

| | | | | |
|--------|-------|---------|---|--|
| d = | 22.2 | in | Comp | |
| d' = | 2.5 | in | | |
| b = | 12 | in | Tension | |
| f'c = | 5000 | psi | | |
| fy = | 60000 | psi | 1 = Simply supported, 2=cantilevered beam | |
| WL = | 1.205 | k/ft | | |
| WD = | 1.21 | k/ft | Span | |
| 1 or 2 | 1 | | | |
| L = | 40 | ft | | |
| Mu = | 8112 | in.kips | | |
| β1 = | 0.8 | | | |

Choose c/d ratio

c/d = 0.300
 $\phi = 0.90$

$$\rho = 0.85\beta_1 \frac{c}{d} \frac{f'_c}{f_y}$$

$\rho = 0.0170$
 $A_s - A'_s = 4.53 \text{ in}^2$

$$A_{s1} = A_s - A'_s = \rho b d$$

a = 5.328

$$a = \frac{(A_s - A'_s) f_y}{0.85 f'_c b}$$

Mn = 5308 in.kips
 Mu2 = 4778 in.kips

$$M_{u2} = \phi (A_s - A'_s) f_y (d - a/2)$$

Mu1 = Mu - Mu2 = 3334 in.kips

Find the compression steel. First check to see if the compression steel will yield at failure

A's = 3.13 in²

$$M_{u1} = \phi (A'_s) f_y (d - d')$$

$$A'_s = \frac{M_{u1}}{\phi f_y (d - d')}$$

Find Find Tension Steel

As = 7.66 in²

$$A_s = (A_s - A'_s) + A'_s$$

Tension Steel

| No. | Bar size | |
|--------|----------|----------------------|
| 4 | 9 | 4.00 in ² |
| 4 | 9 | 4.00 in ² |
| -----> | | 8.00 in ² |

Compression Steel

| No. | Bar size | |
|-----|----------|----------------------|
| 4 | 8 | 3.16 in ² |

Check final design to see if the compression steel will yield with chosen design

Check to see if the compression steel yields at balanced condition

$$\frac{A_s - A'_s}{bd} \geq ? 0.85\beta_1 \frac{f'_c}{f_y} \frac{87}{87 - f_y} \frac{d'}{d}$$

if yes, the compression steel will yield at ultimate strength

| | | |
|-------------|------|--|
| (As-A's)/bd | >= ? | 0.85*beta_1 * (f'c/fy) * (d'/d) * (87000/(87000-fy)) |
| 0.0182 | No | 0.0206 |

Compression Steel does not yield

$A_s^{\min} =$

$$A_{\min} = \frac{3\sqrt{f'_c}}{f_y} bd \geq \frac{200}{f_y} bd$$

$A_s^{\min} = 0.94 \geq 0.888$

$A_s^{\min} = 0.94 \text{ in}^2$

$A_s^{\min} < A_s = 8.00$

----> Therefore it does satisfy the ACI code requirements

Chosen steel properties

| | | | |
|----------------|-------------------|-----------------|-------------|
| No. of bars = | 4 | Stirrup db = | 0.5 |
| bar size = | 9 | Stirrup # | 4 |
| bar diameter : | 1.128 inches | clear spacing = | 1.16 inches |
| bar area = | 1 in ² | bar spacing is | ok |
| width (b) = | 12 in | | |
| chosen cover | 1.5 | | |

Final moment capacity with the chosen dimensions and reinforcing steel

IF COMPRESSION STEEL YIELDS=

a = 5.69 in

c = 7.12 in

c/d = 0.321

$$a = \frac{(A_s - A'_s) f_y}{0.85 f'_c b}$$

Tension-Controlled - Satisfies ACI Code

M_{u1} = 3362 in.kips

$$M_{u1} = \phi(A'_s) f_y (d - d')$$

M_{u2} = 5058 in.kips

$$M_{u2} = \phi(A_s - A'_s) f_y (d - a/2)$$

M_u = M_{u1} + M_{u2}

M_u = 8420 in.kips

> 8112 in.kip

OK

IF COMPRESSION STEEL DOES NOT YIELD=

$$C_s = A'_s f'_s = A'_s \epsilon'_s E_s = A'_s \left(0.003 \frac{c - d'}{c} \right) E_s$$

$$C_c = 0.85 f'_c \beta_1 c b$$

$$T_s = A_s f_y$$

c = 7.33 in Equilibrium = 0 kips

| | Force | Arm | Moment |
|------|-------|-------|--------|
| Cs = | 181 | 19.70 | 3569 |
| Cc = | 299 | 19.27 | 5762 |
| Ts = | 480 | 0.00 | 0 |

Mn = 9331 in-kips
Mu = 8398 in-kips

> 8112 in.kip

OK

Mn = 778 ft-kips
Mu = 700 ft-kips

| | | | | |
|------------------|-------|---------|---------|---|
| d = | 22.2 | in | Comp | |
| d' = | 2.5 | in | | |
| b = | 12 | in | Tension | 1 = Simply supported, 2=cantilevered beam Span |
| f _c = | 5000 | psi | | |
| f _y = | 60000 | psi | | |
| W _L = | 1.205 | k/ft | | |
| W _D = | 1.21 | k/ft | | |
| 1 or 2 | 1 | | | |
| L = | 40 | ft | | |
| M _u = | 8112 | in.kips | | |
| β ₁ = | 0.8 | | | |

Choose c/d ratio

$$c/d = 0.375$$

$$\phi = 0.90$$

$$\rho = 0.85\beta_1 \frac{c}{d} \frac{f_c'}{f_y}$$

$$\rho = 0.0213$$

$$A_s - A'_s = 5.66 \text{ in}^2$$

$$A_{s1} = A_s - A'_s = \rho b d$$

$$a = 6.66$$

$$a = \frac{(A_s - A'_s) f_y}{0.85 f_c' b}$$

$$M_n = 6409 \text{ in.kips}$$

$$M_{u2} = 5747 \text{ in.kips}$$

$$M_{u2} = \phi (A_s - A'_s) f_y (d - a/2)$$

$$M_{u1} = M_u - M_{u2} = 2365 \text{ in.kips}$$

Find the compression steel. First check to see if the compression steel will yield at failure

$$A'_s = 2.23 \text{ in}^2$$

$$M_{u1} = \phi (A'_s) f_y (d - d')$$

$$A'_s = \frac{M_{u1}}{\phi f_y (d - d')}$$

Find Find Tension Steel

$$A_s = 7.89 \text{ in}^2$$

$$A_s = (A_s - A'_s) + A'_s$$

Tension Steel

| No. | Bar size | |
|--------|----------|----------------------|
| 4 | 9 | 4.00 in ² |
| 4 | 9 | 4.00 in ² |
| -----> | | 8.00 in ² |

Compression Steel

| No. | Bar size | |
|-----|----------|----------------------|
| 3 | 8 | 2.37 in ² |

Check final design to see if the compression steel will yield with chosen design
 Check to see if the compression steel yields at balanced condition

$$\frac{A_s - A'_s}{bd} \geq ? 0.85\beta_1 \frac{f'_c}{f_y} \frac{87}{87 - f_y} \frac{d'}{d}$$

if yes, the compression steel will yield at ultimate strength

| | | |
|-------------------|----------|--|
| $(A_s - A'_s)/bd$ | $\geq ?$ | $0.85 \cdot \beta_1 \cdot (f'_c/f_y) \cdot (d'/d) \cdot (87000/(87000 - f_y))$ |
| 0.0211 | Yes | 0.0206 |

Compression Steel Yields

$A_s^{\min} =$

$$A_{\min} = \frac{3\sqrt{f'_c}}{f_y} bd \geq \frac{200}{f_y} bd$$

$A_s^{\min} = 0.94 \geq 0.888$

$A_s^{\min} = 0.94 \text{ in}^2$

$A_s^{\min} < A_s = 8.00$

----> Therefore it does satisfy the ACI code requirements

Chosen steel properties

| | | | |
|----------------|-------------------|-----------------|-------------|
| No. of bars = | 4 | Stirrup db = | 0.5 |
| bar size = | 9 | Stirrup # | 4 |
| bar diameter : | 1.128 inches | | |
| bar area = | 1 in ² | clear spacing = | 1.16 inches |
| width (b) = | 12 in | | |
| chosen cover | 1.5 | bar spacing is | ok |

Final moment capacity with the chosen dimensions and reinforcing steel

IF COMPRESSION STEEL YIELDS=

a = 6.62 in

c = 8.28 in

c/d = 0.373

$$a = \frac{(A_s - A'_s) f_y}{0.85 f'_c b}$$

Tension-Controlled - Satisfies ACI Code

M_{u1} = 2512 in.kips

$$M_{u1} = \phi (A'_s) f_y (d - d')$$

M_{u2} = 5721 in.kips

$$M_{u2} = \phi (A_s - A'_s) f_y (d - a/2)$$

M_u = M_{u1} + M_{u2}

M_u = 8233 in.kips

> 8112 in.kip

OK

IF COMPRESSION STEEL DOES NOT YIELD=

$$C_s = A'_s f'_s = A'_s \epsilon'_s E_s = A'_s \left(0.003 \frac{c - d'}{c} \right) E_s$$

$$C_c = 0.85 f'_c \beta_1 c b$$

$$T_s = A_s f_y$$

c = 7.33 in Equilibrium = -45 kips

| | Force | Arm | Moment |
|------|-------|-------|--------|
| Cs = | 136 | 19.70 | 2677 |
| Cc = | 299 | 19.27 | 5762 |
| Ts = | 480 | 0.00 | 0 |

Mn = 8439 in-kips

Mu = 7567 in-kips

> 8112 in.kip

Length Requirement

Mn = 703 ft-kips

Mu = 631 ft-kips

6.9. Example: Design of a member to satisfy a nominal moment capacity.

A doubly reinforced concrete beam section has a maximum effective depth $d = 25$ in and is subjected to a total factored moment $M_u = 9400$ in-kips, including self weight. Design the section and select the appropriate reinforcement at the tension and the compression faces to carry the required load.

$$f_y = 60,000 \text{ psi}$$

$$f_c' = 4,000 \text{ psi}$$

$$\text{Required } M_n = 9,400 \text{ in-k}$$

Solution

Assume that $b = 14$ in. $= 0.55 d$

See the following pages for design done in a spreadsheet.

| | | | | |
|------------------|-------|---------|---|--|
| d = | 25 | in | Comp | |
| d' = | 2.5 | in | | |
| b = | 14 | in | Tension | |
| f _c = | 4000 | psi | | |
| f _y = | 60000 | psi | 1 = Simply supported, 2=cantilevered beam | |
| W _L = | 1.4 | k/ft | | |
| W _D = | 1.4 | k/ft | Span | |
| 1 or 2 | 1 | | | |
| L = | 40 | ft | | |
| M _u = | 9408 | in.kips | | |
| β ₁ = | 0.85 | | | |

Choose c/d ratio

c/d = 0.333
 $\phi = 0.90$

$$\rho = 0.85\beta_1 \frac{c}{d} \frac{f'_c}{f_y}$$

$\rho = 0.0160$
 $A_s - A'_s = 5.61 \text{ in}^2$

$$A_{s1} = A_s - A'_s = \rho b d$$

a = 7.07625

$$a = \frac{(A_s - A'_s) f_y}{0.85 f'_c b}$$

M_n = 7229 in.kips
M_{u2} = 6506 in.kips

$$M_{u2} = \phi (A_s - A'_s) f_y (d - a/2)$$

M_{u1} = M_u - M_{u2} = 2902 in.kips

Find the compression steel. First check to see if the compression steel will yield at failure

A'_s = 2.39 in²

$$M_{u1} = \phi (A'_s) f_y (d - d')$$

$$A'_s = \frac{M_{u1}}{\phi f_y (d - d')}$$

Find Find Tension Steel

A_s = 8.00 in²

$$A_s = (A_s - A'_s) + A'_s$$

Tension Steel

| No. | Bar size | |
|--------|----------|----------------------|
| 4 | 9 | 4.00 in ² |
| 4 | 9 | 4.00 in ² |
| -----> | | 8.00 in ² |

Compression Steel

| No. | Bar size | |
|-----|----------|----------------------|
| 4 | 7 | 2.40 in ² |

Check final design to see if the compression steel will yield with chosen design

Check to see if the compression steel yields at balanced condition

$$\frac{A_s - A'_s}{bd} \geq ? 0.85\beta_1 \frac{f'_c}{f_y} \frac{87}{87 - f_y} \frac{d'}{d}$$

if yes, the compression steel will yield at ultimate strength

(As-A's)/bd >= ? 0.85*beta_1 * (f'c/fy) * (d'/d)*(87000/(87000-fy))
 0.0160 Yes 0.0155

Compression Steel Yields

$A_s^{min} =$

$$A_{min} = \frac{3\sqrt{f'_c}}{f_y} bd \geq \frac{200}{f_y} bd$$

$A_s^{min} = 1.11 \geq 1.166666667$

$A_s^{min} = 1.17 \text{ in}^2$

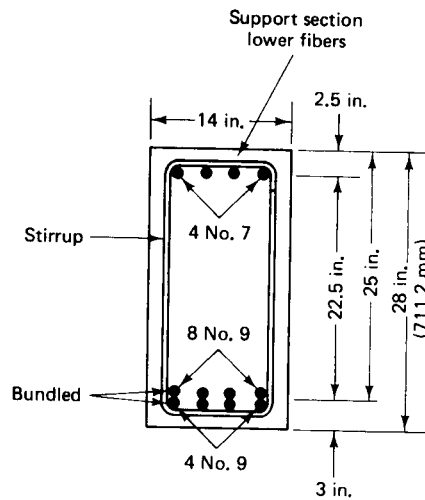
$A_s^{min} < A_s = 8.00$

---->

Therefore it does satisfy the ACI code requirements

Chosen steel properties

| | | | |
|----------------|-------------------|-----------------|-------------|
| No. of bars = | 4 | Stirrup db = | 0.5 |
| bar size = | 9 | Stirrup # | 4 |
| bar diameter : | 1.128 inches | | |
| bar area = | 1 in ² | clear spacing = | 1.83 inches |
| width (b) = | 14 in | | |
| chosen cover | 1.5 | bar spacing is | ok |



Final moment capacity with the chosen dimensions and reinforcing steel

IF COMPRESSION STEEL YIELDS=

a = 7.06 in

c = 8.30 in

c/d = 0.332

$$a = \frac{(A_s - A'_s) f_y}{0.85 f'_c b}$$

Tension-Controlled - Satisfies ACI Code

$$M_{u1} = \phi (A'_s) f_y (d - d')$$

M_{u1} = 2916 in.kips

$$M_{u2} = \phi (A_s - A'_s) f_y (d - a/2)$$

M_{u2} = 6493 in.kips

M_u = M_{u1} + M_{u2}

M_u = 9409 in.kips

> 9408 in.kip

OK

IF COMPRESSION STEEL DOES NOT YIELD=

$$C_s = A'_s f'_s = A'_s \epsilon'_s E_s = A'_s \left(0.003 \frac{c - d'}{c} \right) E_s$$

$$C_c = 0.85 f'_c \beta_1 c b$$

$$T_s = A_s f_y$$

c = 7.33 in Equilibrium = -46 kips

| | Force | Arm | Moment |
|------|-------|-------|--------|
| Cs = | 138 | 22.50 | 3096 |
| Cc = | 297 | 21.88 | 6490 |
| Ts = | 480 | 0.00 | 0 |

Mn = 9586 in-kips
 Mu = 8627 in-kips

> 9408 in.kip

Length Requirement

Mn = 799 ft-kips
 Mu = 719 ft-kips