aligned}
\mathrm{k}_{\mathrm{c}} & =0.651 \quad \text { (see above) } \\
\mathrm{k}_{\mathrm{f}} & =0.748 \text { (see above) } \\
\mathrm{H} & =70 \% \\
\mathrm{t}_{\mathrm{i}} & =1 \text { day } \\
\mathrm{t} & =450 \text { days } \\
\Psi_{(450,1)} & =3.5(0.651)(0.748)(1.58-70 / 120)(1)^{(-0.118)}\left[(450-1)^{0.6} /\left[10+(450-1)^{0.6}\right]\right] \\
& =1.35
\end{aligned}
$$

Calculate the restrained creep coefficient in the beam, $\phi$, as the creep coefficient for creep that takes place after the continuity connection has been established.

$$
\begin{aligned}
\phi & =\psi_{\infty}-\psi_{450} \quad(\text { from PCA publication referenced in Step 5.3.2.2 }) \\
& =1.98-1.35 \\
& =0.63
\end{aligned}
$$

## Design Step

Calculate the prestressed end slope, $\theta$.
For straight strands (debonding neglected). Calculate the end slope, $\theta$, for a simple beam under constant moment.

Moment $=\mathrm{Pe}_{\mathrm{c}}$

$$
\theta=\mathrm{Pe}_{\mathrm{c}} \mathrm{~L}_{\text {span }} / 2 \mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{c}}
$$

where:

## Design Step

Calculate the prestressed creep fixed end action for Span 1
The equation is taken from Table 5.3-9 for prestressed creep FEA, left end span, right moment.

$$
\begin{aligned}
\mathrm{FEM}_{\text {cr }} & =3 \mathrm{E}_{\mathrm{c}} \mathrm{I}_{\mathrm{c}} \theta / \mathrm{L}_{\text {span }} \\
& =[3(4,696)(1,384,254)(0.0052)] / 1,326 \\
& =76,476 / 12 \\
& =6,373 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

End forces due to prestress creep in Span 1:

$$
\begin{aligned}
\text { Left reaction } & =\mathrm{R} 1_{\mathrm{PScr}} \\
& =-\mathrm{FEM}_{\mathrm{cr}} / \mathrm{L}_{\text {span }} \\
& =-(6,373) / 110.5 \\
& =-57.7 \mathrm{k}
\end{aligned}
$$

Right reaction $=\mathrm{R} 2_{\mathrm{PScr}}$

$$
=-\mathrm{R} 1_{\mathrm{PScr}}
$$

$$
=57.7 \mathrm{k}
$$

Left moment $=\mathrm{M} 1_{\text {PScr }}$

$$
=0.0 \mathrm{k}-\mathrm{ft}
$$

Right moment $=\mathrm{M} 2_{\mathrm{PScr}}$

$$
=\mathrm{FEM}_{\mathrm{cr}}
$$

$$
=6,373 \mathrm{k}-\mathrm{ft}
$$

$$
\begin{aligned}
& \mathrm{P}=\text { initial prestressing force after all losses (kips) } \\
& =1,096 \mathrm{kips} \text { (see Design Step } 5.4 \text { for detailed calculations of the } \\
& \text { prestressing force) } \\
& e_{c}=46.54 \text { in. (calculated above) } \\
& \mathrm{L}_{\mathrm{span}}=110.5 \mathrm{ft} \text {. (1,326 in.) (taken equal to the continuous beam span } \\
& \text { length) } \\
& \mathrm{E}_{\mathrm{c}}=\text { the modulus of elasticity of the beam at final condition (ksi) } \\
& =4,696 \mathrm{ksi} \\
& \mathrm{I}_{\mathrm{c}}=\text { moment of inertia of composite beam (in }{ }^{4} \text { ) } \\
& =1,384,254 \text { in }^{4} \\
& \theta=[1,096(46.54)(1,326)] /[2(4,696)(1,384,254)] \\
& =0.0052 \mathrm{rads}
\end{aligned}
$$



Figure C1 - Presstress Creep Restraint Moment

## Design Step

Calculate dead load creep fixed end actions
Calculate the total dead load moment at the midspan

$$
\begin{aligned}
\text { Noncomposite DL moment } & =\mathrm{M}_{\mathrm{DNC}} \\
& =42,144 \mathrm{k} \text {-in }(3,512 \mathrm{k}-\mathrm{ft}) \text { (see Section 5.3) } \\
\text { Composite DL moment } & =\mathrm{M}_{\mathrm{DC}} \\
& =4,644 \mathrm{k} \text {-in }(387 \mathrm{k}-\mathrm{ft}) \text { (see Section 5.3) } \\
\text { Total DL moment } & =\mathrm{M}_{\mathrm{DL}} \\
& =\mathrm{M}_{\mathrm{DNC}}+\mathrm{M}_{\mathrm{DC}} \\
& =42,144+4,644 \\
& =46,788 / 12 \\
& =3,899 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

End forces due to dead load creep in Span 1:

$$
\begin{aligned}
\text { Left reaction } & =\mathrm{R} 1_{\mathrm{DLcr}} \\
& =-\mathrm{M}_{\mathrm{DI}} / \mathrm{L}_{\text {span }} \\
& =-3,899 / 110.5 \\
& =-35.3 \mathrm{k}
\end{aligned}
$$

Right reaction $=\mathrm{R} 2_{\text {DLcr }}$

$$
=-\mathrm{R} 1_{\mathrm{DLcr}}
$$

$$
=35.3 \mathrm{k}
$$

Left moment $=\mathrm{M} 1_{\text {DLcr }}$

$$
=0.0 \mathrm{k}-\mathrm{ft}
$$

Right moment $=$ M2 DLcr

$$
=-\mathrm{M}_{\mathrm{DL}}
$$

$$
=-3,899 \mathrm{k}-\mathrm{ft}
$$



Figure C2 - Dead Load Creep Restraint Moment

Calculate the creep correction factor, $\mathrm{C}_{\mathrm{cr}}$

$$
\begin{aligned}
\mathrm{C}_{\mathrm{cr}} & =1-\mathrm{e}^{-\phi} \quad(\text { from PCA publication referenced in Step 5.3.2.2) } \\
& =1-\mathrm{e}^{-0.63} \\
& =0.467
\end{aligned}
$$

Calculate the total creep (prestress + dead load) fixed end actions for 450 days.

$$
\begin{aligned}
\text { Left reaction } & =\mathrm{R} 1_{\mathrm{cr}} \\
& \left.=\mathrm{C}_{\mathrm{cr}} \mathrm{R} 1_{\mathrm{PScr}}+\mathrm{R} 2_{\mathrm{DLcr}}\right) \\
& =0.467(-57.7+35.4) \\
& =-10.41 \mathrm{k}
\end{aligned}
$$

Right reaction $=\mathrm{R} 2_{\text {cr }}$

$$
=-\mathrm{R} 1_{\mathrm{cr}}
$$

$$
=10.41 \mathrm{k}
$$

Left moment $=\mathrm{M} 1_{\mathrm{cr}}$

$$
=0.0 \mathrm{k}-\mathrm{ft}
$$

Right moment $=\mathrm{M} 2_{\text {cr }}$

$$
\begin{aligned}
& =\mathrm{C}_{\mathrm{cr}}\left(\mathrm{M} 2_{\mathrm{PScr}}+\mathrm{M} 2_{\mathrm{DLcr}}\right) \\
& =0.467[6,373+(-3,899)] \\
& =1,155 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$



## Figure C3 - Total Creep Fixed End Actions

## Design Step

## Creep final effects

The fixed end moments shown in Figure C3 are applied to the continuous beam. The beam is analyzed to determine the final creep effects. Due to the symmetry of the two spans of the bridge, the final moments at the middle support are the same as the applied fixed end moments. For a bridge with more than two spans or a bridge with two unequal spans, the magnitude of the final moments would be different from the fixed end moments.


Figure C4 - Creep Final Effects for a Deck and Continuity Connection Cast 450 Days After the Beams were Cast

Design Step
C2.1

Analysis of shrinkage effects on the example bridge
Calculate shrinkage strain in beam at infinite time according to S5.4.2.3.3
Calculate the size factor, $\mathrm{k}_{\mathrm{s}}$.

$$
\begin{equation*}
\mathrm{k}_{\mathrm{s}}=\left[\frac{\left(\frac{\mathrm{t}}{26 \mathrm{e}^{0.36\left(\mathrm{~V} / \mathrm{S}_{\mathrm{b}}\right.}+\mathrm{t}}\right)}{\left(\frac{\mathrm{t}}{45+\mathrm{t}}\right)}\right]\left[\frac{1,064-94(\mathrm{~V} / \mathrm{S})_{\mathrm{b}}}{923}\right] \tag{SC5.4.2.3.3-1}
\end{equation*}
$$

where:
t = drying time
$=$ infinite days
$\mathrm{e}=$ natural log base (approx. 2.71828)
$(\mathrm{V} / \mathrm{S})_{\mathrm{b}}=4.406 \mathrm{in}$.

$$
\begin{aligned}
& \mathrm{k}_{\mathrm{s}}=[1]\left[\frac{1,064-94(4.406)}{923}\right] \\
& \mathrm{k}_{\mathrm{s}}=0.704
\end{aligned}
$$

Calculate the humidity factor, $\mathrm{k}_{\mathrm{h}}$
Use Table S5.4.2.3.3-1 to determine $\mathrm{k}_{\mathrm{h}}$ for $70 \%$ humidity, $\mathrm{k}_{\mathrm{h}}=1.0$.

Assume the beam will be steam cured and devoid of shrinkage-prone aggregates, therefore, the shrinkage strain in the beam at infinite time is calculated as:

$$
\begin{equation*}
\varepsilon_{\mathrm{sh}, \mathrm{~b}, \infty}=-\mathrm{k}_{\mathrm{s}} \mathrm{k}_{\mathrm{h}}[\mathrm{t} /(55.0+\mathrm{t})]\left(0.56 \times 10^{-3}\right) \tag{S5.4.2.3.3-2}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{k}_{\mathrm{s}} & =0.704 \\
\mathrm{k}_{\mathrm{h}} & =1.0 \text { for } 70 \% \text { humidity }(\text { Table S5.4.2.3.3-1) } \\
\mathrm{t} \quad & =\text { infinite days } \\
\varepsilon_{\text {shb, }, \infty} & =-(0.704)(1.0)[1]\left(0.56 \times 10^{-3}\right) \\
& =-3.94 \times 10^{-4}
\end{aligned}
$$

Design Step C2.2

Calculate shrinkage strain in the beam at the time the slab is cast (S5.4.2.3.3)
$\mathrm{t}=$ time the slab is cast
$=450$ days (maximum value)
Calculate the size factor, $\mathrm{k}_{\mathrm{s}}$.

$$
\begin{equation*}
\mathrm{k}_{\mathrm{s}}=\left[\frac{\left(\frac{\mathrm{t}}{26 \mathrm{e}^{0.36\left(\mathrm{~V} / \mathrm{S}_{\mathrm{b}}\right.}+\mathrm{t}}\right.}{\left(\frac{\mathrm{t}}{45+\mathrm{t}}\right)}\right]\left[\frac{1,064-94(\mathrm{~V} / \mathrm{S})_{\mathrm{b}}}{923}\right] \tag{SC5.4.2.3.3-1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{t} & =450 \text { days } \\
\mathrm{e} & =\text { natural } \log \text { base (approx. } 2.71828) \\
(\mathrm{V} / \mathrm{S})_{\mathrm{b}} & =4.406 \text { in. }
\end{aligned}
$$

$$
\mathrm{k}_{\mathrm{s}}=\left[\frac{\left(\frac{450}{26 \mathrm{e}^{0.36(4.406}+450}\right)}{\left(\frac{450}{45+450}\right)}\right]\left[\frac{1,064-94(4.406)}{923}\right]
$$

$$
\mathrm{k}_{\mathrm{s}}=0.604
$$

Assume the beam will be steam cured and devoid of shrinkage-prone aggregates, therefore, the shrinkage strain in the beam at infinite time is calc ulated as:

$$
\begin{equation*}
\varepsilon_{\text {sh, }, 4,450}=-\mathrm{k}_{\mathrm{s}} \mathrm{k}_{\mathrm{h}}[\mathrm{t} /(55.0+\mathrm{t})]\left(0.56 \times 10^{-3}\right) \tag{S5.4.2.3.3-2}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{k}_{\mathrm{s}} & =0.604 \\
\mathrm{k}_{\mathrm{h}} & =1.0 \text { for } 70 \% \text { humidity (Table S5.4.2.3.3-1) } \\
\mathrm{t} \quad & =450 \text { days } \\
\varepsilon_{\mathrm{sh}, \mathrm{~b}, 450} & =-(0.604)(1.0)[450 /(55.0+450)]\left(0.56 \times 10^{-3}\right) \\
& =-3.01 \times 10^{-4}
\end{aligned}
$$

## Design Step

Calculate the shrinkage strain in the slab at infinite time (S5.4.2.3.3)
Calculate the size factor, $\mathrm{k}_{\mathrm{s}}$

$$
\begin{equation*}
\mathrm{k}_{\mathrm{s}}=\left[\frac{\left(\frac{\mathrm{t}}{26 \mathrm{e}^{0.36(\mathrm{~V} /)_{s}}+\mathrm{t}}\right)}{\left(\frac{\mathrm{t}}{45+\mathrm{t}}\right)}\right]\left[\frac{1,064-94(\mathrm{~V} / \mathrm{S})_{\mathrm{b}}}{923}\right] \tag{SC5.4.2.3.3-1}
\end{equation*}
$$

where:
t = infinite days
$\mathrm{e} \quad=$ natural log base (2.71828)
Compute the volume to surface area ratio for the slab.

$$
(\mathrm{V} / \mathrm{S})_{\mathrm{s}}=\left(\mathrm{b}_{\text {slab }}\right)\left(\mathrm{t}_{\text {slab }}\right) /\left(2 \mathrm{~b}_{\text {slab }}-\mathrm{w}_{\mathrm{tf}}\right)
$$

where:

$$
\begin{array}{ll}
\mathrm{b}_{\text {slab }} & =\text { slab width taken equal to girder spacing (in.) } \\
\mathfrak{t}_{\text {slab }} & =\text { slab structural thickness (in.) } \\
\mathrm{w}_{\mathrm{tf}} & =\text { beam top flange width (in.) }
\end{array}
$$

$(\mathrm{V} / \mathrm{S})_{\mathrm{s}}=116(7.5) /[2(116)-42]$

$$
=4.58 \mathrm{in} .
$$

$$
\mathrm{k}_{\mathrm{s}}=[1]\left[\frac{1,064-94(4.58)}{923}\right]
$$

$$
\mathrm{k}_{\mathrm{s}}=0.686
$$

The slab will not be steam cured, therefore, use

$$
\begin{equation*}
\varepsilon_{\mathrm{sh}, \mathrm{~s}, \infty}=-\mathrm{k}_{\mathrm{s}} \mathrm{k}_{\mathrm{h}}[\mathrm{t} /(35.0+\mathrm{t})]\left(0.51 \times 10^{-3}\right) \tag{S5.4.2.3.3-1}
\end{equation*}
$$

where:

$$
\mathrm{k}_{\mathrm{s}}=0.686
$$

$$
\mathrm{k}_{\mathrm{h}}=1.0 \text { for } 70 \% \text { humidity (Table S5.4.2.3.3-1) }
$$

$$
\mathrm{t}=\text { infinite days }
$$

$$
\varepsilon_{\mathrm{sh}, \mathrm{~s}, \infty}=-(0.686)(1.0)[1.0]\left(0.51 \times 10^{-3}\right)
$$

$$
=-3.50 \times 10^{-4}
$$

Design Step
Calculate the differential shrinkage strain as the difference between the deck total shrinkage strain and the shrinkage strain of the beam due to shrinkage that takes place after the continuity connection is cast.

$$
\begin{aligned}
\Delta \varepsilon_{\mathrm{sh}} & =\varepsilon_{\mathrm{sh}, \mathrm{~s}, \infty}-\left(\varepsilon_{\mathrm{sh}, \mathrm{~b}, \infty}-\varepsilon_{\mathrm{sh}, \mathrm{~b}, 450}\right) \\
& =-3.50 \times 10^{-4}-\left[-3.94 \times 10^{-4}-\left(-3.01 \times 10^{-4}\right)\right] \\
& =-2.57 \times 10^{-4}
\end{aligned}
$$

Calculate the shrinkage driving end moment, $\mathrm{M}_{\mathbf{s}}$
$\mathrm{M}_{\mathrm{s}}=\Delta \varepsilon_{\text {sh }} \mathrm{E}_{\mathrm{cs}} \mathrm{A}_{\text {slabe }}{ }^{\prime}$ (from PCA publication referenced in Design Step 5.3.2.2)
where:
$\Delta \varepsilon_{\text {sh }} \quad=$ differential shrinkage strain
$\mathrm{E}_{\mathrm{cs}} \quad=$ elastic modulus for the deck slab concrete (ksi)
$\mathrm{A}_{\text {slab }}=$ cross-sectional area of the deck slab (in ${ }^{2}$ )
$\mathrm{e}^{\prime} \quad=$ the distance from the centroid of the slab to the centroid of the composite section (in.)
$=\mathrm{d}_{\text {beam }}+\mathrm{t}_{\text {slab }} / 2-\mathrm{NA}_{\text {beam bottom }}$
$=72+7.5 / 2-51.54$
$=24.21 \mathrm{in}$.
$\mathrm{M}_{\mathrm{s}}=\left(-2.57 \times 10^{-4}\right)(3,834)(116)(7.5)(24.21)$
$=20,754 / 12$
$=1,730 \mathrm{k}$-ft (see notation in Table 5.3-9 for sign convention)


Figure C5 - Shrinkage Driving Moment

For beams under constant moment along their full length, the restraint moment may be calculated as shown above for the case of creep due to prestressing force or according to Table 5.3-9.

Shrinkage fixed end actions $=-1.5 \mathrm{M}_{\mathrm{s}}=-1.5(1,730)$

$$
=-2,595 \mathrm{k}-\mathrm{ft}
$$



## Figure C6 - Shrinkage Fixed End Actions

## Design Step

Analyze the beam for the fixed end actions
Due to symmetry of the spans, the moments under the fixed end noments shown in Figure C6 are the same as the final moments (shown in Fig. C7). For bridges with three or more spans and for bridges with two unequal spans, the continuity moments will be different from the fixed end moments.


Figure C7 - Shrinkage Continuity Moments

Design Step
C2.7
Calculate the correction factor for shrinkage.

$$
\begin{aligned}
\mathrm{C}_{\mathrm{sh}} & =\left(1-\mathrm{e}^{-\phi}\right) / \phi \text { (from PCA publication referenced in Step 5.3.2.2) } \\
& =\left[1-\mathrm{e}^{-0.63}\right] / 0.63 \\
& =0.742
\end{aligned}
$$

Calculate the shrinkage final moments by applying the correction factor for shrinkage to the sum of the shrinkage driving moments (Figure C5) and the shrinkage continuity moment (Figure C7) fixed end actions.

End moments, Span 1:

$$
\begin{aligned}
\text { Left end moment } & =\mathrm{M} 1_{\mathrm{sh}} \\
& =\mathrm{C}_{\mathrm{sh}}\left(\mathrm{M}_{\mathrm{sh}, \mathrm{dr}}+\text { shrinkage continuity moment }\right) \\
& =0.742(1,730+0) \\
& =1,284 \mathrm{k}-\mathrm{ft}
\end{aligned}
$$

Right end moment $=\mathrm{M} 2_{\text {sh }}$
$=\mathrm{C}_{\text {sh }}\left(\mathrm{M}_{\text {sh,dr }}+\right.$ shrinkage continuity moment $)$

$$
=0.742(1,730-2,595)
$$

$$
=-642 \mathrm{k}-\mathrm{ft}
$$



Figure C8 - Final Total Shrinkage Effect

Tables C1 and C2 provide a summary of the final moments for the case of the deck poured 30 days after the beams were cast.

Table C1-30 Day Creep Final Moments

| Span | M1 <br> $(k-f t)$ | M2 <br> $(k-f t)$ | $R 1$ <br> $(k)$ | $R 2$ <br> $(k)$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 1,962 | -17.7 | 17.7 |
| 2 | $-1,962$ | 0 | 17.7 | -17.7 |

Table C2-30 Day Shrinkage Final Moments

| Span | M1 <br> $(k-f t)$ | M2 <br> $(k-f t)$ | R 1 <br> $(k)$ | R 2 <br> $(k)$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 75.9 | -37.9 | -2.06 | 2.06 |
| 2 | -37.9 | 75.9 | 2.06 | -2.06 |

When a limit state calls for inclusion of the creep and shrinkage effects and/or the design procedures approved by the bridge owner calls for their inclusion, the final creep and shrinkage effects should be added to other load effect at all sections. The positive moment connection at the bottom of the beams at the intermediate support is designed to account for the creep and shrinkage effects since these effects are the major source of these moments.

Notice that when combining creep and shrinkage effects, both effects have to be calculated using the same age of beam at the time the continuity connection is established.

