- ➤ Influence lines are important in the design of structures that resist large live loads.
- In our work up to this point, we have discussed analysis techniques for structures subjected to *dead* or *fixed loads*.

### **Influence Lines**

- We learned that shear and moment diagrams are important in determining the maximum internal force in a structure.
- If a structure is subjected to a *live* or *moving load*, the variation in shear and moment is best described using *influence lines*.

# **Influence Lines**

Consider a transport truck moving over a simply-support bridge beam.



# **Influence Lines**

Definition of an influence line:

An *influence line* represents the variation of the reaction, shear, moment, or deflection at a *specific point* in a member as a concentrated force moves over the member.

#### **Influence Lines**

- Once the *influence line* is drawn, the location of the live load which will cause the greatest influence on the structure can be found very quickly.
- Therefore, *influence lines* are important in the design of a structure where the loads move along the span (bridges, cranes, conveyors, etc.).

#### **Influence Lines**

Although the procedure for constructing an *influence line* is rather simple, it is important to remember the difference between constructing an influence line and constructing a shear or moment diagram

- Influence lines represent the effect of a moving load only at a specified point on a member.
- Whereas shear and moment diagrams represent the effect of fixed loads at all points along the member.

#### Influence Lines

**Tabular Procedure** for determining the *influence line* at a point **P** for any function (reaction, shear, or moment).

- Place a unit load (a load whose magnitude is equal to one) at a point, x, along the member.
- Use the equations of equilibrium to find the value of the function (reaction, shear, or moment) at a specific point P due the concentrated load at x.

#### **Influence Lines**

**Tabular Procedure** for determining the *influence line* at a point **P** for any function (reaction, shear, or moment).

- 3. Repeat Steps 1 and 2 for various values of *x* over the whole beam.
- 4. Plot the values of the reaction, shear, or moment for the member.

# **Influence Lines**

**Influence-Line Equations Procedure** for determining the *influence line* at a point **P** for any function (reaction, shear, or moment).

- 1. Place a unit load (a load whose magnitude is equal to one) at a point, *x*, along the member.
- Use the equations of equilibrium to find the value of the reaction, shear, or moment at a specific point P due the concentrated load as a function of x.

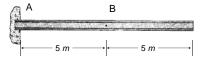
#### Influence Lines

**Influence-Line Equations Procedure** for determining the *influence line* at a point **P** for any function (reaction, shear, or moment).

3. Plot the values of the reaction, shear, or moment for the member.

#### Influence Lines

**Example:** Let's draw an *influence line* for the reaction, shear, and moment for both points A and B using the tabular method.



Example: First, let's construct the influence line for the vertical reaction at point A



$$\begin{array}{c}
M_A \\
\uparrow \\
A_y
\end{array}$$

$$^{+}$$
  $\sum F_{y} = 0 = A_{y} - 1$ 

$$A_{\rm v} = 1$$

# **Influence Lines**

 $\textit{Example}\!:$  First, let's construct the influence line for the vertical reaction at point A



$$\begin{array}{c|c}
M_A & 1 \\
\hline
& x = 5 m
\end{array}$$

$$^{+}\uparrow\sum F_{y}=0=A_{y}-1$$

$$A_{v} = 1$$

# **Influence Lines**

Example: First, let's construct the influence line for the vertical reaction at point A



$$\begin{array}{c}
M_{A} \\
\downarrow \\
A_{A}
\end{array}$$

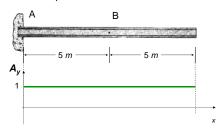
$$\begin{array}{c}
1 \\
x = 10 \ m
\end{array}$$

$$^{+}$$
  $\uparrow$   $\sum F_{y} = 0 = A_{y} - 1$ 

$$A_{y} = 1$$

# **Influence Lines**

Example: First, let's construct the influence line for the vertical reaction at point A



# **Influence Lines**

Example: Construct the influence line for the bending moment at point A





$$O^{+}\sum M_{A} = 0 = -M_{A} - 1(0 m)$$
  $M_{A} = 0$ 

# **Influence Lines**

Example: Construct the influence line for the bending moment at point A





$$O^{+}\sum M_{A} = 0 = -M_{A} - 1(3 m)$$
  $M_{A} = -3 m$ 

Example: Construct the influence line for the bending moment at point A



$$M_{A} \longrightarrow 1 \qquad x = 6 m$$

$$O^{+}\sum M_{A} = 0 = -M_{A} - 1(6 m)$$
  $M_{A} = -6 m$ 

$$M_{\rm A} = -6 \ m$$

### Influence Lines

Example: Construct the influence line for the bending moment at point A



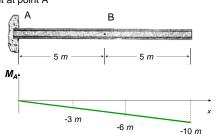
$$\begin{array}{c}
M_{A} \\
\uparrow \\
A_{A}
\end{array}$$

$$\begin{array}{c}
1 \\
x = 10 \text{ m}
\end{array}$$

$$O^{+}\sum M_{A} = 0 = -M_{A} - 1(10 \text{ m})$$
  $M_{A} = -10 \text{ m}$ 

# **Influence Lines**

Example: Construct the influence line for the bending moment at point A



# **Influence Lines**

Example: Construct the influence line for the shear at point B

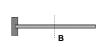




$$^{+}$$
  $\uparrow$   $\sum F_y = 0 = A_y - 1$ 

# **Influence Lines**

**Example**: Construct the *influence line* for the shear at point B



$$M_A$$
 $x$ 
 $\downarrow$ 
 $1$ 
 $5 m$ 
 $V_B$ 

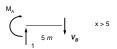
$$^{+}$$
  $\sum F_{y} = 0 = -V_{B} - 1 + 1$ 

$$V_{\rm R} = 0$$

# **Influence Lines**

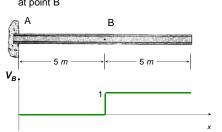
**Example**: Construct the *influence line* for the shear at point B





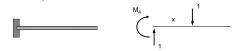
$$^{+}$$
  $\sum F_{y} = 0 = -V_{B} + 1$ 

**Example**: Construct the *influence line* for the shear at point B



# **Influence Lines**

**Example**: Construct the **influence line** for the bending moment at point B



$$O^+\sum M_A=0=-M_A-1x$$

 $M_A = -x$ 

# **Influence Lines**

**Example**: First, let's construct the *influence line* for the bending moment at point B



$$O^{+}\sum M_{cut} = 0 = M_{B} + x - 5 + (5 - x)$$

 $M_{\rm B} = 0$ 

# **Influence Lines**

**Example**: First, let's construct the **influence line** for the bending moment at point B

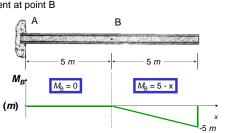


$$O^{+}\sum M_{cut} = 0 = M_{B} + x - 5$$

$$M_{\rm B} = 5 - {\rm x}$$

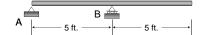
# **Influence Lines**

**Example**: Construct the *influence line* for the bending moment at point B



# **Influence Lines**

Example : Construct the influence line for the reaction at B



Example: Construct the influence line for the shear at C



### Influence Lines

Example: Construct the influence line for the moment at C

$$A \stackrel{C}{\longleftarrow} B \\ \longleftarrow 5 \text{ ft.} \longrightarrow \longleftarrow 5 \text{ ft.} \longrightarrow \longleftarrow 5 \text{ ft.} \longrightarrow$$

# **Influence Lines**

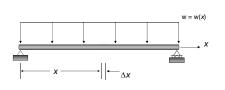
- Since beams or girders are usually major loadcarrying members in large structures, it is important to draw *influence lines* for reaction, shear, and moment at specified points.
- Once an *influence line* has been drawn, it is possible to locate the live loads on the beam so that the maximum value of the reaction, shear, or moment is produced.
- > This is very important in the design procedure.

# **Influence Lines**

**Concentrated Force** - Since we use a unit force (a dimensionless load), the value of the function (reaction, shear, or moment) can be found by multiplying the ordinate of the influence line at the position x by the magnitude of the actual force  $\mathbf{P}$ .

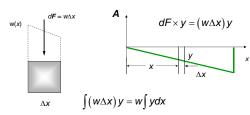
### Influence Lines

**Uniform Force -** consider the portion of the beam  $\Delta x$ 

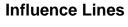


# **Influence Lines**

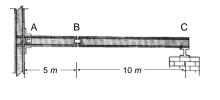
Let's examine the interval  $\Delta x$ 



 $\int y dx$  is the area under the influence line

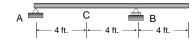


**Example:** The beam below is subject to a dead load of 1.5 kN/m and a single live load of 10 kN. Determine the maximum **negative** moment created by these loads at point A and the maximum **positive** shear at point B.



# **Influence Lines**

**Example**: Determine the maximum **positive** moment that can be developed at point C on the beam shown below due to a single concentrated live load of 8 k, a uniform live load of 3 k/ft., and a beam weight (dead load) of 1 k/ft.



# **End of Influence Lines - Part 1**

Any questions?

