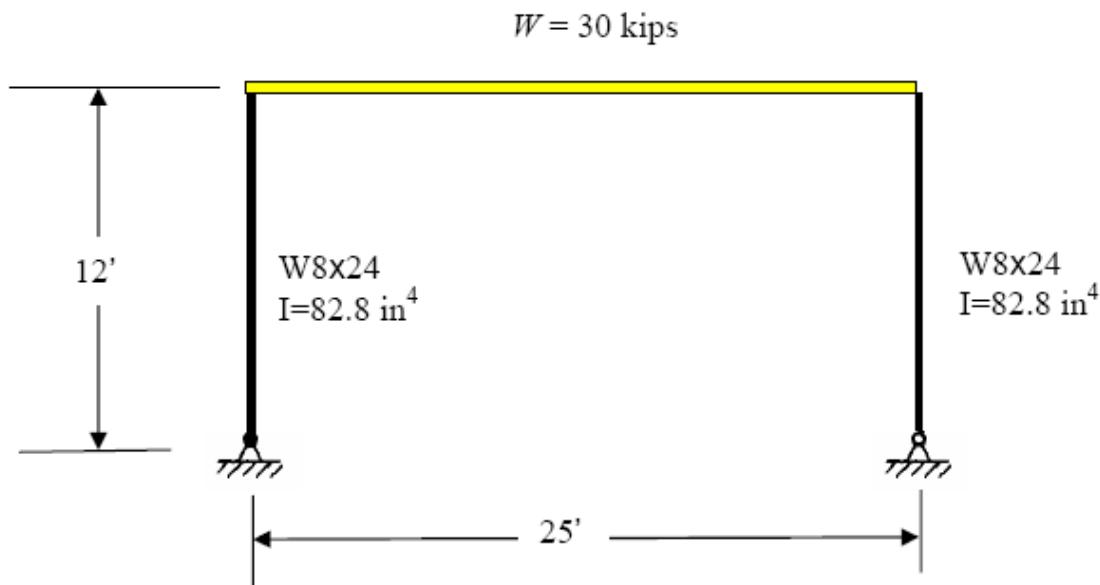


The portal frame in the figure is located in Memphis (35.11 Lat. -89.94 Long.). Compute the confidence levels on having:

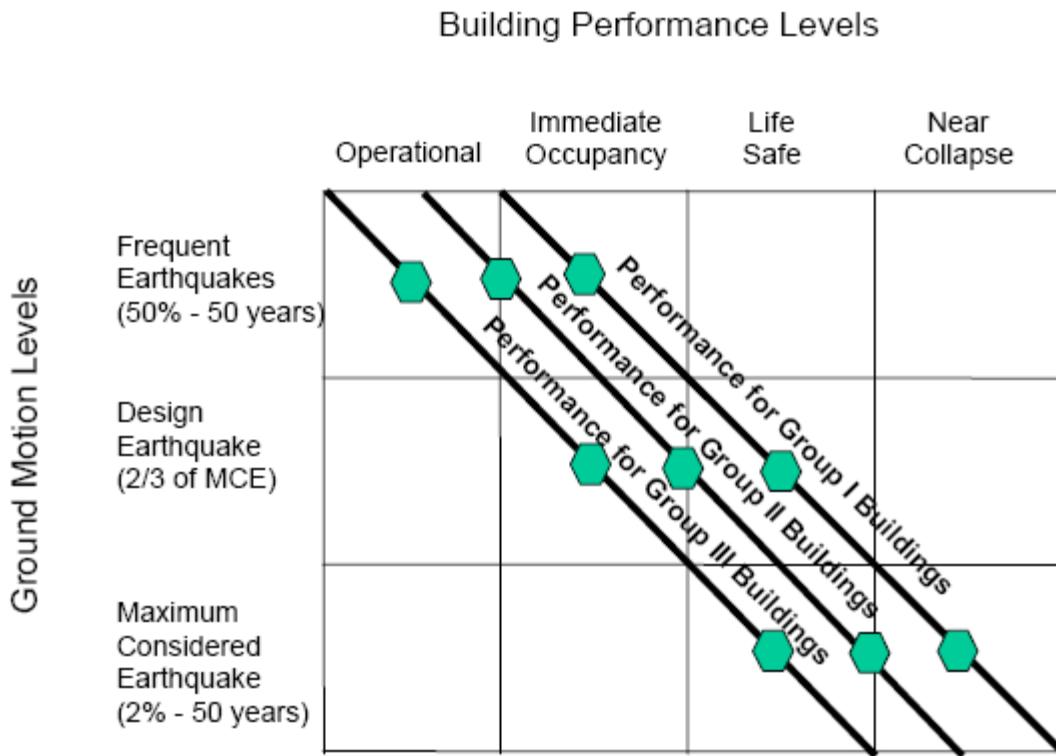
- Less than 5% probability of a performance poorer than Collapse Prevention (CP) in 50 years life cycle of the building, and
- Less than 50% probability of having a performance poorer than Immediate Occupancy (IO) in 50 years.

Use LSP.

Assume first mode equivalent damping ratio of 8%. Shear wave velocity at the site is measured 2000 ft/sec. Assume post-Northridge pre-qualified dog-bone moment connections in a shear building.



dog bone moment connections or reduced beam section (RBS) imply special moment frames or intermediate moment frames, assuming special moment frames  
assuming rigid floor  
using elf procedure for lateral loads



### Part 2, General data and functions

$$\text{ORIGIN} := 1 \quad k := 1000 \text{lb} \quad \text{Int}(x_1, y_1, x_2, y_2, x) := \left( \frac{y_2 - y_1}{x_2 - x_1} \right) \cdot (x - x_1) + y_1$$

$$E_s := 29000 \frac{k}{\text{in}^2}$$

### Part 3, Definition of structure and site.

$$\begin{aligned} \text{llf} &:= (0) \frac{\text{lb}}{\text{ft}^2} & \text{frsp} &:= 1 \text{ft} & \text{bay} &:= 25 \text{ft} & \text{dlf} &:= (1.2) \frac{k}{\text{ft}^2} & 1 \text{ is furthest from ground} \\ & & & & & & & & \\ \text{nfr} &:= 1 & & & & & & & \end{aligned}$$

$$\text{llwf} := \text{llf} \cdot \text{frsp} \cdot \text{bay} \quad \text{llbrf} := \frac{\text{llwf}}{2} \quad \text{dlwf} := \text{dlf} \cdot \text{frsp} \cdot \text{bay} \quad \text{dlbrf} := \frac{\text{dlwf}}{2}$$

$$\text{llwf} = (0) \text{k} \quad \text{llbrf} = (0) \text{k} \quad \text{dlwf} = (30) \text{k} \quad \text{dlbrf} = (15) \text{k}$$

$$F_y := 50 \frac{k}{in^2} \quad R_y := 1.1 \quad Z_{xc} := 23.2 in^3$$

$$h := (12) ft \quad bldg_{height} := \sum_{i=1}^{length(h)} h_i \quad bldg_{height} = 12 ft$$

Seismic force resisting system (SFRS), SFRS := "Special Steel Moment Frames"

$$v_s := 2000 \frac{ft}{sec} \quad LOC := "Memphis, Tennessee" \quad \zeta := 0.08$$

$$lat := 35.11 \quad lon := -89.94$$

$$I_c := (82.8) \cdot in^4 \quad mf := \frac{dlwf}{g} \quad mf = (0.078) k \cdot \frac{s^2}{in} \quad kf := \left( \frac{6 \cdot E_s \cdot I_c}{h^3} \right) \quad kf = (4.825) \frac{k}{in}$$

#### Part 4, General Code information:

##### Chapter 1, General Provisions

##### 1.2 Occupancy importance factor (pg 4)

$$\text{Seismic Use Group (enter as integer): } SUG := 1$$

##### 1.3 Occupancy importance factor (pg 5)

$$I_f := \begin{cases} 1.0 & \text{if } SUG = 1 \\ 1.25 & \text{if } SUG = 2 \\ 1.5 & \text{otherwise} \end{cases} \quad I_f = 1$$

##### 1.4 Seismic Design category (SDC) (pg 5)

Determination of SDS and SD1 from chapter 3 of code:

Ss and S1, section 3.3.1 (pg 19), Figures 3.3-1 through 3.3-14 (pgs 20 to 37), or USGS website

$$LOC = "Memphis, Tennessee" \quad lat = 35.11 \quad lon = -89.94$$

$$S_s := 1.166g \quad S_1 := 0.325g$$

##### Sms and Sm1, section 3.3.2 (pg 19)

$$\text{Site class, section 3.5 (pg 47)} \quad v_s = 2 \times 10^3 \frac{ft}{s}$$

$$\text{SiteClass := "C"}$$

Fa and Fv from tables 3.3-1 and 3.3-2 (pgs 19 and 38, respectively)

$$F_a := 1.0 \quad F_a = 1$$

$$F_v := \text{Int}\left(0.3, 1.5, 0.4, 1.4, \frac{S_1}{g}\right) \quad F_v = 1.475$$

$$S_{MS} := F_a \cdot S_s \quad \text{Eq. 3.3-1} \quad S_{MS} = 1.166 \text{ g}$$

$$S_{M1} := F_v \cdot S_1 \quad \text{Eq. 3.3-2} \quad S_{M1} = 0.479 \text{ g}$$

$$S_{DS} := \frac{2}{3} \cdot S_{MS} \quad \text{Eq. 3.3-3} \quad S_{DS} = 0.777 \text{ g}$$

$$S_{D1} := \frac{2}{3} \cdot S_{M1} \quad \text{Eq. 3.3-4} \quad S_{D1} = 0.32 \text{ g}$$

$SDC_1 := "D"$  Based on Table 1.4-1, (pg 6)

$SDC_2 := "D"$  Based on table 1.4-2, (pg 6)

$$SDC := \begin{cases} "E" & \text{if } (SUG = 1 \vee SUG = 2) \wedge \frac{S_1}{g} \geq 0.75 \\ "F" & \text{if } SUG = 3 \wedge \frac{S_1}{g} \geq 0.75 \\ \max(SDC) & \text{otherwise} \end{cases}$$

Seismic design Category:  
 $SDC = "D"$

Note: may follow procedures of section 1.5 (pg 6) if seismic design category is A

Chapter 2 is based on quality assurance

Chapter 3, Ground Motion

3.2.1, Site Class (pg 19)    SiteClass = "C"

3.2.2, Procedure selection: General Procedure

3.3.1, Mapped Acceleration parameters.     $S_s = 1.166 \text{ g}$      $S_1 = 0.325 \text{ g}$

3.3.2, Site coefficients and adjusted acceleration parameters.

$$F_a = 1 \quad F_v = 1.475 \quad S_{MS} = 1.166 \text{ g} \quad S_{M1} = 0.479 \text{ g}$$

3.3.3, Design acceleration parameters (pg 38)

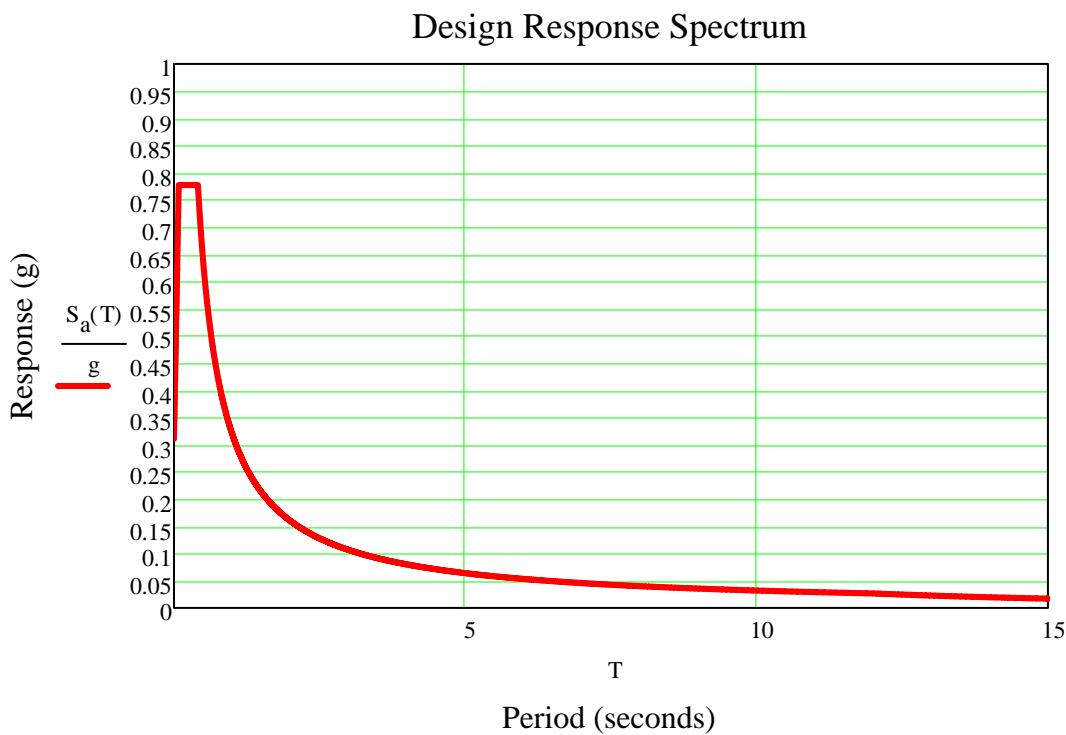
$$S_{DS} = 0.777 \text{ g} \quad S_{D1} = 0.32 \text{ g}$$

3.3.4, Design response spectrum

$\text{Tr} := 0\text{sec}, 0.001\text{sec} .. 15\text{sec}$      $T_L := 12\text{sec}$     T.L given in figures 3.3-16 through 3.3-21  
on pages 40 through 45

$$T_S := \frac{S_{D1}}{S_{DS}} \cdot \text{sec} \quad T_S = 0.411 \text{ s} \quad T_0 := 0.2 \cdot T_S \quad T_0 = 0.082 \text{ s}$$

$$S_a(T) := \begin{cases} 0.6 \cdot \frac{S_{DS}}{T_0} \cdot T + 0.4 \cdot S_{DS} & \text{if } T \leq T_0 \\ S_{DS} & \text{if } T_0 < T \leq T_S \\ \frac{S_{D1} \cdot sec}{T} & \text{if } T_S < T \leq T_L \\ \frac{S_{D1} \cdot T_L \cdot sec}{T^2} & \text{otherwise} \end{cases} \quad \begin{matrix} \text{Eq. 3.3-5} \\ \text{Eq. 3.3-6} \\ \text{Eq. 3.3-7} \end{matrix}$$



3.5.1 Site classification for seismic design (pg 47)      SiteClass = "C"

Chapter 4, Structural design Criteria

4.2.2 Combination of Load effects (pg 54), will be incorporated after loads are calculated

4.3 Seismic Force Resisting System (pg 55)

4.3.1 Selection and limitations, Table 4.3-1 (pgs 56 to 60)

SFRS = "Special Steel Moment Frames"      SDC = "D"

$R_f := 8$      $\Omega_0 := 3$      $C_d := 5.5$

Detailing reference section: AISC Seismic, Part I, Sec. 9

Limitations based on Seismid Design Category: NL

Table 4.3-2 Plan Structural Irregularities (pg 64):                    SDC = "D"

No plan structural irregularities noted.                    PSI := "None"

Table 4.3-3 Vertical Structural Irregularities (pg 65)

No vertical structural irregularities noted.                    VSI := "None"

#### 4.3.3 Redundancy

$$r_{\max,x} := 0.33 \quad \rho := \min \left( \max \left( 2 - \frac{20}{r_{\max,x} \cdot \sqrt{\frac{\text{bay}}{\text{ft}} \cdot \frac{\text{frsp}}{\text{ft}} \cdot \text{nfr}}} , 1 \right) , 1.5 \right) \quad \rho = 1$$

(From 1997 Provisions, chapter 5, pg 55)

Table 4.4-1 Analysis Procedures

SDC = "D"                    PSI = "None"                    VSI = "None"

5.2.2.1 Approximate Fundamental Period (pg 88)

Table 5.2-2 Approximate period parameters (pg 88)

$$C_r := 0.028 \quad x_f := 0.8$$

$$T_a := C_r \left( \frac{\text{bldgheight}}{\text{ft}} \right)^{x_f} \cdot \text{sec} \quad T_a = 0.204 \text{ s}$$

From Table 5.2-1 (pg 88)      \$D\_1 = 0.32 \text{ g}\$

$$C_u := 1.4$$

$$T_{\max} := C_u \cdot T_a \quad T_{\max} = 0.286 \text{ s} \quad 3.5 \cdot T_S = 1.439 \text{ s}$$

Tmax < 3.5Ts and no irregularities noted, All design procedures are permitted.

Table 4.5-1, Allowable Story Drift

SUG = 1                    SFRS = "Special Steel Moment Frames"

$$h = (12) \text{ ft}$$

$$ASD_f := 0.025$$

$$ASD := ASD_f \cdot h \quad ASD = (3.6) \text{ in}$$

### First Analysis by Response Spectrum Procedure of FEMA 302

5.3 Response Spectrum Procedure (pg 92)

5.3.2 and 5.3.3 modes and modal properties (pg 92)

$$mf = (0.078) \frac{k \cdot s^2}{in} \quad kf = (4.825) \frac{k}{in}$$

$$M := mf_1 \quad K := kf_1$$

$$\omega := \sqrt{\frac{K}{M}} \quad \omega = 7.88 \frac{1}{s} \quad T := 2 \cdot \frac{\pi}{\omega} \quad T = 0.797 \text{ s} \quad f := \frac{1}{T} \quad f = 1.254 \frac{1}{s}$$

only one lateral mode, 100% of modal mass accounted for

5.3.4 Modal base shear, pg 92

$$C_s := \frac{S_a(T)}{\frac{R_f}{I_f}} \quad C_s = 0.05 g \quad \text{Eq. 5.3-3, pg 93}$$

$$w := dlwf \quad w = (30) k \quad W := w \quad W = (30) k$$

$$V_m := \frac{C_s}{g} \cdot W \quad V_m = (1.503) k \quad \text{Eq. 5.3-1} \quad tm := \sum_{i=1}^1 m f_i \quad tm = 0.078 \frac{k \cdot s^2}{in}$$

$$mf = (0.078) \frac{k \cdot s^2}{in}$$

Mode 1:

Eq. 5.3-7, pg 94

$$C_{vx1} := C_s$$

$$C_{vx1} = 1.612 \frac{ft^2}{s^2} \quad F_{x1} := \frac{C_{vx1}}{g} \cdot V_{m1} \quad F_{x1} = 0.075 k$$

## 5.3.6, Modal story shears and moments

$$V_{x1} := (F_{x1}) \quad M_{x1} := (F_{x1} \cdot h_1)$$

$$V_{x1} = (0.075) k \quad M_{x1} = (0.904) k \cdot ft$$

$$\delta_{xe1} := \left( \frac{g}{4 \cdot \pi^2} \right) \cdot \left( \frac{T^2 \cdot F_{x1}}{w} \right) \quad \delta_{xe1} = (0.016) \text{ in} \quad \text{Eq. 5.3-9, pg 94}$$

$$\delta_{x1} := \frac{C_d \cdot \delta_{xe1}}{I_f} \quad \delta_{x1} = (0.086) \text{ in} \quad \text{Eq. 5.3-8, pg 94}$$

## 5.3.7 Design values (combination of modes) pg 94:

Using cqc combination so that it will not be necessary to check against spread of periods or make a determination of what is considered too much or too little spread in the data.

no combination of modes here as there is only one mode

$$F_{xm} := (F_{x1}) \quad V_{xm} := (V_{x1}) \quad M_{xm} := (M_{x1}) \quad \delta_{xm} := (\delta_{x1})$$

Comparison with ELF procedure

$$T = 0.797 \text{ s} \quad T_{max} = 0.286 \text{ s} \quad T_{elfc} := \min(T, T_{max}) \quad T_{elfc} = 0.286 \text{ s}$$

$$C_{selfc} := \max \left[ \min \left[ \frac{S_{DS}}{\frac{R_f}{I_f}}, \begin{cases} \frac{S_{D1}}{\frac{T_{elfc}}{\text{sec}} \cdot \left( \frac{R_f}{I_f} \right)} & \text{if } T_{elfc} \leq T_L \\ \frac{S_{D1}}{\left( \frac{T_{elfc}}{\text{sec}} \right)^2 \cdot \left( \frac{R_f}{I_f} \right)} & \text{otherwise} \end{cases} \right] \cdot \frac{1}{g}, 0.01 \right] \quad \text{Eq. 5.2-2}$$

Eq. 5.2-3

Eq. 5.2-4

$C_{selfc} = 0.097$

$$S_1 = 0.325 \text{ g} \quad C_{selfc} := \begin{cases} C_{selfc} & \text{if } \frac{S_1}{g} < 0.6 \\ \max \left( C_{selfc}, \frac{0.5 \cdot S_1 \cdot I_f}{R_f \cdot g} \right) & \text{otherwise} \end{cases} \quad \text{Eq. 5.2-5}$$

$C_{selfc} = 0.097$

$$\text{bld}_W := W \quad \text{bld}_W = (30) k \quad \text{bld.w represents one frame only}$$

$$V_{elfc} := C_{selfc} \cdot \text{bld}_W \quad V_{elfc} = (2.915) k$$

$$\text{Base shear from elf procedure:} \quad V_{elfc} = (2.915) k$$

$$\text{Base shear from modal analysis:} \quad V_{xm_1} = 0.075 k$$

$$elfc_f := \max\left(0.85 \cdot \frac{V_{elfc}}{V_{xm_1}}, 1\right) \quad elfc_f = 32.904$$

$$F_{xm} := elfc_f \cdot F_{xm} \quad V_{xm} := elfc_f \cdot V_{xm} \quad M_{xm} := elfc_f \cdot M_{xm} \quad \delta_{xm} := elfc_f \cdot \delta_{xm}$$

$$F_{xm} = (2.478) k \quad V_{xm} = (2.478) k \quad M_{xm} = (29.733) k \cdot ft \quad \delta_{xm} = (2.824) \text{ in}$$

5.3.10 P-delta effects, determine P-delta in accordance with 5.2.6, determine drift limits in accordance with 5.2.6.1

#### 5.2.6.1 Story drift determination (pg 91)

$$F_{xm} = (2.478) k \quad kf = (4.825) \frac{k}{in} \quad C_d = 5.5 \quad I_f = 1 \quad nfr = 1$$

$$V_{xm} = (2.478) k \quad \delta_{xm} = (2.824) \text{ in} \quad \delta_{xmt} := (\delta_{xm_1}) \quad \delta_{xmt} = (2.824) \text{ in}$$

$$\Delta := (\delta_{xm_1}) \quad \Delta = (2.824) \text{ in} \quad ASD = (3.6) \text{ in}$$

$$\text{drift}_{\text{status}} := \begin{cases} \text{"DRIFT OK"} & \text{if } \Delta_1 \leq ASD_1 \\ \text{"EXCEEDS ALLOWABLE DRIFT LIMITS"} & \text{otherwise} \end{cases}$$

$$\text{drift}_{\text{status}} = \text{"DRIFT OK"}$$

#### 5.2.6.2 P-delta limit (pg 91)

$$llcrf := (llbrf_1) \quad llcrf = (0) k \quad dlcrf := (dlbrf_1) \quad dlcrf = (15) k$$

$$P_x := llcrf + dlcrf + \frac{V_{xm} \cdot h}{\text{bay}} \quad P_x = (16.189) k$$

$$\theta := \frac{P_x \cdot \Delta_1 \cdot I_f}{V_{xm_1}} \quad \theta = (0.047) \quad \text{All } \theta \text{ less than 0.1, P-delta limit ok.}$$

$$\frac{2}{2} \cdot h_1 \cdot C_d$$

$$P_{delta\_status} := \begin{cases} "OK" & \text{if } \theta_1 < 0.1 \\ "Must check P-delta" & \text{otherwise} \end{cases} \quad P_{delta\_status} = "OK"$$

Axial: Unfactored Loads at column bases, positive force is downward force:

Seismic Load effect of section 4.2.2.1 (pg 55)       $\rho = 1$        $S_{DS} = 0.777 g$

$$Q_E := \frac{\sum_{i=1}^1 (h_i \cdot F_{xm_1})}{\text{bay}} \quad Q_E = 1.189 \text{ k} \quad D := \sum_{i=1}^1 dlbrf_i \quad D = 15 \text{ k}$$

Seismic Load effect:

$$E_p := \rho \cdot Q_E + 0.2 \cdot \frac{S_{DS}}{g} \cdot D \quad E_p = 3.521 \text{ k}$$

$$E_n := -\rho \cdot Q_E + 0.2 \cdot \frac{S_{DS}}{g} \cdot D \quad E_n = 1.143 \text{ k}$$

$$L := \sum_{i=1}^1 llbrf_i \quad L = 0 \text{ k} \quad L_r := llbrf_1 \quad L_r = 0 \text{ k}$$

$$S := 0 \cdot \text{kip} \quad W_p := 0 \cdot \text{kip} \quad W_n := 0 \cdot \text{kip} \quad H := 0 \cdot \text{kip}$$

$$F := 0 \cdot \text{kip} \quad T_f := 0 \cdot \text{kip} \quad R := 0 \cdot \text{kip} \quad (\text{These loads not present or assumed to not control})$$

Load combinations:       $f_1 := 1$

$$\text{Comb} := \begin{bmatrix} 1.4(D + F) \\ 1.2(D + F + T_f) + 1.6(L + H) + 0.5 \cdot \max(L_r, S, R) \\ 1.2 \cdot D + 1.6 \cdot \max(L_r, S, R) + \max(f_1 \cdot L, 0.8 \cdot W_p) \\ 1.2 \cdot D + 1.6 \cdot W_p + f_1 \cdot L + 0.5 \cdot \max(L_r, S, R) \\ 1.2D + 1.0 \cdot E_p + f_1 \cdot L + 0.2 \cdot S \\ 0.9D + 1.6 \cdot W_n + 1.6H \\ 0.9D + 1.0 \cdot E_n + 1.6H \end{bmatrix} \quad \text{Comb} = \begin{pmatrix} 21 \\ 18 \\ 18 \\ 18 \\ 21.521 \\ 13.5 \\ 14.643 \end{pmatrix} \text{ k}$$

$$P_{\max} := \max(\text{Comb}) \quad P_{\max} = 21.521 \text{ k} \quad P_{\min} := \min(\text{Comb}) \quad P_{\min} = 13.5 \text{ k}$$

Bending: loads due to horizontal reaction at base, assuming columns share load equally, and assuming columns are fixed at the base:

$$E := \frac{\sum_{i=1}^1 F_{xm_i} h_1}{2} \cdot \frac{h_1}{2} \quad E = 7.433 \text{ k}\cdot\text{ft}$$

$$\begin{aligned} D &:= 0 \cdot \text{kip} & L &:= 0 \cdot \text{kip} & L_w &:= 0 \cdot \text{kip} & S &:= 0 \cdot \text{kip} & W &:= 0 \cdot \text{kip} & H &:= 0 \cdot \text{kip} \\ F &:= 0 \cdot \text{kip} & T_f &:= 0 \cdot \text{kip} & R &:= 0 \cdot \text{kip} & & & & & & \end{aligned} \quad (\text{These loads not present or assumed to not control})$$

Load combinations:  $f_{1k} := 1$

$$\text{Comb} := \begin{bmatrix} 1.4(D + F) \\ 1.2 \cdot (D + F + T_f) + 1.6 \cdot (L + H) + 0.5 \cdot \max(L_r, S, R) \\ 1.2 \cdot D + 1.6 \cdot \max(L_r, S, R) + \max(f_1 \cdot L, 0.8 \cdot W_p) \\ 1.2 \cdot D + 1.6 \cdot W_p + f_1 \cdot L + 0.5 \cdot \max(L_r, S, R) \\ 1.2 \cdot D + 1.0 \cdot E + f_1 \cdot L + 0.2 \cdot S \\ 0.9 \cdot D + 1.6 \cdot W_n + 1.6 \cdot H \\ 0.9 \cdot D + 1.0 \cdot E + 1.6 \cdot H \end{bmatrix} \quad \text{Comb} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 7.433 \\ 0 \\ 7.433 \end{pmatrix} \text{ k}\cdot\text{ft}$$

$$M_{\max} := \max(\text{Comb}) \quad M_{\max} = 7.433 \text{ k}\cdot\text{ft} \quad V_{\max} := \frac{M_{\max}}{0.5 h_1} \quad V_{\max} = 1.239 \text{ k}$$

Summary of results:

$$P_{\max} = 21.521 \text{ k} \quad P_{\min} = 13.5 \text{ k} \quad M_{\max} = 7.433 \text{ k}\cdot\text{ft} \quad V_{\max} = 1.239 \text{ k}$$

### Part A. Analysis by Fema 350

Response spectrum from Fema 273

From 5% in 50 year hazard maps (2002 data from USGS java applet)

$$S_{0.05} := 0.6563 \text{g} \quad S_{1.0} := 0.1683 \text{g}$$

F273, 2.6.1.4, adjustment for site class (pg 2-21)

$$\text{SiteClass} := \text{"C"}$$

$$F_a := 1.16 \quad F_a = 1.16$$

$$F_v := 1.64 \quad F_v = 1.64$$

$$S_{xs} := F_a \cdot S_s \quad S_{xs} = 0.761 \text{ g} \quad S_{x1} := F_v \cdot S_1 \quad S_{x1} = 0.276 \text{ g}$$

F273, 2.6.1.5, general response spectrum

$$T_e := 0 \text{sec}, 0.001 \text{sec} \dots 15 \text{sec}$$

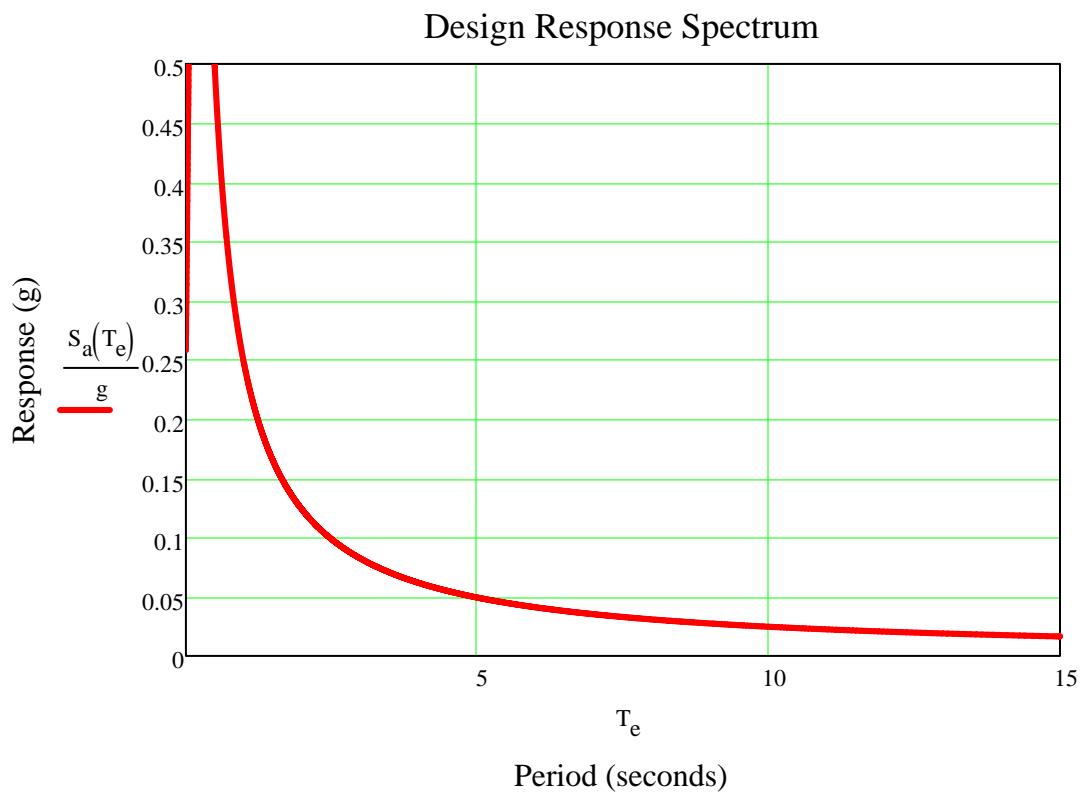
$$\beta := 100\zeta \quad \beta = 8$$

$$B_s := \text{Int}(5, 1.0, 10, 1.3, \beta) \quad B_s = 1.18$$

$$B_1 := \text{Int}(5, 1.0, 10, 1.2, \beta) \quad B_1 = 1.12$$

$$T_0 := \left( \frac{S_{x1} \cdot B_s}{S_{xs} \cdot B_1} \right) \cdot \text{sec} \quad T_0 = 0.382 \text{ s}$$

$$S_{max}(T_e) := \begin{cases} \left( \frac{S_{xs}}{B_s} \right) \cdot \left( 0.4 + \frac{3 \cdot T_e}{T_0} \right) & \text{if } T_e \leq 0.2 \cdot T_0 \\ \frac{S_{x1} \cdot \text{sec}}{B_1 \cdot T_e} & \text{if } T_e > T_0 \\ \frac{S_{xs}}{B_s} & \text{otherwise} \end{cases}$$



P-delta by section 3.8.6 of fema 350 (2000, pg2-17)

$$P := W \quad R_f = 8 \quad \Delta = (2.824) \text{ in} \quad V_{xm} = (2.478) \text{ k} \quad h = (12) \text{ ft}$$

$$V_y := \frac{2 \cdot R_y \cdot F_y \cdot Z_{xc}}{h_1} \quad V_y = 17.722 \text{ k} \quad \psi := \frac{P_{x1} \cdot R_f \cdot \Delta_1}{V_y \cdot h_1} \quad \psi = 0.143$$

$\psi$  is less than one, structure is stable

Using linear static procedure of analysis as given

#### 4.4.3.2 period of structure (4-15)

$$T_a = 0.204 \text{ s}$$

#### 4.4.3.3.1 Pseudo lateral load, pg 4-16

$$\text{TS} := 0.2 \cdot T_0 \quad T_S = 0.076 \text{ s} \quad T_0 = 0.382 \text{ s}$$

$$C_1 := \begin{cases} 1 & \text{if } T_a \geq T_0 \\ 1.5 & \text{if } T_a \leq T_S \\ \text{Int}(T_S, 1.5, T_0, 1.0, T_a) & \text{otherwise} \end{cases} \quad C_1 = 1.291$$

$$C_2 := 1.0$$

$$C_{3IO} := 1 \quad C_{3CP} := 1.2 \quad \text{Table 4.4, pg 4-18}$$

$$W := \text{dlwf}_1 \quad W = 30 \text{ k} \quad S_a(T_a) = 0.645 \text{ g}$$

$$V_{IO} := C_1 \cdot C_2 \cdot C_{3IO} \cdot \frac{S_a(T_a)}{g} \cdot W \quad V_{IO} = 24.979 \text{ k}$$

$$V_{CP} := C_1 \cdot C_2 \cdot C_{3CP} \cdot \frac{S_a(T_a)}{g} \cdot W \quad V_{CP} = 29.974 \text{ k}$$

$$k_{cvx}(T) := \begin{cases} 1 & \text{if } T \leq 0.5\text{sec} \\ 2 & \text{if } T \geq 2.5\text{sec} \\ \text{Int}(0.5\text{sec}, 1, 2.5\text{sec}, 2, T) & \text{otherwise} \end{cases} \quad k_{cvx}(T) = 1.149$$

$$n := 1 \quad i := 1 .. n$$

$$\text{sum} := \sum_{i=1}^n \left[ \frac{w_i}{k} \cdot \left( \frac{h_i}{ft} \right)^{k_{cvx}(T)} \right] \quad \text{sum} = 520.897 \quad C_{vx_i} := \frac{\frac{w_i}{k} \cdot \left( \frac{h_i}{ft} \right)^{k_{cvx}(T)}}{\text{sum}} \quad C_{vx} = (1)$$

C.vx = 1 as expected for one story building

4.4.3.3.5: Interstory Drift  $k_f = (4.825) \frac{k}{in}$   
analysis uncertainty and demand variability factor from section 4.6

$$\text{From Table 4-8, } \gamma_{aIO} := 0.94 \quad \gamma_{aCP} := 0.70$$

$$\text{From Table 4-9, } \gamma_{IO} := 1.5 \quad \gamma_{CP} := 1.3$$

$$\text{From Table 4-10, } C_{IO} := 0.02 \quad C_{CP} := 0.10$$

$$\phi_{IO} := 1 \quad \phi_{CP} := 0.9$$

$$\text{From Table 4-12, } But_{IO} := 0.2 \quad But_{CP} := 0.3$$

$$\Delta_{IO} := \frac{V_{IO}}{kf_1} \cdot \gamma_{aIO} \cdot \gamma_{IO} \quad \Delta_{IO} = 7.3 \text{ in}$$

$$\Delta_{CP} := \frac{V_{CP}}{kf_1} \cdot \gamma_{aCP} \cdot \gamma_{CP} \quad \Delta_{CP} = 5.653 \text{ in}$$

### Drift Capacities

$$\Delta_{allIO} := C_{IO} \cdot \phi_{IO} \cdot h_1 \quad \Delta_{allIO} = 2.88 \text{ in}$$

$$\Delta_{allCP} := C_{CP} \cdot \phi_{CP} \cdot h_1 \quad \Delta_{allCP} = 12.96 \text{ in}$$

$$\lambda_{IO} := \frac{\Delta_{IO}}{\Delta_{allIO}} \quad \lambda_{IO} = 2.535 \quad \lambda_{CP} := \frac{\Delta_{CP}}{\Delta_{allCP}}$$

Immediate occupancy:  $\lambda_{IO} = 2.535$        $\text{But}_{IO} := 0.2$

$\lambda_{CP} = 0.436$        $\text{But}_{CP} := 0.3$

From Table 4-6, Confidence levels greater than 99% for both collapse prevention and immediate occupancy

$$P_{max} = 21.521 \text{ k} \quad P_{min} = 13.5 \text{ k} \quad M_{max} = 7.433 \text{ k}\cdot\text{ft} \quad V_{max} = 1.239 \text{ k}$$

### Part B. Analysis by Fema 350

Response spectrum from Fema 273

From 50% in 50 year hazard maps (2002 data from USGS java applet)

$$S_{0.05} := 0.0432 \text{g} \quad S_{0.1} := 0.0092 \text{g}$$

F273, 2.6.1.4, adjustment for site class (pg 2-21)

$$\text{SiteClass} := \text{"C"}$$

$$F_a := 1.2 \quad F_a = 1.2$$

$$F_v := 1.7 \quad F_v = 1.7$$

$$S_{xs} := F_a \cdot S_s \quad S_{xs} = 0.052 \text{ g} \quad S_{x1} := F_v \cdot S_1 \quad S_{x1} = 0.016 \text{ g}$$

F273, 2.6.1.5, general response spectrum

$$T_e := 0 \text{sec}, 0.001 \text{sec} \dots 15 \text{sec}$$

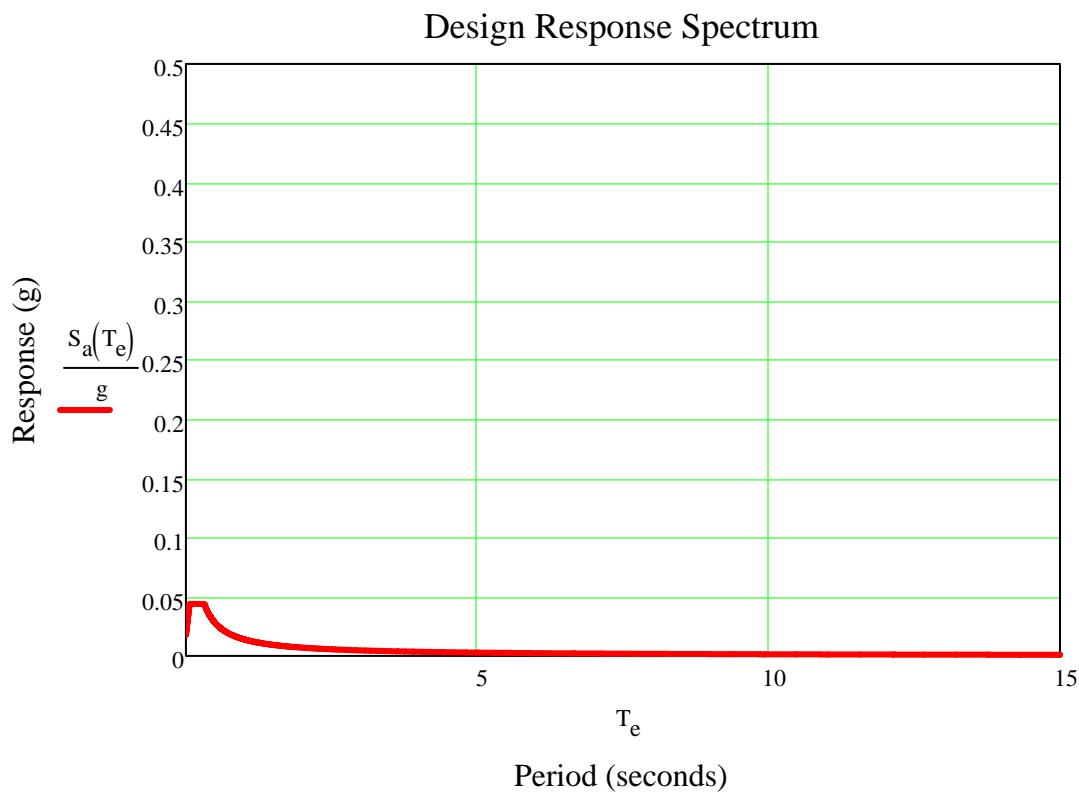
$$\beta := 100\zeta \quad \beta = 8$$

$$B_s := \text{Int}(5, 1.0, 10, 1.3, \beta) \quad B_s = 1.18$$

$$B_1 := \text{Int}(5, 1.0, 10, 1.2, \beta) \quad B_1 = 1.12$$

$$T_0 := \left( \frac{S_{x1} \cdot B_s}{S_{xs} \cdot B_1} \right) \cdot \text{sec} \quad T_0 = 0.318 \text{ s}$$

$$S_{xs}(T_e) := \begin{cases} \left( \frac{S_{xs}}{B_s} \right) \cdot \left( 0.4 + \frac{3 \cdot T_e}{T_0} \right) & \text{if } T_e \leq 0.2 \cdot T_0 \\ \frac{S_{x1} \cdot \text{sec}}{B_1 \cdot T_e} & \text{if } T_e > T_0 \\ \frac{S_{xs}}{B_s} & \text{otherwise} \end{cases}$$



P-delta by section 3.8.6 of fema 350 (2000, pg2-17)

$$\text{P} := W \quad R_f = 8 \quad \Delta = (2.824) \text{ in} \quad V_{xm} = (2.478) \text{ k} \quad h = (12) \text{ ft}$$

$$V_y := \frac{2 \cdot R_y \cdot F_y \cdot Z_{xc}}{h_1} \quad V_y = 17.722 \text{ k} \quad \psi := \frac{P_{x1} \cdot R_f \cdot \Delta_1}{V_y \cdot h_1} \quad \psi = 0.143$$

$\psi$  is less than one, structure is stable

Using linear static procedure of analysis as given

#### 4.4.3.2 period of structure (4-15)

$$T_a = 0.204 \text{ s}$$

#### 4.4.3.3.1 Pseudo lateral load, pg 4-16

$$T_S := 0.2 \cdot T_0 \quad T_S = 0.064 \text{ s} \quad T_0 = 0.318 \text{ s}$$

$$C_1 := \begin{cases} 1 & \text{if } T_a \geq T_0 \\ 1.5 & \text{if } T_a \leq T_S \\ \text{Int}(T_S, 1.5, T_0, 1.0, T_a) & \text{otherwise} \end{cases} \quad C_1 = 1.223$$

$$C_2 := 1.0$$

$$C_{3IO} := 1 \quad C_{3CP} := 1.2 \quad \text{Table 4.4, pg 4-18}$$

$$W := \text{dlwf}_1 \quad W = 30 \text{ k} \quad S_a(T_a) = 0.044 \text{ g}$$

$$V_{IO} := C_1 \cdot C_2 \cdot C_{3IO} \cdot \frac{S_a(T_a)}{g} \cdot W \quad V_{IO} = 1.612 \text{ k}$$

$$V_{CP} := C_1 \cdot C_2 \cdot C_{3CP} \cdot \frac{S_a(T_a)}{g} \cdot W \quad V_{CP} = 1.934 \text{ k}$$

$$k_{cvx}(T) := \begin{cases} 1 & \text{if } T \leq 0.5 \text{ sec} \\ 2 & \text{if } T \geq 2.5 \text{ sec} \\ \text{Int}(0.5 \text{ sec}, 1, 2.5 \text{ sec}, 2, T) & \text{otherwise} \end{cases} \quad k_{cvx}(T) = 1.149$$

$$\begin{aligned} n &:= 1 & i &:= 1 .. n \\ \text{sum} &:= \sum_{i=1}^n \left[ \frac{w_i}{k} \cdot \left( \frac{h_i}{ft} \right)^{k_{cvx}(T)} \right] & \text{sum} &= 520.897 \quad C_{vx_i} := \frac{\frac{w_i}{k} \cdot \left( \frac{h_i}{ft} \right)^{k_{cvx}(T)}}{\text{sum}} \quad C_{vx} = (1) \end{aligned}$$

C.vx = 1 as expected for one story building

4.4.3.3.5: Interstory Drift  $k_f = (4.825) \frac{k}{in}$   
analysis uncertainty and demand variability factor from section 4.6

From Table 4-8,  $\gamma_{aIO} := 0.94$   $\gamma_{aCP} := 0.70$

From Table 4-9,  $\gamma_{IO} := 1.5$   $\gamma_{CP} := 1.3$

From Table 4-10,  $C_{IO} := 0.02$   $C_{CP} := 0.10$

$$\phi_{IO} := 1 \quad \phi_{CP} := 0.9$$

From Table 4-12,  $But_{IO} := 0.2$   $But_{CP} := 0.3$

$$\Delta_{IO} := \frac{V_{IO}}{k_f_1} \cdot \gamma_{aIO} \cdot \gamma_{IO} \quad \Delta_{IO} = 0.471 \text{ in}$$

$$\Delta_{CP} := \frac{V_{CP}}{k_f} \cdot \gamma_{aCP} \cdot \gamma_{CP} \quad \Delta_{CP} = 0.365 \text{ in}$$

Drift Capacities

$$\Delta_{allIO} := C_{IO} \cdot \phi_{IO} \cdot h_1 \quad \Delta_{allIO} = 2.88 \text{ in}$$

$$\Delta_{allCP} := C_{CP} \cdot \phi_{CP} \cdot h_1 \quad \Delta_{allCP} = 12.96 \text{ in}$$

$$\lambda_{IO} := \frac{\Delta_{IO}}{\Delta_{allIO}} \quad \lambda_{IO} = 0.164 \quad \lambda_{CP} := \frac{\Delta_{CP}}{\Delta_{allCP}}$$

Immediate occupancy:  $\lambda_{IO} = 0.164$        $But_{IO} := 0.2$

$\lambda_{CP} = 0.028$        $But_{CP} := 0.3$

From Table 4-6, Confidence levels greater than 99% for both collapse prevention and immediate occupancy