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### Chapter 3.6 – Design

- The **design of a tension member** involves finding a member with **adequate gross and net areas**.
- If the member has a bolted connection, the selection of a suitable cross-section requires an accounting for the **area lost because of holes**.
- For a member with a rectangular cross-section, the calculations are relatively straightforward.
- If a rolled shape is to be used, however, the area to be **deducted cannot be predicted in advance** because the member's thickness at the location of the holes is not known.

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### Chapter 3.6 – Design

- A secondary consideration in the design of tension members is **slenderness**.
- If a structural member has a small cross-section in relation to its length, it is said to be **slender**.
- A more precise measure is the **slenderness ratio,  $L/r$** , where  $L$  is the member length and  $r$  is the minimum radius of gyration of the cross-sectional area.
- The minimum radius of gyration is the one corresponding to the minor principal axis of the cross-section.

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### Chapter 3.6 – Design

- Although **slenderness** is critical to the strength of a **compression** member, it is inconsequential for a tension member.
- In many situations, however, it is **good practice** to limit the slenderness of tension members.

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**CHAPTER D**  
DESIGN OF MEMBERS FOR TENSION

D1. SLENDERNESS LIMITATIONS

There is no maximum slenderness limit for members in tension.

**User Note:** For members designed on the basis of tension, the slenderness ratio of the member as fabricated—taken as the fabricated length of the member, divided by the least radius of gyration of the section—preferably should not exceed 300. This suggestion does not apply to rods.

$$\frac{L}{r} \leq 300$$

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### Chapter 3.6 – Design

- It is only a recommended value because **slenderness** has no structural significance for tension members.
- This limit does not apply to **cables**, and the user note explicitly excludes **rods**.

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**CHAPTER D**  
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D1. SLENDERNESS LIMITATIONS

There is no maximum slenderness limit for members in tension.

**User Note:** For members designed on the basis of tension, the slenderness ratio of the member as fabricated—taken as the fabricated length of the member, divided by the least radius of gyration of the section—preferably should not exceed 300. This suggestion does not apply to rods.

$$\frac{L}{r} \leq 300$$

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### Chapter 3.6 – Design

- The central problem of all member **design**, including tension member design, is to **find a cross-section** for which the required strength does not exceed the available strength.
- For tension members designed by **LFRD**, the requirement is

$$P_u \leq \phi_t P_n \quad \text{or} \quad \phi_t P_n \geq P_u$$

where  $P_u$  is the sum of the factored loads.

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### Chapter 3.6 – Design

- To prevent **yielding**,
 
$$0.90F_y A_g \geq P_u \quad \text{or} \quad A_g \geq \frac{P_u}{0.90F_y}$$
- To prevent **rupture**,
 
$$0.75F_u A_e \geq P_u \quad \text{or} \quad A_e \geq \frac{P_u}{0.75F_u}$$
- The **slenderness ratio** limitation will be satisfied if:
 
$$r \geq \frac{L}{300}$$

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### Chapter 3.6 – Design

- For **ASD**, if we use the allowable **stress** form, the requirement corresponding to **yielding** is
 
$$P_a \leq F_t A_g$$

$$A_g \geq \frac{P_a}{F_t} \quad \text{or} \quad A_g \geq \frac{P_a}{0.6F_y}$$
- For the limit state of **rupture**, the required effective area is
 
$$A_e \geq \frac{P_a}{F_t} \quad \text{or} \quad A_e \geq \frac{P_a}{0.5F_u}$$

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### Chapter 3.6 – Design

- **Example 3.11:** A tension member with a length of 6 ft. must resist a service dead load of 15 k and a service live load of 45 k.
- Select a member with a **rectangular cross-section**. Use **A36** steel and assume a connection with one line of 1/2-in bolts.
- For **LRFD**:
 
$$P_u = 1.2D + 1.6L = 1.2(15k) + 1.6(45k) = 90 \text{ k}$$

$$A_g = \frac{P_u}{0.90F_y} = \frac{90k}{0.90(36\text{ksi})} = 2.778 \text{ in}^2$$

$$A_e \geq \frac{P_u}{0.75F_u} = \frac{90k}{0.75(58\text{ksi})} = 2.069 \text{ in}^2$$

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### Chapter 3.6 – Design

- **Example 3.11:** Let's try a thickness of **t = 1 in.**

$$w_g = \frac{\text{required } A_g}{t} = \frac{2.778 \text{ in}^2}{1 \text{ in.}} = 2.778 \text{ in.}$$

Let's try a **1 in. x 3 in.** cross-section

$$A_g = (1.00 \text{ in})(3.00 \text{ in}) = 3.00 \text{ in}^2$$

Is trial **A<sub>g</sub>** > required **A<sub>g</sub>**?  $3.00 \text{ in}^2 > 2.778 \text{ in}^2$  **OK**

$$d_{\text{hole}} = d_{\text{bolt}} + \frac{1}{8} \text{ in.} = (\frac{1}{2} \text{ in.}) + (\frac{1}{8} \text{ in.}) = \frac{5}{8} \text{ in.}$$

$$A_e = A_n = A_g - A_{\text{holes}} = 3.00 \text{ in}^2 - (1 \text{ in.})(\frac{5}{8} \text{ in.})(1 \text{ hole}) = 2.375 \text{ in}^2$$

Is trial **A<sub>e</sub>** > required **A<sub>e</sub>**?  $2.375 \text{ in}^2 > 2.069 \text{ in}^2$  **OK**

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### Chapter 3.6 – Design

- **Example 3.11:** Check the slenderness ratio
 
$$I_{\min} = \frac{wt^3}{12} = \frac{(3.00 \text{ in.})(1 \text{ in.})^3}{12} = 0.250 \text{ in}^4$$

$$r_{\min} = \sqrt{\frac{I_{\min}}{A}} = \sqrt{\frac{0.250 \text{ in}^4}{3.00 \text{ in}^2}} = 0.2887 \text{ in.}$$

$$\frac{L}{r_{\min}} = \frac{72 \text{ in.}}{0.2887 \text{ in.}} = 249.4$$

Is trial **r/L** < 300?  $249.4 < 300$  **OK**

Use a **PL1.0 x 3.0**

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### Chapter 3.6 – Design

- The member in Example 3.11 is **less than 8 in. wide** and thus is classified as a **bar** rather than a **plate**.
- Bars should be specified to the **nearest 1/4-inch in width** and to the **nearest 1/8-inch in thickness**.
- The classification system is given in **Part 1 of the Manual** page 1-9 under the heading "Plate and Bar Products."
- It is common practice to use the **PL** (Plate) designation for both bars and plates.

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## Chapter 3.6 – Design

➤ **Part 1 of the Manual page 1-9 “Plate and Bar Products.”**

STRUCTURAL PRODUCTS 1-9

**Plate and Bar Products**

Plate products may be ordered as sheet, strip, or bar material. Sheet and strip are distinguished from structural bars and plates by their dimensional characteristics, as outlined in Table 2-3 and Table 2-5.

The historical classification system for structural bars and plates suggests that there is only a physical difference between them based upon size and production procedure. In raw form, flat stock has historically been classified as a bar if it is less than or equal to 8 in. wide and as a plate if it is greater than 8 in. wide. Bars are rolled between horizontal and vertical rolls and trimmed to length by shearing or thermal cutting on the ends only. Plates are generally produced using one of two methods:

1. Sheared plates are rolled between horizontal rolls and trimmed to width and length by shearing or thermal cutting on the edges and ends; or
2. Stripped plates are sheared or thermal cut from wider sheared plates.

There is very little, if any, structural difference between plates and bars. Consequently, the term plate is becoming a universally applied term today, and a  $PL\frac{1}{2}\times 4\frac{1}{2}\times 18\ 3$  in., for example, might be fabricated from plate or bar stock.

For structural plates, the preferred practice is to specify thickness in  $\frac{1}{8}$  in. increments up to  $\frac{3}{8}$  in. thickness,  $\frac{1}{4}$  in. increments over  $\frac{3}{8}$  in. to 1 in. thickness, and  $\frac{1}{2}$  in. increments over 1 in. thickness. The current extreme width for sheared plates is 200 in. Because mill practice regarding plate widths vary, individual mills should be consulted to determine preferences.

For bars, the preferred practice for squares and rectangles is to specify width in  $\frac{1}{4}$  in. increments, and thickness in  $\frac{1}{8}$  in. increments, for rounds, diameter in  $\frac{1}{8}$  in. increments.

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## Chapter 3.6 – Design

- If an **angle** shape is used as a tension member and the connection is made by bolting, there must be enough room for the bolts.
- Space will be a problem only when there are two lines of bolts in a leg.
- The usual fabrication practice is to punch or drill holes in standard locations in the angle legs.

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➤ These hole locations are given in **Table 1-7A “Workable Gages in Angle Legs”** in **Part 1 of the Manual, page 1-52.**

**Table 1-7A**  
**Workable Gages in Angle Legs, in.**

$g$	Leg	12	10	8	7	6	5	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1 $\frac{1}{8}$	1 $\frac{1}{4}$	1
$g$		6	5	4 $\frac{1}{2}$	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1	$\frac{7}{8}$	$\frac{3}{4}$	$\frac{3}{8}$	$\frac{1}{4}$	$\frac{1}{8}$
$g_1$		3	3	3	2 $\frac{1}{2}$	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_2$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	3	3	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_3$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—
$g_4$		2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—

Note: Other gages are permitted to suit specific requirements subject to clearances and edge distance limitations.

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## Chapter 3.6 – Design

- Gage distance  $g$  applies when there is one line of bolts
- Gage distances  $g_1$  and  $g_2$  apply when there are two lines.

**Table 1-7A**  
**Workable Gages in Angle Legs, in.**

$g$	Leg	12	10	8	7	6	5	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1 $\frac{1}{8}$	1 $\frac{1}{4}$	1
$g$		6	5	4 $\frac{1}{2}$	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1	$\frac{7}{8}$	$\frac{3}{4}$	$\frac{3}{8}$	$\frac{1}{4}$	$\frac{1}{8}$
$g_1$		3	3	3	2 $\frac{1}{2}$	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_2$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	3	3	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_3$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—
$g_4$		2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—

Note: Other gages are permitted to suit specific requirements subject to clearances and edge distance limitations.

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## Chapter 3.6 – Design

- The values  $g_1$ ,  $g_2$ , and  $g_3$  apply are for three lines.
- The values  $g_1$ ,  $g_2$ ,  $g_3$ , and  $g_4$  apply are for four lines.

**Table 1-7A**  
**Workable Gages in Angle Legs, in.**

$g$	Leg	12	10	8	7	6	5	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1 $\frac{1}{8}$	1 $\frac{1}{4}$	1
$g$		6	5	4 $\frac{1}{2}$	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1	$\frac{7}{8}$	$\frac{3}{4}$	$\frac{3}{8}$	$\frac{1}{4}$	$\frac{1}{8}$
$g_1$		3	3	3	2 $\frac{1}{2}$	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_2$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	3	3	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_3$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—
$g_4$		2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—

Note: Other gages are permitted to suit specific requirements subject to clearances and edge distance limitations.

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## Chapter 3.6 – Design

➤ The table shows that a:

- 5-inch** leg is needed to accommodate two lines,
- 10-inch** leg is needed for three lines, and
- 12-inch** leg is needed for four lines.

**Table 1-7A**  
**Workable Gages in Angle Legs, in.**

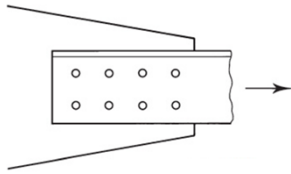
$g$	Leg	12	10	8	7	6	5	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1 $\frac{1}{8}$	1 $\frac{1}{4}$	1
$g$		6	5	4 $\frac{1}{2}$	4	3 $\frac{1}{2}$	3	2 $\frac{1}{2}$	2	1 $\frac{3}{4}$	1 $\frac{1}{2}$	1	$\frac{7}{8}$	$\frac{3}{4}$	$\frac{3}{8}$	$\frac{1}{4}$	$\frac{1}{8}$
$g_1$		3	3	3	2 $\frac{1}{2}$	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_2$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	3	3	2 $\frac{1}{2}$	2	—	—	—	—	—	—	—	—	—	—
$g_3$		2 $\frac{1}{2}$	2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—
$g_4$		2 $\frac{1}{2}$	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—

Note: Other gages are permitted to suit specific requirements subject to clearances and edge distance limitations.

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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- Use **A572 Grade 50** with two lines of 3/8-in bolts.



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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- For **LRFD**:

$$P_u = 1.2D + 1.6L = 1.2(35k) + 1.6(75k) = 162.0 k$$

$$A_g = \frac{P_u}{0.90F_y} = \frac{162.0k}{0.90(50ksf)} = 3.600 \text{ in}^2$$

$$A_e = \frac{P_u}{0.75F_u} = \frac{162.0k}{0.75(65ksf)} = 3.323 \text{ in}^2$$

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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- The radius of gyration should be at least:

$$\frac{L}{300} = \frac{144 \text{ in.}}{300} = 0.480 \text{ in}$$

- To find the **lightest shape** that satisfies these criteria, we search the dimensions and properties table for the unequal-leg angle that has the **smallest acceptable gross area** and then check the **effective net area**.

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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- The radius of gyration should be at least:

$$\frac{L}{300} = \frac{144 \text{ in.}}{300} = 0.480 \text{ in}$$

- The radius of gyration can be checked by inspection.
- There are two lines of bolts, so the connected leg must be at least **5 inches long** (see **AISC Table 1-7A**).

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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- The radius of gyration should be at least:

$$\frac{L}{300} = \frac{144 \text{ in.}}{300} = 0.480 \text{ in}$$

- Starting at either end of the table, we find that the shape with the **smallest area** that is at least equal to **3.60 in<sup>2</sup>** and a minimum radius of gyration of **0.48 in**.

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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- Let's try a **L5 x 3 x 1/2**  $A_g = 3.75 \text{ in}^2 > 3.60 \text{ in}^2$

Table 1-7 (continued)  
Angles  
Properties

Shape	k	Wt.	Area, A	Axis X-X						Flexural-Torsional Properties		
				I	S	r	y-bar	Z	J	C <sub>w</sub>	r <sub>p</sub>	
	in	lb/ft	in <sup>2</sup>	in <sup>4</sup>	in <sup>3</sup>	in	in	in <sup>3</sup>	in	in <sup>4</sup>	in <sup>6</sup>	in
L5x3x1/2	1 1/4	12.8	3.75	4.43	2.89	1.58	1.74	5.12	1.25	0.322	0.454	2.38
x3/8	1 1/4	9.80	2.86	7.35	2.22	1.60	1.69	3.93	1.19	0.141	0.196	2.41
x3/8	3/4	8.20	2.41	6.24	1.87	1.61	1.67	3.32	1.14	0.0832	0.116	2.42
x1/2	1 1/4	6.60	1.94	5.09	1.51	1.62	1.64	2.68	1.12	0.0438	0.0606	2.43

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### Chapter 3.6 – Design

- **Example 3.12:** Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- Let's try a **L5 x 3 x 1/2**  $A_g = 3.75 \text{ in}^2$   $r_{\min} = 0.642 \text{ in}$

Table 1-7 (continued)  
Angles  
Properties  
L5-L3 1/2

Shape	Axis Y-Y					Axis Z-Z					Tan α
	I	S	r	$\bar{x}$	Z	I	S	r	Tan α		
L5x3x1/2	2.55	1.13	0.824	0.746	2.08	0.375	1.55	0.957	0.642	0.357	
x3/4	2.29	1.00	0.831	0.722	1.82	0.331	1.37	0.980	0.664	0.361	
x3/8	2.01	0.874	0.838	0.698	1.57	0.296	1.20	0.727	0.646	0.354	
x1/2	1.72	0.739	0.846	0.673	1.31	0.241	1.01	0.606	0.649	0.368	
x3/8	1.41	0.600	0.853	0.648	1.05	0.194	0.825	0.491	0.652	0.371	

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### Chapter 3.6 – Design

- **Example 3.12:**
- $d_{hole} = d_{bolt} + \frac{1}{8} \text{ in.} = (\frac{7}{8} \text{ in.}) + (\frac{1}{8} \text{ in.}) = 1 \text{ in.}$
- $A_n = A_g - A_{holes} = 3.75 \text{ in}^2 - (\frac{1}{2} \text{ in.})(1 \text{ in.})(2 \text{ holes}) = 2.75 \text{ in}^2$
- Because the length of the connection is not known, we cannot compute the shear lag factor U.
- Since there are four bolts in the direction of the load, we will use the alternative value of **U = 0.80**.
- $A_e = A_n U = (0.80)2.75 \text{ in}^2 = 2.200 \text{ in}^2$
- Is  $A_e >$  required  $A_e$ ?  $2.200 \text{ in}^2 < 3.323 \text{ in}^2$  **N.G.**

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### Chapter 3.6 – Design

- **Example 3.12:**
- $A_e = A_n U = U(A_g - A_{holes}) \therefore A_g = \frac{A_e}{U} + A_{holes}$
- $A_g = \frac{3.323 \text{ in}^2}{0.80} + (\frac{1}{2} \text{ in.})(1 \text{ in.})(2 \text{ holes}) = 5.15 \text{ in}^2$

Table 1-7  
Angles  
Properties

Shape	k	Wt. A	Axis X-X					Flexural-Torsional Properties				
			I	S	r	$\bar{y}$	Z	J	$C_w$	$r_z$		
L7x4x3/4	1 1/4	26.2	7.74	37.8	8.39	2.21	2.50	14.8	1.84	1.47	3.97	3.31
x3/4	1 1/4	23.8	6.92	33.8	7.12	2.08	2.45	12.5	1.68	0.866	2.97	2.94
x3/8	1 1/4	17.0	5.26	23.6	5.79	2.25	2.40	10.2	1.74	0.456	1.25	3.37
x1/2	1 1/4	13.6	4.00	20.5	4.42	2.27	2.35	7.81	1.67	0.198	0.544	3.40

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### Chapter 3.6 – Design

- **Example 3.12:**
- Let's try a **L7 x 4 x 1/2**  $A_g = 5.26 \text{ in}^2$

Table 1-7  
Angles  
Properties

Shape	k	Wt. A	Axis X-X					Flexural-Torsional Properties				
			I	S	r	$\bar{y}$	Z	J	$C_w$	$r_z$		
L7x4x3/4	1 1/4	26.2	7.74	37.8	8.39	2.21	2.50	14.8	1.84	1.47	3.97	3.31
x3/4	1 1/4	23.8	6.92	33.8	7.12	2.08	2.45	12.5	1.68	0.866	2.97	2.94
x3/8	1 1/4	17.0	5.26	23.6	5.79	2.25	2.40	10.2	1.74	0.456	1.25	3.37
x1/2	1 1/4	13.6	4.00	20.5	4.42	2.27	2.35	7.81	1.67	0.198	0.544	3.40

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### Chapter 3.6 – Design

- **Example 3.12:**
- Let's try a **L7 x 4 x 1/2**  $A_g = 5.26 \text{ in}^2$   $r_{\min} = 0.866 \text{ in}$

Table 1-7 (continued)  
Angles  
Properties  
L12-L7

Shape	Axis Y-Y					Axis Z-Z					Tan α
	I	S	r	$\bar{x}$	Z	I	S	r	Tan α		
L7x4x1/2	9.00	3.01	1.08	1.00	5.60	0.553	5.63	2.56	0.855	0.324	
x3/4	7.79	2.50	1.10	0.956	4.69	0.494	4.61	2.17	0.866	0.363	
x3/8	6.48	2.10	1.11	0.910	3.77	0.376	3.94	1.75	0.886	0.354	
x1/2	5.17	1.69	1.12	0.865	2.91	0.331	3.39	1.33	0.895	0.337	
x3/8	5.06	1.61	1.12	0.861	2.84	0.286	3.04	1.33	0.873	0.339	

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### Chapter 3.6 – Design

- **Example 3.12:**
- Let's try a **L7 x 4 x 1/2**  $A_g = 5.26 \text{ in}^2$   $r_{\min} = 0.866 \text{ in}$
- $A_n = A_g - A_{holes} = 5.26 \text{ in}^2 - (\frac{1}{2} \text{ in.})(1 \text{ in.})(2 \text{ holes}) = 4.260 \text{ in}^2$
- $A_e = A_n U = (0.80)4.260 \text{ in}^2 = 3.408 \text{ in}^2$
- Is  $A_e >$  required  $A_e$ ?  $3.408 \text{ in}^2 > 3.323 \text{ in}^2$  **O.K.**
- Is  $r_{\min} >$  required  $r_{\min}$ ?  $0.866 \text{ in} > 0.48 \text{ in}$  **O.K.**

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### Chapter 3.6 – Design

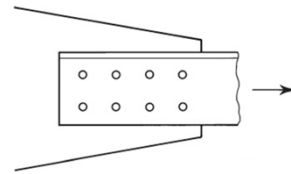
Let's work on some problems



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### Chapter 3.6 – Design

- **Example 3.13:** Repeat Example 3.12 with the aid of the design tables in *Part 5 of the Manual*.
- Select an unequal-leg angle tension member 12 ft. long to resist a service dead load of 35 k and a service live load of 75 k.
- Use **A572 Grade 50** with two lines of 7/8-in bolts.



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### Chapter 3.6 – Design

- **Example 3.13:** Repeat Example 3.12 with the aid of the design tables in *Part 5 of the Manual*. **LRFD** Solution

$$P_u = 1.2D + 1.6L = 1.2(35k) + 1.6(75k) = 162 k$$

$$r_{min} \geq 0.600 \text{ in.}$$

- Design tables of tension members give values of  $A_g$  and  $A_e$  for various shapes based on the assumption that  $A_e = 0.75A_g$ .
- In addition, the corresponding available strengths based on **yielding** and **rupture** are given.
- All values available for angles are for **A572 Grade 50** steel.

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### Chapter 3.6 – Design

- **Example 3.13:**

$$L7 \times 4 \times 7/16$$

$$A_g = 4.63 \text{ in}^2$$

Shape	Gross Area, $A_g$	Yielding				Rupture, $A_n = 0.75A_g$							
		kips		kips		kips		kips					
		$P_t / \Omega_t$	$\phi_t P_t$	$P_t / \Omega_t$	$\phi_t P_t$	$P_t / \Omega_t$	$\phi_t P_t$	$P_t / \Omega_t$	$\phi_t P_t$				
in <sup>2</sup>		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD				
L12x12x1 1/2	31.1	931	1400	757	1140	L7x4x1/2	7.74	232	345	189	283		
	x1/4	28.4	859	1300	682		1040	x1/4	6.99	195	293	159	238
	x1/8	25.8	772	1160	631		946	x1/8	6.26	167	251	151	221
	x1	23.0	689	1040	562		843	x1	5.54	147	216	137	201
L10x10x1 1/2	25.8	766	1150	624	806	L7x4x1/4	4.00	115	169	102	150		
	x1/4	23.4	701	1050	572		688	L6x3x1/4	11.0	329	495	268	402
	x1/8	21.3	638	959	520		780	x1/4	9.75	282	439	238	356
	x1	19.0	569	855	465		697	x1/8	8.46	253	381	208	310
L8x8x1 1/2	18.8	503	756	410	614	L6x3x1/2	6.45	189	290	157	236		
	x1/4	14.5	434	653	354		531	x1/2	5.77	163	249	141	211
	x1/8	13.3	398	599	324		487	x3/8	5.08	152	229	124	188
	x1	11.5	344	518	280		421	x1/4	4.38	131	197	107	160
L6x6x1 1/2	9.89	290	436	236	354	L6x3x1/4	3.67	110	165	93.4	134		
	x1/4	8.77	263	395	214		321	x1/8	3.00	84.0	126	69.5	103
	x1/8	8.00	240	360	195		293	x1/4	2.67	74.0	111	61.4	91.4
	x1	7.84	238	354	191		287	x1/8	2.86	77.0	114	64.0	94.0

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### Chapter 3.6 – Design

- **Example 3.13:** From the dimensions and properties tables in *Part 1 of the Manual*:

$$L7 \times 4 \times 7/16 \quad A_g = 4.63 \text{ in}^2 \quad r_{min} = 0.869 \text{ in.}$$

- To check this selection, we must compute the actual net area. If we assume that  $U = 0.80$

$$A_n = A_g - A_{holes} = 4.63 \text{ in}^2 - \left(\frac{7}{16} \text{ in.}\right)(1 \text{ in.})(2 \text{ holes}) = 3.754 \text{ in}^2$$

$$A_e = A_n U = (0.80)3.754 \text{ in}^2 = 3.003 \text{ in}^2$$

$$\phi_t P_n = \phi_t F_u A_e = 0.75(65 \text{ ksi})(3.003 \text{ in}^2) = 146.4 k < 162 k \quad \text{N.G.}$$

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### Chapter 3.6 – Design

- **Example 3.13:** From the dimensions and properties tables in *Part 1 of the Manual*:

$$L7 \times 4 \times 7/16 \quad A_g = 4.63 \text{ in}^2 \quad r_{min} = 0.869 \text{ in.}$$

- This shape did not work because the ratio of  $A_e$  to  $A_g \neq 0.75$ .

$$\text{The ratio is: } \frac{3.003 \text{ in}^2}{4.630 \text{ in}^2} = 0.648$$

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### Chapter 3.6 – Design

- **Example 3.13:** From the dimensions and properties tables in *Part 1 of the Manual*:
- This corresponds to a required  $\phi_t P_n$  (based on rupture) of:
 
$$\frac{0.75}{\text{actual ratio}} \times P_u = \frac{0.75}{0.648} \times 162k = 187.5k$$

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### Chapter 3.6 – Design

- **Example 3.13:**

**L7 x 4 x 1/2**

$A_g = 5.26 \text{ in}^2$

Rupture on net section  
 $\phi_t P_n = 193k$

Yielding on gross section  
 $\phi_t P_n = 237k$

Table 5-2  
Available Strength in Axial Tension

$F_y = 50 \text{ ksi}$   
 $F_u = 65 \text{ ksi}$

Angles  $P_u > 187.5k$

Shape	Gross Area, $A_g$	Yielding			Rupture, $A_n = 0.75A_g$			Shape	Gross Area, $A_g$	Yielding			Rupture, $A_n = 0.75A_g$		
		$P_u$	$P_u$	$P_u$	$P_u$	$P_u$	$P_u$			$P_u$	$P_u$	$P_u$	$P_u$	$P_u$	
	in <sup>2</sup>	ADD	LFRD	ASD	LFRD	ASD			in <sup>2</sup>	ADD	LFRD	ASD	LFRD	ASD	
L7x4x1/2	5.26	1400	787	1140	1140	787	L7x4x1/2	5.26	1400	787	1140	1140	787	787	
		kips	kips	kips	kips	kips			kips	kips	kips	kips	kips	kips	

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### Chapter 3.6 – Design

- **Example 3.13:**
- The actual effective net area and rupture strength are computed as follows:
 
$$A_n = A_g - A_{holes} = 5.26 \text{ in}^2 - (\frac{1}{2} \text{ in.})(1 \text{ in.})(2 \text{ holes}) = 4.26 \text{ in}^2$$

$$A_e = A_n U = (0.80)4.26 \text{ in}^2 = 3.408 \text{ in}^2$$

$$\phi_t P_n = \phi_t F_u A_e = 0.75(65 \text{ ksi})(3.408 \text{ in}^2) = 166.1k > 162k \quad \text{OK}$$
- Use an **L7 x 4 x 1/2** connected through the 7-inch leg.

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### Chapter 3.6 – Design

Let's work on some problems

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### Chapter 3.6 – Design

Any questions?

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