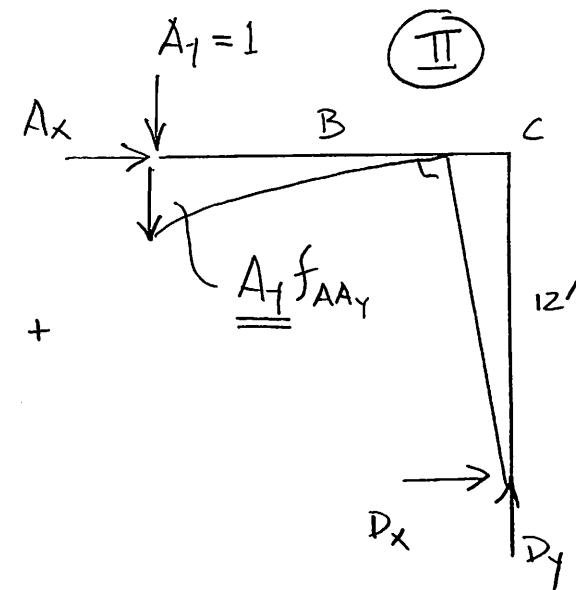
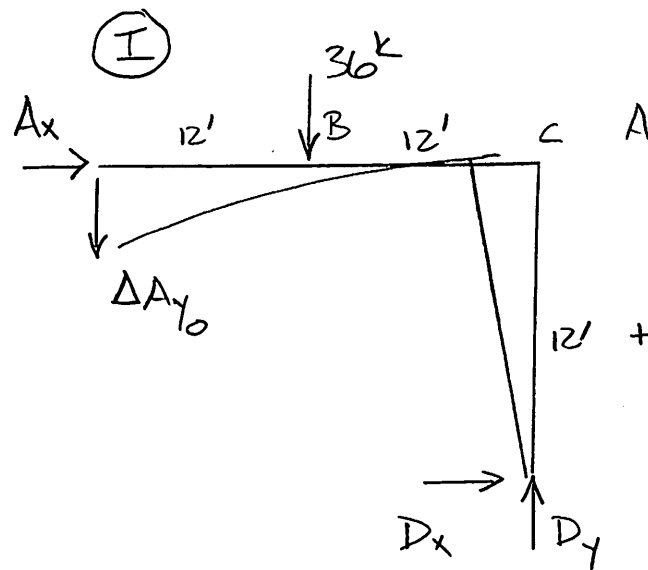
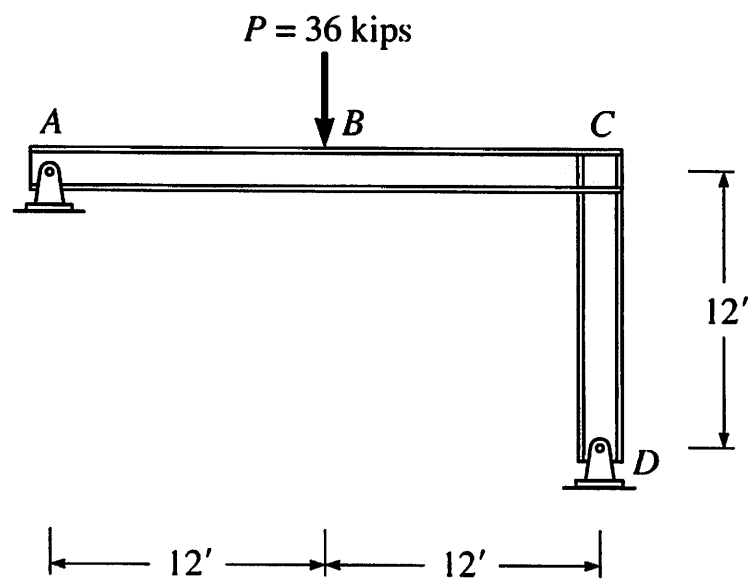


Problem 9b-2 – Compute the reactions for the following frame. Assume A_y is the redundant force.



$$\Delta A_y = 0 = \Delta A_{y_0} + A_1 f_{AA_y}$$

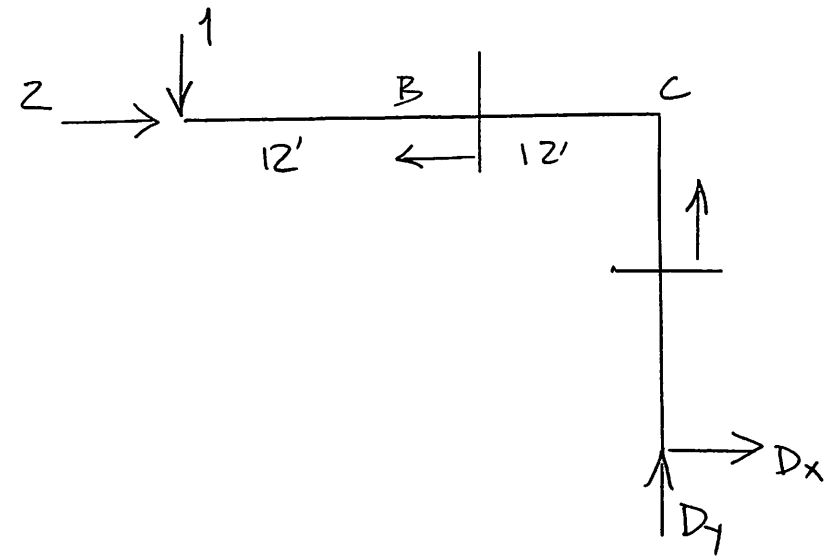
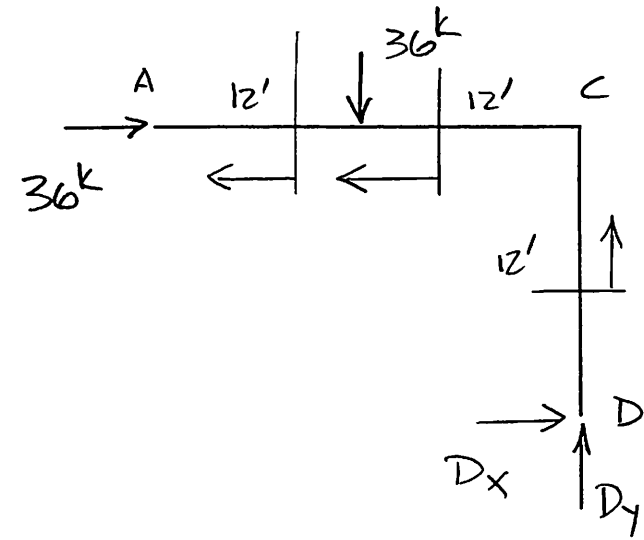
$$\textcircled{\text{I}} \quad \sum M_D = 0 = 36^k(12') - A_x(12')$$

$$\underline{A_x = 36^k}$$

$$\textcircled{\text{II}} \quad \sum M_D = 0 = 1(24') - A_x(12')$$

$$\underline{A_x = 2}$$

Problem 9b-2 – Compute the reactions for the following beam.



SECTION AB

$$\sum M_{cut} = 0$$

$$= M_{AB} = 0$$

SECTION BC

$$\sum M_{cut} = 0$$

$$= M_{BC} + 36(x_1)$$

$$M_{BC} = -36x_1$$

SECTION CD

$$\sum M_{cut} = 0$$

$$= M_{CD} + 36(12') - 36(y_1)$$

$$M_{CD} = 36(y_1 - 12)$$

SECTION AB

$$\sum M_{cut} = 0$$

$$= M_{AB} + 1(x) \quad M_{AB} = -x$$

SECTION BC

$$\sum M_{cut} = 0$$

$$= M_{BC} + 1(x_1 + 12)$$

$$M_{BC} = -(12 + x_1)$$

SECTION CD

$$\sum M_{cut} = 0$$

$$= M_{CD} + 1(24') - 2(y_1)$$

$$M_{CD} = 2y_1 - 24$$

$$= 2(y_1 - 12)$$

Problem 9b-2 – Compute the reactions for the following beam.

$$EI \Delta A_{y_0} = \int_0^{12} (-36x_1)(12+x_1) dx_1 + \int_0^{12} 72(y_1-12)^2 dy_1$$

$$= \left[216x_1^2 + 12x_1^3 \right]_0^{12} + 72 \left[\frac{y_1^3}{3} - 12y_1^2 + 144y_1 \right]_0^{12} = \underline{93,312 \text{ k ft}^3}$$

$$EI f_{AA_y} = \int_0^{12} (-x)^2 dx + \int_0^{12} (12+x)^2 dx + \int_0^{12} 4(y-12)^2 dy$$

$$= \left. \frac{x_1^3}{3} \right|_0^{12} + \left[144x_1 + 12x_1^2 + \frac{x_1^3}{3} \right]_0^{12} + 4 \left[\frac{y_1^3}{3} - 12y_1^2 + 144y_1 \right]_0^{12} = \underline{6,912 \text{ ft}^3}$$

$$A_y = \frac{\Delta A_{y_0}}{f_{AA}} = \underline{13.5 \text{ k}}$$

$$\circlearrowleft \sum M_D = 0 = 36 \text{ k}(12') - 13.5 \text{ k}(24') - A_x(12')$$

$$\underline{A_x = 9 \text{ k}}$$

$$+\uparrow \sum F_y = 0 = D_y + 13.5 \text{ k} - 36 \text{ k} \quad \underline{D_y = 22.5 \text{ k}}$$

$$+\rightarrow \sum F_x = 0 = A_x + D_x \quad \underline{D_x = -9 \text{ k}}$$

