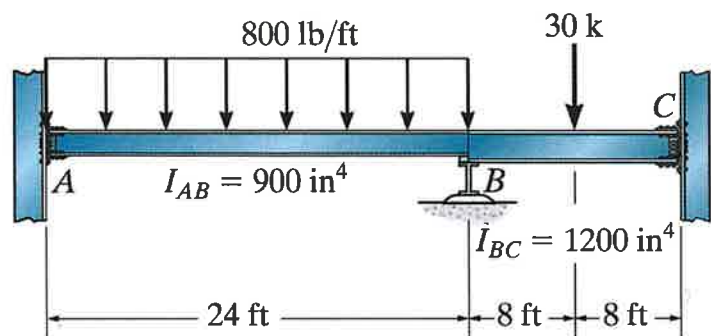


Problem 10a-4 – Determine the moments at A, B, and C. Assume A and C are fixed, B is a roller, and EI is constant.



$$I_{AB} = \frac{3}{4} I_{BC} \quad I_{BC} = \frac{4}{3} I_{AB}$$

$$FEM_{AB} \left(\text{Diagram of beam AB with UDL} \right) \frac{WL^2}{12}$$

$$\frac{800 \text{ lb/ft} (24')^2}{12} = \pm 38.4 \text{ kft}$$

$$FEM_{BC} \left(\text{Diagram of beam BC with point load P at center} \right) \frac{PL}{8}$$

$$\frac{30 \text{ k} (16')}{8} = \pm 60 \text{ kft}$$

$$M_{AB} = \frac{2EI_{AB}}{L_{AB}} \left[2\theta_A + \theta_B - \frac{3\Delta}{4} \right] - 38.4 \text{ kft} \quad (1)$$

$$M_{BA} = \frac{2EI_{AB}}{L_{AB}} \left[2\theta_B + \theta_A - \frac{3\Delta}{4} \right] + 38.4 \text{ kft} \quad (2)$$

$$M_{BC} = \frac{2E(\frac{4}{3}I_{AB})}{L_{BC}} \left[2\theta_B + \theta_C - \frac{3\Delta}{4} \right] - 60 \text{ kft} \quad (3)$$

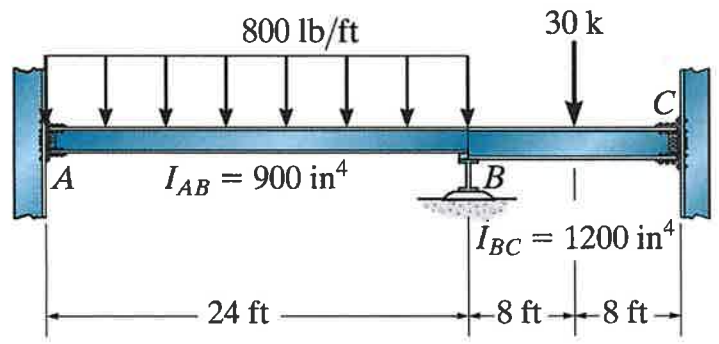
$$M_{CB} = \frac{2E(\frac{4}{3}I_{AB})}{L_{BC}} \left[2\theta_C + \theta_B - \frac{3\Delta}{4} \right] + 60 \text{ kft} \quad (4)$$

JOINT B

$$\begin{aligned} M_{BA} \quad M_{BC} \quad \sum M_B = 0 \\ = -M_{BA} - M_{BC} \end{aligned}$$

$$M_{BA} + M_{BC} = 0 \quad (5)$$

Problem 10a-4 – Determine the moments at A, B, and C. Assume A and C are fixed, B is a roller, and EI is constant.



$$M_{BA} + M_{BC} = 0 = \underbrace{\frac{2EI_{AB}}{24 \text{ ft}} [2\theta_B] + 38.4 \text{ kft}}_{M_{BA}} + \underbrace{\frac{2E(\frac{4}{3}I_{AB})}{16 \text{ ft}} [2\theta_B] - 60 \text{ kft}}_{M_{BC}}$$

$$\frac{1}{2}\theta_B = \frac{21.6 \text{ kft}^2}{EI_{AB}} \qquad \theta_B = \frac{43.2 \text{ kft}^2}{EI_{AB}}$$

$$M_{AB} = \frac{2EI_{AB}}{24 \text{ ft}} [\theta_B] - 38.4 \text{ kft} = \underline{-34.8 \text{ kft}}$$

$$M_{BA} = \frac{2EI_{AB}}{24 \text{ ft}} [2\theta_B] + 38.4 \text{ kft} = \underline{45.6 \text{ kft}}$$

$$M_{BC} = \frac{2E(\frac{4}{3}I_{AB})}{16 \text{ ft}} [2\theta_B] - 60 \text{ kft} = \underline{-45.6 \text{ kft}}$$

$$M_{CB} = \frac{2E(\frac{4}{3}I_{AB})}{16 \text{ ft}} [\theta_B] + 60 \text{ kft} = \underline{67.2 \text{ kft}}$$