CIVL 7111 - Special Modelling Project 12

Heat Transfer - Steady State Heat Conduction

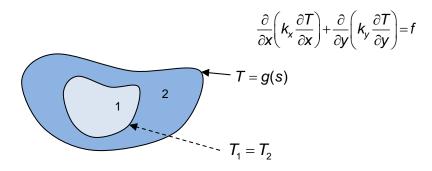
<u>Problem Statement</u> - Consider the problem of the steady state heat conduction. The general two-dimensional boundary-value problem is

$$\frac{\partial}{\partial x} \left(k_x \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left(k_y \frac{\partial T}{\partial y} \right) = f \quad \text{in } \Omega$$

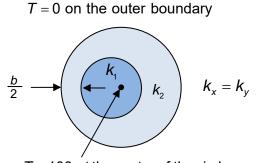
$$T = g(s) \quad \text{on } \Gamma$$

where the dependent variable T is the temperature and k_x and k_y are the thermal conductivites in the x and y directions.

Consider the a cross-section shown in the diagram below:



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T = 100 at the center of the circle

a = outer diameter = 1

b=inner diameter

$$\frac{a}{b}$$
 = 2 and 4

$$\frac{k_1}{k_2}$$
 = 1, 5, and 10

Use **POIS36** to the model this problem for the various cases indicated by the ratio a/b and k_1/k_2 . From these results plot the temperature over the doamin.